



Tho. Dilworth
Schoolmaster

H. Gravelot delin.

H. Burgh Sculp.



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THE
Schoolmasters Assistant:
BEING A
Compendium of ARITHMETIC,
BOT H
Practical and Theoretical.

In Four PARTS.

CONTAINING,

I. Arithmetic in Whole Numbers, wherein all the common Rules, having each of them a sufficient Number of Questions, with their Answers, are methodically and briefly handled.	III. Decimals, in which, among other Things, are considered the Extraction of Roots; Interest, both Simple and Compound; Annuities; Rebate, and Equation of Payments.
II. Vulgar Fractions, wherein several Things, not commonly met with, are there distinctly treated of, and laid down in the most plain and easy Manner.	IV. A large Collection of Questions, with their Answers, serving to exercise the foregoing Rules; together with a few others, both pleasant and diverting.

The WHOLE,

Being delivered in the most familiar Way of *Question* and *Answer*, is recommended by several eminent *Mathematicians*, *Accomptants* and *Schoolmasters*, as necessary to be used in *Schools* by all Teachers, who would have their *Scholars*, thoroughly understand, and make a quick Progress in ARITHMETIC.

To which is prefixt,

An ESSAY on the *Education of YOUTH*, humbly offer'd to the Consideration of PARENTS.

The Second Edition.

By THOMAS DILWORTH,
• AUTHOR of the

New Guide to the English Tongue; and *Schoolmaster in Wappin*.

All Things, which from the very first Original Being of Things, have been framed and made, do appear to be framed by the Reason of Number; for this was the principal Example or Pattern in the Mind of the C R E A T O R.

Anitius Boetius.

Thou [O L O R D] hast ordered all Things in Measure, Number, and Weight.

Wisdom xi. 20.

L O N D O N:

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THE
PREFAGE Dedicatory.

To the Reverend and Worthy

SCHOOLMASTERS
IN
GREAT BRITAIN and IRELAND.

GENTLEMEN,

 *FTER returning You my most hearty
Thanks for Your kind Acceptance of my
New Guide to the English Tongue,
permit me to lay before You the following
Pages, which are intended as an Help towards a
more speedy Improvement of Your Scholars in
Numbers, and at the same time, to take off that
heavy Burden of writing out Rules and Questions,
which You have so long labour'd under.*

*I need not, I presume, say any thing concerning
the Usefulness of, and Advantages that accrue to
Mankind in general, from Arithmetic, since they
are by this time, pretty well known; and also deserve
the Employment of a much better Pen than mine can
pretend to be; but I will venture to say thus much,
and I believe You will pardon me for it, that THIS
(by putting one into each Arithmetician's Hand) will
not only prove a kind ASSISTANT to You, but,
upon Trial, be found at once, both to delight and im-
prove the Minds of those who are committed to Your
Care.*

iv The PREFACE Dedicatory.

I have gone through all the Parts of Arithmetic, commonly taught in Schools, and have included several others no less Useful: And though I have given more Questions to work upon in each Rule, (which was absolutely necessary; none having yet calculated their Performances, of this Kind, for the Use of School-Boys) I have endeavoured at the same time to reduce the Whole, to as neat and portable a Volume, as any that have gone before me.

I must confess, I do not propose by THIS, to add to any Master's Knowledge in Arithmetic, who, I imagin, is already acquainted with every thing contained in this Compendium; for which Reason it is reduced to the narrow Compass it now appears in, without particular Directions for working the Operations at large; and therefore, I conceive, here is room enough left for every Man to speak his own Mind, and instruct his Pupils in his own Method. And,

I believe, it is confess'd by All, that it is a Task too hard for Children to be made compleat Masters of Arithmetic; and therefore the best Way of instructing them in it, is, most certainly, to give them a general Notion of it in the easiest Manner, and to enlarge upon it afterward, if there be Time; otherwise it must be done by themselves, as their Increase in Years, and Growth in Understanding will permit. * " For Arithmetic is the more valuable, " as it is the more exact, easy and short; and the " Art lies in giving as few Rules as possible, and " clearly explaining them; and not confounding " Principles together, and then diversifying them " into several Rules, when they are built on the " same Reason, which has not only made Arith-

* WATTS's Essay.

" metic

The P R E F A C E Dedicatory.

"metic seem difficult of Access, but has hinder'd
many from being Accomptants."

To enter into a Detail of the following Particulars, would be tedious, and swell this Preface beyond its just Limits; but that the kind Reader may not be wholly at a Loss, I shall beg Leave to speak as follows, viz.

1. That the Whole is divided into Four Parts, as the Title-Page expresses it.

2. That the Rules and Examples are contrived in the easiest Manner, and the Whole put in such an easy Method, as is no where else extant.

3. I have omitted Reduction of Foreign Coins, partly because all those Tables, which I have met with, which shew the Value of Foreign Coin in English Mony, are very erroneous; but principally because all such Questions as relate to the turning of the Mony of one Country into that of another, are much better answered under the Head of Exchange. For the Value of Foreign Species (such I mean as relate only to Exchange) both of Gold and Silver, in every Country is unsettled, and therefore such Coins are subject to vary in their Prices, as the Merchants find an Opportunity to profit by them. Hence proceed the various Courses of Exchange; and from them again, the particular Worth of any Quantity of Foreign Coin in English Mony, which is sometimes more, sometimes less, according as the Course of Exchange runs at that Time when such Foreign Coin becomes due. Add to this the Agio or Advance-Mony, usually paid Abroad on the changing Current Mony into Exchange or Bank-Mony, which is 2, 3, or more per Cent. in Payment, according to what the Exchange or Bank-

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Mony is worth more than the Current Mony, and this cannot be done otherwise than by the Rule of Three.

4. In Interest, &c. by Decimals, I have follow'd Mr. WARD's Method, by which Means the Rule is drawn into a much narrower Compass; and appears more beautiful to the Eye than in Words at length.

5. In all Places where it could be done conveniently, I have given Directions for varying the Examples by way of Proof; because it not only discovers the Reason of the Operation, but at the same Time both produces a new Question, and proves the old One. And sure I am, that the varying the Question, when it may be done under the same Rule, contributes very much towards a thorough Understanding of it, and making a good Accomptant, as every one's Experience will teach him.

6. I have thrown the Subject of the following Pages into a Catechetical Form, that they may be the more instructive; for Children can better judge of the Force of an Answer, than follow Reason thro' a Chain of Consequences. Hence also it proves a very good examining Book; for at any Time, in what Place soever the Scholar appears to be defective, he can immediately be put back to that Place again, without the formal Way of beginning every Thing anew. And,

7. In order to make the Progress still quicker, every Example, to be wrought, hath its Answer annexed to it: So that they who do not chuse to have every Operation proved by varying the Question, may know without it, whether the Work be right or not.

And now after all, it is possible that some, who like best to tread the old beaten Path, and to sweat

at

at their Business when they may do it with Pleasure, may start an Objection against the Use of this well-intended Assistant, because the Course of Arithmetic is always the same; and therefore say, That some Boys lazily inclined, when they see another at work upon the same Question, will be apt to make his Operation pass for their own: But these little Forgeries are soon detected by the Diligence of the Tutor: Therefore, as different Questions to different Boys, do not in the least promote their Improvement: So neither do the same Questions hinder it. Neither is it in the Power of any Master (in the Course of his Business) how full of Spirits soever he be, to frame new Questions at Pleasure in any Rule, but the same Questions will frequently occur in the same Rule, notwithstanding his greatest Care and Skill to the contrary.

It may also be further objected, That to teach by a printed Book, is an Argument of Ignorance and Incapacity, which is no less trifling than the former. He indeed (if any such there be) who is afraid his Scholars will improve too fast, will undoubtedly decry this Method: But that Master's Ignorance can never be brought in question, who can begin and end it readily; and most certainly that Scholar's Non-improvement can be as little questioned, who makes a much greater Progress by This, than by the common Method.

As to the Order of the Rules, I can hardly find two Masters follow it alike; some liking best to teach that Rule first, which another thinks more convenient to teach afterward; while a third looks upon it as a Matter quite indifferent, among some Rules, which he teaches first. But this need be no Hindrance:

viii The P R E F A C E Dedicatory.

drance to the Use of this Book. For however the Rules are placed here, every Man may turn to that Rule first, which he likes should be taught first; and if a Master have a mind to teach Vulgar Fractions immediately after Reduction in Whole Numbers, as some do, he may do it as easily, as in the Order they now lie.

I should have been very glad to have seen an Attempt of this Nature, stampt by the Authority of some Person of Distinction, and of better Abilities; but since no abler Hand has undertaken it, I hope its homely Appearance will not lessen its Usefulness.

The Printer's Errors, as well as my own Defects, I hope will candidly be overlook'd: But because a Man's Failings are so familiar to himself, that he can scarce discern them; therefore the kind Admonitions of a good-natur'd Reader, shall always be very acceptable.

I have nothing more to add, but my repeated Thanks for Favours received, together with my earnest Desire that you may be prosperous in Your several Undertakings, and to beg this additional Favour of being esteemed,

GENTLEMEN,

Your most humble, and

most obedient Servant,

THOMAS DILWORTH.

ON THE
Education of YOUTH;
A. N.
ESSAY
Humbly offer'd to the Consideration of
PARENTS.

THE right Education of Children, is a Thing of the highest Importance, both to Themselves and the Common-wealth. It is this, which is the natural Means of preserving Religion and Virtue in the World: And the earlier good Instructions are given, the more lasting will be their Impression. For it is as unnatural to deny these to Children, as it would be to with-hold from them their necessary Sustenance. And happy are all those, who, by a religious Education and watchful Care of their Parents, their wise Precepts and good Examples, have contracted such a Love of Virtue and hatred of Vice, as to be removed out of the Way of Temptations. And 'tis owing to the Want of this Education, that many, when they leave their Schools, do not prove so well qualified as might be expected. This great Omission being for the most part chargeable on the Parents, I hope the following Particulars (which are the common Voice of our Profession) will not be taken amiss. And,

1. A constant Attendance at School is one main Axis whereon the great Wheel of Education turns. Therefore if that Observation, which is commonly made by Parents be true, That the Masters have

Holidays enough of their own making, *there is, by their own Confession, no Necessity for them to make an Addition.*

2. Parents should never let their own Commands run counter to the Master's, but whatever Task be imposes on his Pupils to be done at Home, they should be careful to have it perform'd in the best Manner, in order to keep them out of Idleness.

“ * For vacant Hours move on heavily, and drag Rust and Filth along with them ; and ‘tis full Employment, and a close Application to Busines, that is the only Barrier to keep out the Enemy, and save the future Man.”

3. Parents should endeavour to be sensible of their Childrens Defects and want of Parts ; and not blame the Master for Neglect, when his greatest Skill, with some, will produce but a small Share of Improvement. But the great Misfortune is, as the Proverb expresses it ; Every Bird thinks her own Young the fairest : And the tender Mother, tho' her Son be of an ungovernable Temper, will not scruple to say, He is a meek Child, and will do more with a Word than a Blow, when neither Words nor Blows are available. On the other Hand, some Children are of a very dull and heavy Disposition ; and are a long Time in gathering but a little Learning, and yet their Parents think them as capable of Instruction, as those who have the most bright and promising Parts : And when it happens that they improve but slowly, tho' it be in Proportion to their own Abilities, they are burried about from School to School, till at last they lose that Share of Learning, which otherwise, by staying at the same School they might have been Masters

of. Just like a sick, but impatient Man, who employs a Physician to cure him of his Malady ; and then, because the Distemper requires Time, as well as Skill to procure his Health, tells him, He has all along taken a wrong Method ; turns him off ; and then applics to another whom he serves in the same Manner ; and so proceeds till the Distemper proves incurable.

4. It is highly necessary that Children should be early made sensible of the Scandal of telling a Lye : To that End Parents must inculcate upon them, betimes, that most necessary Virtue of speaking Truth, as one of the best and strongest Bands of human Society and Commerce, and the Foundation of all Moral Honesty.

5. Injustice (I mean the Tricking each other in Trifles which so frequently happens among Children, and is very often countenanced by the Parents, and looked on as the Sign of a very promising Genius) ought to be discouraged betimes, lest it should betray them into that vile Sin of pilfering and purloining in their riper Years ; to which the grand Enemy of Mankind is not wanting to prompt them by his Suggestions, whenever he finds their Inclinations have a Tendency that Way.

6. Immoderate Anger and desire of Revenge, must never be suffered to take Root in Children. For (as a most Reverend Divine observes) * " If any of these be cherished, or even let alone in them, they will in a short Time grow headstrong and unruly ; and when they come to be Men, will corrupt the Judgment, and turn good Nature into Humour, and Understanding into Prejudice and Wilfulness."

* A. B. TILLOTSON.

7. Children are very apt to say at Home what they see and hear at School, and oftentimes more than is true, and some Parents, as often, are weak enough to believe it. Hence arise those great Un-easinesses between the Parents and the Master, which sometimes are carried so high, as for the Parent, in the Presence of the Child, to reproach him with hard Names, and perhaps with more abusive Language. On the contrary,

8. If Parents would have their Children improve in their Learning they must cause them to submit to the little (imaginary) Hardships of the School, and support them under them by suitable Encouragements. They should not fall out with the Master upon every idle Tale, nor even give their Children the Liberty of expressing themselves that way; but they should, by all Means, inform them frequently, That they ought to be good Boys, and learn their Book, and always do as their Master bids them, and that if they do not, they must undergo the Pain of Correction. And it is very observable what a Harmony there is between the Master and the Scholar, when the latter is taught to love and have a good Opinion of the former; and then With what Ease does the Scholar learn! With what Pleasure does the Master communicate!

9. The last Thing that I shall take Notice of is, That while the Master endeavours to keep Peace, good Harmony, and Friendship among his Scholars, they are generally taught the Reverse at Home,
* " It is indeed but too common for Children to
" encourage one another, and be encouraged by
" their Friends in that Savage and Brutal Way
" of Contention, and to count it an hopeful Sign

* TALBOTT's Christian Schoolmaster.

of

“ of Mettle in them to give the *last Blow*, if not
“ the *first*, where-ever they are provoked ; for-
“ getting at the same Time, that to teach *Chil-*
“ *dren* betimes to love and be good natured to-
“ others, is to lay early the true Foundation of
“ an *honest Man*. Add to this, that *cruel Delight*
“ which some are seen to take in tormenting and
“ worrying such poor *Animals* as have the Mis-
“ fortune to fall into their Hands. But *Children*
“ should not only be restrained from such *barba-*
“ *rrous Diversions*, but should be bread up from the
“ Beginning to an Abhorrence of them,” and at
the same Time be taught that great Rule of Huma-
nity, *To do to others, as we would they should do to us.*

From what has been said relating to the Management of Children at Home ; the Necessity of the Parents joining Hands with the Schoolmaster appears very evidently. For when the Master commands his Pupils to employ their leisure Time in getting some necessary Parts of Learning ; their Friends should not command them to forbear : And when they ought to be at School at the stated Hours, they should not be sent an Hour or two after, in the Time of Health, sometimes with a Lye in their Lips to excuse their Tardiness ; and sometimes with an Order, and a brazen Front to tell their Master, Their Friends think it Time enough to come to School at Nine in the Morning, because the Weather is a little Cold, or because they must have their Breakfast first. I say, Parents should not act so indiscreetly, because it clips the Wings of the Master’s Authority : It makes Boys first despise and undervalue their Teachers, and then become unmannerly and impertinent to them ; Correction for which

which, makes the Tutor hated by the Children, and then there naturally follows either a total disregard to Business, or a general Carelessness in every Thing they do. And

While I am speaking of the Education of Children, I hope I shall be forgiven, if I drop a Word or two relating to the fair Sex.— It is a general Remark that they are so unhappy as seldom to be found either to Spell, Write, or Cypher well: And the Reason is very obvious; because they do not stay at their Writing Schools long enough. A Year's Education in Writing is by many thought enough for a Girl; and by others it is thought Time enough to put them to it, when they are Eighteen or Twenty Years of Age; whereas by sad Experience, both these are found to be, the one too short a Time, and the other too late. The first is a Time too short, because, when they are taken from the Writing School, they generally forget what they learnt for want of Practice: And the other is too late, because then they are apt to look too forward, imagin all Things will come of themselves without any trouble, and think they can learn a great deal in a little Time; and when they find they cannot compass their Ends so soon as they would, then every little Difficulty discourages them: And hence it is that adult Persons seldom improve in the first Principles of Learning so fast as younger Ones. For a Proof of these, I appeal to every Woman, whether I am just in my Sentiments or not. The Woman who has had a liberal Education this Way, knows the Advantages that arise from the ready Use of the Pen; and the Woman who has learnt little or nothing of it, cannot but lament the Want of it. Girls therefore ought to be

put

put to the Writing School as early as Boys, and continued in it as long, and then it may reasonably be expected that both Sexes should be alike ready at their Pen. But for want of this, How often do we see Women, when they are left to shift for themselves in the melancholy State of Widowhood, (and what Woman knows that she shall not be left in the like State?) obliged to leave their Business to the Management of others ; sometimes to their great Loss, and sometimes to their utter Ruin ; when, on the contrary, had they been ready at their Pen, could Spell well, and understand Figures, they might not only have saved themselves from Ruin, but perhaps have been Mistresses of a good Fortune ? Hence then, may be drawn the following, but most natural Conclusion, viz. * " The Education of Youth is " of such vast Importance, and of such singular " Use in the Scene of Life, that it visibly carries " its own Recommendation along with it : For " on it, in a great Measure depends all that we " hope to be ; every Perfection that a generous " and well-disposed Mind would gladly arrive at : " 'Tis this that stamps the Distinction of Mankind, and renders one Man preferable to another : Is almost the very Capacity of doing well ; and remarkably adorns every Point of Life." And as the great End of human Learning is to teach a Man to know himself, and thereby fit him for the Kingdom of Heaven : So he that knows most, consequently is enabled to practise the best, and become an Example to those who know but little, or are quite ignorant of their Duty. I am,

Your and your Childrens Well-wisher,

* WATTS's Essay.

THOMAS DILWORTH.



To Mr. THOMAS DILWORTH,
ON HIS
Compendium of ARITHMETIC,
INTITLED,
The *Schoolmasters Assistant.*

WHILE some, seductive of the rising Age
Expose for Hire the lewd, or factious Page,
On ev'ry Stall appear the public Pest,
Deep Bane instilling in the tender Breast ;
Thou, Friend of moral as of social Truth !
Employ'st thy Toils to mend our growing Youth.
Thy Cares, how worthy of the Good and Wise,
Impow'r the Embrio-Genius firt to rise ;
Make the dark Clues of Science plain to find,
And thro' its Mazes lead the pleasur'd Mind.
E'en now afresh, unweary'd in thy Pains,
For future Times thy recent Task remains :
By double Motives it assures to please,
The Youth's Instructor, and the Tutor's Ease :
From darker Forms it clears encumber'd Rules,
And Learning makes the fit Delight of Schools.

Thy Labours, Friend, have found their just Success,
And gen'ral Plaudits thy Desert confess.
O may THIS WORK, nor THIS be found thy last,
No sordid Pride o'erlook, or Envy blast,
Far as our Mother-Tongue extends, be known,
And grateful Pupils thy Assistance own.

MOSES BROWNE.

To Mr. Thomas Dilworth, *Author of*
The Schoolmasters Assistant.

S I R,

As you was pleas'd to favour me with the Perusal of Your *Schoolmasters Assistant* in Manuscript, which gave me a sensible Pleasure; You have thereby obliged me, in Justice to your Merit, to give my humble Opinion upon it.— That a Work of *this Kind* has been long wanted, admits of no Dispute. And, I must confess, that you have treated the Subject so methodically, laid down the several Rules so very plain, yet concise, as must make this Book of general Use and Advantage: And I heartily wish you may meet with equal Encouragement in the Publication of this, as you did in Your excellent *New Guide to the English Tongue.* I am, S I R,

London, 29th of
November,
1742.

Your sincere Friend,

And humble Servant,

B R I G H T W H I L T O N.

To Mr. Thomas Dilworth, *on his*
Schoolmasters Assistant.

S I R,

I Have perused, with Pleasure, Your *Schoolmasters Assistant*, and give You my Thanks for Your kind Endeavours to further the Improvement of Youth with greater Facility to the Tutor.

I am convinced, *that Piece* is well calculated to promote both, and therefore wish You the Success due to so much useful Labour, I am,

S I R,

Twelve-Bell Court
in Bow Church-
Yard, 13 Jan.
1742.

Your Friend and Servant,

WILLIAM COLES.

To Mr. Thomas Dilworth, on his
Treatise of ARITHMETIC, intitled,
The Schoolmasters Assistant.

SIR,

IT is universally allow'd (in all Nations civiliz'd) that the Instruction of Youth is of the greatest Importance, the Happiness of every Individual, and Society in general thereon depending; and that it is of two Kinds, *viz.* To form the good Man and the good Scholar. To compleat the latter, those Studies are chiefly to be pursu'd, which are adequate to the Disposition of the Pupil, and to compleat the Man of Business he is design'd for: But I do not know any Business that can be well executed without ARITHMETIC. THIS therefore claims the first Place, and due Care of the Master, to inculcate and explain its Rudiments, which will not only ground the *Tyro*, but also give him some Glances of those Beauties and Uses, he may expect from his present Labours: Every Help then, that may gain the Master Time in the Discharge of his Duty, will (in consequence) add to the Improvement of his Scholars: For which Use and Purpose, that THIS Book is well adapted, (having perus'd it some Time ago in Manuscript) is the ingenuous Opinion of, SIR,

Gainsford-street, Sbast-
Thames, Southwark,
the 9th of May 1743.

Your respectful Friend and Servant,

WILLIAM MOUNTAINE.

To Mr. Thomas Dilworth, Author
of the Schoolmasters Assistant.

SIR,

I Have perus'd your Book, intitled, The Schoolmasters Assistant, and readily recommend it as a proper Companion for such as are employ'd in teaching ARITHMETIC, as well as for those who are desirous of Improvement in that useful and necessary SCIENCE. I am,

SIR,

The Academy in
Little Tower-
street, 29 March
1744.

Your humble Servant,

EM. AUSTIN.

WE whose Names are underwritten, having perused this Book, intitled, *The SCHOOLMASTERS ASSISTANT*, do recommend it to be used in SCHOOLS, for the speedy Improvement of YOUTH in ARITHMETIC, as the only one for that Purpose, that hath yet been made public.

Charles Bellenger, *M. A.*
Lecturer of Trinity, Minories, and Master of the Brewers-School in Seething-Lane.

Francis Chapman, *Writing-Master and Accomptant, in Shadwel.*

Francis Hopkins, *Writing-Master and Accomptant, in Cavendish-Court, near Devonshire-Square.*

John Loveday, *Schoolmaster at Stepney.*

Ebenezer Bramble, *Writing-Master and Accomptant, in Bull and Mouth-street, near Aldersgate.*

William Mercer, *Writing-Master at Maidstone.*

William Tully, *Master of the Boarding-School at Stanmore, in Middlesex.*

John Thorpe, *Master of one of the Corporation Schools at St. Edmunds Bury, Suffolk.*

Thomas Evans, *Schoolmaster at Hampstead.*

Richard Astell, *Writing-Master at Epsom.*

Robert Pierson, *Schoolmaster in Redcros-street.*

John Richardson, *Schoolmaster by London Wall.*

George Watts, *Schoolmaster in Penny-Fields, Poplar.*

Augustine Gradwell, *Master of Mr. Worral's Free-School in Cherry-Tree-Alley, Golden-Lane, St. Luke's.*

John Tuckett, *Writing-Master and Teacher of the Mathematics, at the Hand and Pen and Globe in New-street, near Fleet-street.*

George Caffey, *Schoolmaster in Whitechapel.*

Edward Rayne, *Schoolmaster, near the May-Pole, East-Smithfield.*

John Shortland, *Schoolmaster, near Salters-Hall, in St. Swithin's-Lane, Cannon-street.*



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P A R T IV.

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The



The Explication of some Marks used in this C O M P E N D I U M.

- = TWO Parallel Lines are the Marks of *Equality* ;
as, $12 \text{ oz.} = 1 \text{ lb.}$ signifies that 12 Ounces are *equal* to 1 Pound.
- + Saint George's Cross signifies *more*, or *Addition* ; as,
 $4 + 2 = 6$: i. e. 4 *more* 2, is *equal* to 6.
- A straight Line signifies *less*, or *Subtraction* ; as,
 $4 - 2 = 2$: i. e. 4 *less* 2, is *equal* to 2.
- × Saint Andrew's Cross denotes *Multiplication* ; as,
 $4 \times 2 = 8$: i. e. 4 *multiplied* by 2, is *equal* to 8.
- ÷ A Line between two Points, is the Sign of *Division* ; as,
 $4 \div 2 = 2$: i. e. 4 *divided* by 2, is *equal* to 2.
- ((The reverse Parenthesis denotes *Division* also ; as,
 $2)4(z$: i. e. 4 *divided* by 2, is *equal* to 2.

⁴⁷⁶¹
₃₂ Numbers placed in a Fraction-like manner, do likewise denote *Division* ; the lower Number being the *Divisor*, and the upper Number the *Dividend*.

:: Four Points, set in the middle of four Numbers, denote them to be proportional to one another, by the *Rule of Three* ; as, $2 \dots 4 :: 8 \dots 16$: that is, as 2 is to 4, so is 8 to 16.

Apothecaries Weights.

lb	Pounds.
oz	Ounces.
scr	Scruples.
dr	Drams.
$gr.$	Grains.

Motion.	
°	Degrees.
'	Minutes.
''	Seconds.

Explication of some Marks, &c.

$\overline{z + 3} \times 5 = 25$, Signifies that the Sum of z and 3 multiplied by 5, is equal to 25.

$\overline{3 - z} 2 \times 5 = 5$, Signifies that the Difference between 3 and z , multiplied by 5, is equal to 5.

\checkmark or $\checkmark q$. Prefixt to any Number, supposes that the *Square-Root* of that *Number* is required. Sometimes it is the Sign of *Irrationality*, and signifies that the *Square-Root* of such a *Number* can never be truly found.

$\checkmark c$. Prefixt to any Number, supposes that the *Cube-Root* of that *Number* is required. Sometimes it is the Sign of *Irrationality*, and signifies that the *Cube-Root* of such a *Number* can never be truly found.

$3 aa + 3 a$, Signifies 3 times the *Square* of a , more 3 times a .

$3 aae + 3 eea + eee$, Signifies 3 times the *Square* of a , multiplied by e , more 3 times the *Square* of e , multiplied by a , more the *Cube* of e , as in the *Cube-Root*.



THE



THE Schoolmasters Assistant.

P A R T I.

Of Arithmetic in Whole Numbers.

The INTRODUCTION.

Of Arithmetic in general.

Q.



HAT is Arithmetic?

A. *Arithmetic* is the Art or Science of computing by Numbers, either Whole or in Fractions.

Q. *What* is Number?

A. *Number* is one or more Quantities, answering to the Question, *How many*.

Q. *What* is *Arithmetic in Whole Numbers*?

A. *Arithmetic in Whole Numbers* or *Integers*, supposes its Numbers to be intire Quantities, and not divided into Parts.

Q. *What* is *Arithmetic in Fractions*?

A. *Arithmetic in Fractions*, supposes its Numbers to be the Parts of some intire Quantity.

Q. *How* do you consider *Arithmetic* with regard to *Art* and *Science*?

A. Both in *Theory* and *Practice*.

Q. *What* is *Theoretical Arithmetic*?

A. *Theoretical Arithmetic* considers the Nature and Quality of Numbers, and demonstrates the Reason of Practical Operations. And in this Sense *Arithmetic* is a *Science*.

Q. *What* is *Practical Arithmetic*?

A. *Practical Arithmetic* is that which shews the Method of working by Numbers, so as may be most useful and expeditious for Business. And in this Sense *Arithmetic* is an *Art*.

Q. *What* is the *Nature* of all *Arithmetical Operations*?

A. The *Nature* of all *Arithmetical Operations* is, by some Quantities that are given, to find out others that are required.

Q. *Which* are the *fundamental Rules* in *Arithmetic*?

A. These Five; *Notation*, *Addition*, *Subtraction*, *Multiplication*, and *Division*.

Of NOTATION.

Q. **W**HAT is Notation?

A. It is the Art of expressing Numbers by certain Characters or Figures.

Q. What is the Use of Notation?

A. Notation teaches to read and write Numbers by their true Value.

Q. How many Sorts of Characters or Figures are Numbers usually expressed by?

A. Two; viz. The Arabic Figures, and the Latin Letters.

Q. How are the Arabic Figures express'd?

A. The Arabic Figures are thus express'd; One 1, Two 2, Three 3, Four 4, Five 5, Six 6, Seven 7, Eight 8, Nine 9, Nought or Cypher 0. And this is the Notation or reading and writing of every single Figure.

Q. How far may the Use of these Figures be extended?

A. These Ten Characters or Figures may be used to express all manner of Numbers, from the least to the greatest, that can be conceived, even without End.

Q. How many Figures are sufficient to express most ordinary Concerns?

A. Nine; and therefore the Table of Notation commonly extends no farther than to nine Places.

Q. Why does it consist of nine Places, rather than of eight or ten?

A. Because they make up three even Periods.

Q. What do you mean by a Period?

A. A Period is a Quantity express'd by three Figures, whereof the first to the right Hand signifies so many Units, or single Things; the second so many Tens; and the third so many Hundreds.

Q. Why are three Figures called a Period?

A. Because if the Number be increased above three Places, there is still the same periodical Return of the Value of those Places, and every third Figure to the left Hand, will always be Hundreds, if it be never so far extended.

Q. Is an Unit or One, a Number?

A. An Unit is a Number, because it may properly answer the Question, How many?

Q. Give an Example or two.

A. How many Gods do we believe? The Answer is, One. How many Sundays in the compass of a Week? Answer, One.

Q. In what nature or proportion of Value, do Numbers increase from the Units Place, to the left Hand?

A. By Tens.

Q. How

Q. How must they be read?

A. From the left to the right Hand.

Q. If two Figures are given to be read together, how must they be valued?

A. The first Figure towards the right Hand is *Units*, and the next to that is so many *Tens*; as 89, *Eighty-nine*. Where 9 is the Place of *Units*, and 8 is the Place of *Tens*; for 8 *Tens* are properly called *Eighty*.

Q. If three Figures or a whole Period be given, how is it to be valued?

A. Beginning at the last Figure on the right Hand, I value them *Units, Tens, Hundreds*; as 789, *Seven Hundred Eighty and Nine*.

Note, As every third Figure from the Place of *Units*, bears the Name of *Hundreds*: So for any great Sum to be distinguished into Periods (as in the following Tables) will be of good Use to the Learner, in the easier valuing and expressing that Sum.

TABLE I.

First Period	Units
Tens	9 9 9 9 9
Hundreds	8 8 8 8 9
Thousands	7 7 7 8 9
X Thousands	8 9 9 7 8
C Thousands	7 8 9 7 8
Millions	6 8 9 7 8
X Millions	7 8 9 7 8
C Millions	7 8 9 7 8

TABLE II.

First Period	Units
Tens	4 3
Hundreds	7 5
Thousands	9 6
X Thousands	7 1
C Thousands	4 9
Millions	2 3
X Millions	1 3
C Millions	4 6

Note, See the Notation of Numbers by Latin Letters, in the New Guide to the English Tongue, p. 88.

EXAMPLES for Practice.

Write down in proper Figures the following Numbers, viz.

Twenty-nine.

Three Hundred and forty-eight.

Seven Thousand, two Hundred and twenty-six.

One Thousand, three Hundred and ninety.

Nineteen Thousand, seven Hundred and twenty-eight.

Four Hundred and twenty-seven Thousand, three Hundred and ninety-six.

Nine Hundred and forty-two Thousand, seven Hundred.

Four Millions, seven Hundred and eighty-nine Thousand, three hundred and twenty-eight.

Seven Millions, nine Hundred and forty-two Thousand, four Hundred and seventy-five.

Twenty-six Millions, three Hundred and fourteen Thousand, one Hundred and ninety-five.

One Hundred and ninety-seven Millions, four Hundred and thirty-six Thousand, one Hundred and ninety-one.

Seven Hundred and fourteen Millions, one Hundred and nineteen Thousand, seven Hundred and four.

Of ADDITION.

Q. **W**HAT is the Use of Addition?

A. Addition teacheth to bring several particular Numbers into one Total Sum.

Q. How many Sorts of Addition are there?

A. Two, viz. Simple and Compound.

Of Simple ADDITION.

Q. What is Simple Addition?

A. Simple or Single Addition, is the adding of several Numbers together, whose Signification is the same; as 6 Yards and 8 Yards, make 14 Yards.

Q. If several Numbers are given to be added in one Sum, how are they to be placed?

A. They must be placed in such manner, that Units may stand under Units; Tens under Tens, &c. Pounds under Pounds; Shillings under Shillings, &c.

Q. How do you prove Addition?

A. The best Way of proving Addition is to begin at the Top of the Sum, and reckon the Figures downward, in the same manner that they were added upwards; and if the second Line or Sum Total be equal to the first, it is right.

Ex-

EXAMPLES for Practice.

<i>L.</i>	<i>Yds.</i>	<i>Gals.</i>	<i>Tons.</i>	<i>Hbds.</i>	<i>lb.</i>
4	43	764	3746	47476	461743
7	17	147	7416	73712	761710
3	19	384	4346	31819	476312
2	14	736	7198	31243	126712
1	37	197	3173	71208	310748
7	46	473	4731	70956	471381
6	23	382	1262	81461	704714
4	59	769	4731	31269	312624
7	94	367	7169	74196	781462
—	—	—	—	—	—
—	—	—	—	—	—

<i>Miles.</i>	<i>Leagues.</i>	<i>Years.</i>
4734736	46431734	347312484
3474312	71261374	168126312
4161322	12612714	718126191
7369138	31371261	731618191
3142618	74147312	312134716
4731216	47312614	171216198
4713147	47167471	312614712
3712612	31216126	171614712
7126981	31184712	312814797
—	—	—
—	—	—

Of Compound ADDITION.

Q. What is Compound Addition?

A. Compound Addition is the adding of several Numbers together, having divers Denominations.

I. Of MONY.

Q. Which are the Parts and Denominations of English Mony?

A. 4 Farthings make 1 Penny.

12 Pence — 1 Shilling.

20 Shillings — 1 Pound Sterling.

Q. Are there no other Names of Money used in England?

A. Yes; such as,

	£	s.	d.
A Moidore	==	1	7 0
A Guinea	==	1	1 0
A Half Guinea	==	0	10 6
A Crown	==	0	5 0
A Half Crown	==	0	2 6

☞ There are also several smaller Pieces which speak their own Value; as, a Six-pence, Four-pence, Three-pence, Two-pence, Penny, Half-penny, Farthing.

Note, The following Pieces are only imaginary; as,

	£	s.	d.
A Carolus	==	1	5 0
A Jacobus	==	1	3 0
A Mark	==	0	13 4
An Angel	==	0	10 0
A Noble	==	0	6 8

Q. Are there not some Tables that may be learned by Heart?

A. Yes; these following, called Pence-Tables.

d.	s.	d.	s.	d.		
20	==	1	8	2	==	24
30	==	2	6	3	==	36
40	==	3	4	4	==	48
50	==	4	2	5	==	60
60	==	5	0	6	==	72
70	==	5	10	7	==	84
80	==	6	8	8	==	96
90	==	7	6	9	==	108
100	==	8	4	10	==	120
110	==	9	2	11	==	132
120	==	10	0	12	==	144

Note 1. Tho' I say these Tables may be learned by Heart, I do not say they must; for then, by the same Rule, it would be necessary to have Tables to every Rule in Addition, which no Body uses, and not every one the Pence-Tables; because when they are learnt never so perfectly, their Use extends no farther than Money; and therefore they may very well be omitted, and a better Method substituted in their room, I mean that of Pointing, which, I am sure, is both easier and safer; to Beginners especially. However, I choose to set them down in their Place, that they, who approve of them, may use them; and they who do not, can easily omit them.

2. As all the Parts of Addition are built upon the same Reason: So the Method of Pointing may serve as a general Rule, when any Denomination is to be added.

EXAMPLES.

EXAMPLES.

\mathcal{L}	s.	d.									
4	3	6	1	4	3	4	1	6 $\frac{1}{2}$	14	12	1
1	7	8 $\frac{1}{4}$	3	8	1 $\frac{1}{4}$	1	2	7 $\frac{1}{4}$	17	11	2 $\frac{3}{4}$
2	7	4	1	2	6	3	1	4 $\frac{1}{4}$	19	12	1 $\frac{1}{2}$
1	9	4 $\frac{1}{2}$	3	4	7 $\frac{1}{2}$	3	3	6	16	13	1 $\frac{3}{4}$
3	1	3 $\frac{3}{4}$	1	2	6	1	4	1 $\frac{1}{2}$	12	10	6
1	2	1	3	1	8 $\frac{1}{4}$	3	1	2	14	12	7 $\frac{1}{4}$
4	7	6 $\frac{1}{2}$	7	1	6	1	4	8 $\frac{1}{2}$	19	13	4
3	1	9	4	1	7 $\frac{3}{4}$	3	1	1	12	11	6

\mathcal{L}	s.	d.	\mathcal{L}	s.	d.	\mathcal{L}	s.	d.	\mathcal{L}	s.	d.
19	13	4	47	12	10	21	12	10 $\frac{1}{2}$	12	13	10
12	11	6	17	10	11	31	11	11 $\frac{1}{2}$	71	16	8
17	14	1 $\frac{1}{2}$	17	19	4 $\frac{1}{4}$	47	12	10 $\frac{1}{4}$	19	4	6 $\frac{1}{4}$
19	13	4 $\frac{1}{2}$	31	12	6	19	11	4	12	3	1
12	11	6	11	19	4	31	12	6 $\frac{1}{2}$	26	1	6 $\frac{1}{4}$
19	13	1 $\frac{3}{4}$	12	12	6 $\frac{3}{4}$	12	11	4 $\frac{3}{4}$	31	11	1
36	12	1	11	13	1	37	12	4	14	12	6
19	11	4 $\frac{1}{4}$	11	11	2 $\frac{1}{4}$	19	11	3	19	18	7 $\frac{1}{4}$

\mathcal{L}	s.	d.									
44	12	6 $\frac{1}{4}$	21	11	11 $\frac{1}{2}$	47	12	6 $\frac{1}{2}$	47	11	3 $\frac{1}{4}$
31	18	1 $\frac{1}{2}$	16	12	6	16	19	11 $\frac{1}{4}$	31	17	3
47	12	4	11	9	10 $\frac{1}{2}$	17	12	10 $\frac{1}{4}$	17	13	11 $\frac{3}{4}$
14	12	10 $\frac{3}{4}$	16	12	4 $\frac{1}{4}$	19	12	10	18	14	10 $\frac{1}{2}$
16	14	11	44	1	10	17	12	11 $\frac{3}{4}$	16	11	11
19	12	2	17	14	11 $\frac{1}{4}$	17	19	4 $\frac{1}{2}$	17	14	3 $\frac{1}{4}$
16	11	3	71	3	8 $\frac{3}{4}$	47	13	6	11	18	6
17	12	1 $\frac{1}{4}$	16	1	4	72	18	6	17	17	3 $\frac{1}{2}$

The SCHOOLMASTERS Assistant.

A Mercer's Bill.

Bought of George Bailey, May 17, 1743.

		s.	d.	£	s.	d.
9 Yards of Silk	— — —	at 14	6	per Yd.	6	10 6
12 Yards of flower'd Silk	— — —	at 16	8	—	10	0 0
16 Yards of Sarsenet	— — —	at 6	9	—	5	8 0
10 Yards of Satten	— — —	at 9	6	—	4	15 0
15 Yards of Brocade	— — —	at 10	8	—	8	0 0
11 Scarves	— — —	at 2	0	each	1	2 0
14 Yards of Genoa-Velvet	— — —	at 17	4	per Yd.	12	2 8
19 Yards of Lustre	— — —	at 5	2	—	2	11 8

Sum

A Woollen-Draper's Bill.

Bought of Thomas Simmonds, June 19, 1743.

		s.	d.	£	s.	d.
16 Yards of Drugget	— — —	at 7	0	per Yd.	5	12 0
12 Yards of Broad Cloth	— — —	at 15	0	—	9	0 0
9 Yards of Black Cloth	— — —	at 16	5	—	7	7 9
10 Yards of Shalloon	— — —	at 1	8	—	0	16 8
15 Yards of Serge	— — —	at 1	10	—	1	7 6
7 Yards of fine Spanish Black, at 18	— — —	0	—	—	6	6 0
16 Yards of Frieze	— — —	at 4	6	—	3	12 0
12 Yards of superfine Scarlet	— — —	at 18	0	—	10	16 0

Sum

A Linen-Draper's Bill.

Bought of John Clay, July 17, 1743.

		s.	d.	£	s.	d.
26 Ells of Dowlas	— — —	at 1	4	per Ell	1	14 8
18 Ells of Holland	— — —	at 4	0	—	3	12 0
12 Ells of Diaper	— — —	at 1	0	—	0	12 0
12 Damask Napkins	— — —	at 2	0	each	1	4 0
20 Yards of printed Linen	— — —	at 2	0	p. Yd.	2	0 0
10 Yards of Cambric	— — —	at 12	0	—	6	0 0
10 Yards of Muslin	— — —	at 7	0	—	3	10 0
14 Yards of Canvas	— — —	at 3	4	—	2	6 8

Sum

A Grocer's

The SCHOOLMASTERS Assistant.

9

A Grocer's Bill.

Bought of Thomas Hartley, May 19, 1743.

	s. d.	£ s. d.
8 lb. of Raisins of the Sun — at	0 5 per lb.	0 3 4
15 lb. of Malaga-Raisins — — at	0 4½ —	0 5 7½
10 lb. of Currants — — — at	0 6½ —	0 5 5
11 lb. of Sugar — — — at	0 4½ —	0 4 1½
2 Sugar-Loaves, wt. 15 lb. — — at	0 9 —	0 11 3
13 lb. of Rice — — — at	0 3 —	0 3 3
5 lb. of black Pepper — — — at	1 6 —	0 7 6
10 Oz. of Cloves — — — at	0 10 per oz.	0 8 4
		Sum
		—

A Cheesemonger's Bill.

Bought of Daniel Bridge, July 17, 1743.

	s. d.	£ s. d.
3 Gloucestershire Cheeses, wt. 24 lb. at	0 4 per lb.	0 8 0
1 Cheshire — — — wt. 28 lb. at	0 4 —	0 9 4
3 Warwickshire — — — wt. 20 lb. at	0 3 —	0 5 0
½ Firkin of Butter — — — wt. 28 lb. at	0 6 —	0 14 0
1 Flitch of Bacon — — — wt. 6 Sto. at	4 0 p. Sto.	1 4 0
7 lb. of Cambridge-Butter — — at	0 6 per lb.	0 3 6
9 lb. of new Cheese — — — at	0 4 —	0 3 0
7 lb. of Cream-Cheese — — — at	0 6 —	0 3 6
		Sum
		—

A Millener's Bill.

Bought of Jane Inman, August 28, 1743.

	s. d.	£ s. d.
15 Yards of silver Ribban — at	2 3 p. Yd.	1 13 9
3 Pair of fine Kid-Gloves — at	2 0 p. pair	0 6 0
6 Dozen of Irish Lamb Ditto — at	1 0 —	3 12 0
6 Sarsenet Hoods — — — at	4 6 each	1 7 0
15 Fans, India-Mount — — — at	4 0 —	3 0 0
3 Setts of Knots — — — at	2 0 p. Sett	0 6 0
16 Yards of fine Lace — — — at	10 0 p. Yd.	8 0 0
20 Pieces of Bobbin — — — at	0 6 p. pce.	0 10 0
		Sum
		—

A Carpenter's Bill.

Mr. John Law, Dr. to John Brooks, for Carpenters Work,
and Materials. viz.

		s.	d.	£	s.	d.
1743.						
May 3	For 30 Feet of Fir Timber, at	0	3	p. Foot	0	7
5	— 18 whole Deals — at	1	6	each	1	7
	— 16 slit Deals — — at	1	0	—	0	16
	— 4 Hundred of six-penny Nails —	—	—	—	0	2
	— 3 Hundred of ten-penny Nails —	—	—	—	0	2
	— 6 Hundred of Brads — — —	—	—	—	0	1
21	— 18 Days Work — at	3	0	p. Day	2	14

A Baker's Bill.

Mr. Thomas Marriot, Dr. To James Barnet, viz.

1743.		£	s.	d.
Feb. 4	For a Peck of Bran	—	—	—
	— a fine peck Loaf	—	—	—
13	— a Peck of fine Flour	—	—	—
17	— a Bushel of Pollard	—	—	—
18	— small Bread	—	—	—
	— Yeast	—	—	—
	— a half peck second Loaf	—	—	—
20	— a quartern second Loaf	—	—	—

A Bill of Disbursement.

		L	s.	d.
1743.				
Feb. 17	Laid out in Lamb, seven Groats	—	—	—
18	— in Sallad, five Farthings	—	—	—
21	— in Beef, nineteen Pence halfpenny	—		
Mar. 7	— in Parsnips, three Halfpence	—		
8	— in Potatoes, a Groat	—	—	—
9	— in Candles, seven Groats and three Pence	—	—	—
10	— in Butter and Cheese, eight and twenty Pence	—	—	—
12	— in Bread, three and twenty Pence	—		

Sum

Suppose

Suppose I am indebted, £. s. d.

To A, twenty Pounds, seven Shillings and four	}
Pence Farthing — — — — —	
— B, nineteen Pounds, thirteen Shillings and	
ten Pence Halfpenny — — — — —	
— C, twelve Pounds, fourteen Shillings and	
seven Pence three Farthings — — — — —	
— D, twenty-six Pounds, seventeen Shillings	
and four Pence Farthing — — — — —	
— E, twenty-eight Pounds, thirteen Shillings	
and seven Pence three Farthings — — — — —	
— F, twenty-one Pounds, fifteen Shillings and	
five Pence Halfpenny — — — — —	
— G, five Pounds, six Shillings and seven Pence	
Farthing — — — — —	

How much is the Debt?	Sum
	—————

2. Of T R O Y - W E I G H T.

Q. Which are the Denominations of Troy-Weight?

A. 24 Grains make 1 Pennyweight.
20 Pennyweights 1 Ounce.
12 Ounces — 1 Pound.

Q. What sort of Things are weighed by this Weight?

A. Gold, Silver, Jewels, Electuaries, Bread, and all Liquors.

Q. What is the Standard for Gold?

A. 22 Carrats of fine Gold, and 2 Carrats of Copper being melted together, are esteemed the true Standard for Gold Coin.

Q. What is a Carrat?

A. A Carrat is not any certain Quantity or Weight, but the twenty-fourth Part of any Quantity or Weight.

Q. What is the Standard for Silver?

A. 11 oz. 2 dwts. of fine Silver, and 18 dwts. of Copper being melted together, are esteemed the true Standard for Silver Coin; called Silver Sterling.

Note, The Ounce of Silver being valued at 5 Shillings, one Pennyweight will be valued at three Pence, and the Grain at half a Farthing.

EXAMPLES.

EXAMPLES.

Oz. dw. gr.	Oz. dw. gr.	lb. oz. dw. gr.	lb. oz. dw. gr.
7 10 12	7 13 12	4 10 12 11	7 10 12 10
6 11 11	6 11 14	3 11 16 12	3 4 16 13
5 16 11	9 12 17	1 4 16 19	3 7 12 11
4 17 10	4 16 13	3 3 11 17	1 1 18 16
1 12 16	7 11 14	4 1 16 14	3 11 16 12
7 12 18	6 19 12	3 3 16 11	4 3 16 21
9 16 19	7 13 16	7 11 16 10	3 4 13 11
8 14 16	3 19 14	6 4 13 15	3 7 18 19
4 16 10	5 9 8	5 11 14 13	9 8 19 9
9 4 8	6 12 13	9 10 15 14	7 11 12 8

3. Of AVOIRDUPOIS-WEIGHT.

Q. Which are the Denominations of Avoirdupois-Weight?

A. 16 Drams make 1 Ounce.

16 Ounces — 1 Pound.

28 Pounds — 1 Quarter of an Hundred Weight.

4 Quarters — 1 Hundred Weight, or 112 Pounds.

20 Hundred Wt. 1 Ton.

Q. What is the Use of Avoirdupois-Weight?

A. Avoirdupois-Weight is used in weighing any Thing of a coarse and drossy Nature, as all Grocery and Chandlers Wares, and all Metals but Silver and Gold.

Q. What is the Difference between a Pound Avoirdupois, and a Pound Troy?

A. The Pound Avoirdupois is equal to 14 oz. 11 dwts. 15 gr. and an half Troy.

Q. What other Denominations are there in this Weight?

A. There are several other Denominations in Avoirdupois-Weight, in some particular Goods, and others only customary in some particular Places; as appears by the following Table.

TABLE.

T A B L E.

	lb.		lb.
A Firkin of Butter is —	56	A Burden of Gad	180
— Soap is — —	64	Steel, or 9 Score —	180
A Barrel of Pot-Ash is 200		A Quintal of Fish in	100
— Anchovies is —	30	Newfoundland is	5
— Candles is — —	120	A Stone of Glafs is	5
— Figs, from — —	98	A Seam of Glafs is 24	120
to 2 C. 3 qrs. —		Stone, or — —	
— Soap is — —	256	<i>For Cheese and Butter.</i>	
— Butter is — —	224	A Clove or half Stone is	8
— Gunpowder is —	112	A Wey in Suffolk is	256
— Raifins is — —	112	32 Cloves, or — —	336
A double Barrel of Anchovies is — }	60	— Essex is 42 Clov. or	
A Puncheon of Prunes is		<i>For Wool.</i>	
10 C. or 12 C.		A Clove is — —	7
A Fother of Lead is 19 C. 2 qrs.		A Stone is — —	14
A Stone of Iron or Shot is 14		A Todd is — —	28
— Butchers Meat is 8		A Wey is 6 Tod and	182
A Gallon of Train Oil is 7½		1 Stone, or — —	
A Faggot of Steel is — 120		A Sack is 2 Weyns, or —	364
		A Last is 12 Sacks, or	4368

E X A M P L E S.

T. C. gr. lb.	C. gr. lb.	lb. oz. dr.	lb. oz. dr.
7 11 1 16	17 1 12	14 10 12	12 11 10
1 12 3 11	16 2 11	16 12 11	17 12 10
3 4 1 17	14 1 12	19 12 12	14 12 13
3 1 2 12	16 3 19	17 12 13	16 12 11
7 11 1 11	19 1 12	14 11 10	19 12 11
6 3 2 13	16 3 18	16 15 14	17 13 4
3 1 2 20	12 1 18	13 11 14	16 11 3
4 1 3 26	16 3 19	17 12 10	21 10 7

4. Of APOTHECARIES-WEIGHT.

Q. Which are the Denominations of Apothecaries-Weight?

A. 20 Grains make 1 Scruple.

3 Scruples — 1 Dram.

8 Drams — 1 Ounce.

12 Ounces — 1 Pound.

Q. What

Q. What is the Use of Apothecaries-Weight?

A. Apothecaries-Weight is such as their Medicins are compounded by.

Note, i. The Apothecaries mix their Medicins by this Rule, yet buy and sell their Commodities by Avoirdupois-Weight.

2. The Apothecaries Pound and Ounce, and the Pound and Ounce Troy are the same, only differently divided and subdivided.

EXAMPLES.

5. Of Long Measure.

Q. Which are the Denominations of Long Measure?

A. 3 Barley Corns make 1 Inch.

4 Inches — — 1 Hand.

12 Inches — — — 1 Foot.

3 Feet — — 1 Yard

6 Feet — — — 1 Fathom.

5 Yards and an Half : Rod, Pole, or Perch.

40 Poles — — — 1 Furlong.

8 Furlongs — — 1 Mile.

3 Miles — — — 1 League.

60 Miles — — — 1 Degree.

Note, A Degree is 69 Miles, and 4 Furlongs, very near, tho' commonly reckoned but 60 Miles.

Q. What is the Use of Long Measure?

A. To measure Distance of Places or any Thing else, where Length is considered, without Regard to the Breadth.

Q. Is the Pole or Perch always of the same Length?

A. No.

Q. What is the Difference?

A. Five Yards and an Half, are the Statute Measure for a Pole or Perch; but for Fens and Woodlands, it is customary to reckon 18 Feet to the Pole; and for Forests 21 Feet.

Q. What is the Use of an Hand?

A. It is used to measure Horses.

Q. What is the Use of a Fathom?

A. It is used to measure Depths.

E X A M P L E S.

M.	f.	p.	Yds.	f.	in.	Le.	m.	f.	p.	Yds.	f.	in.	bc.
17	7	19	14	2	7	17	2	6	14	16	1	0	0
16	1	14	16	0	4	12	1	1	18	14	2	10	1
19	3	16	19	1	10	16	2	1	16	17	1	4	2
17	4	19	16	2	4	19	2	7	11	13	2	11	1
12	1	11	14	2	5	19	0	4	31	16	1	7	2
18	3	16	14	2	1	17	2	1	12	17	1	4	1
19	7	14	31	1	3	12	1	2	17	19	2	6	2
16	6	26	11	0	1	17	1	1	14	19	2	1	1

6. Of CLOTH-MEASURE.

Q. Which are the Denominations of Cloth-Measure?

A. 2 Inches and a Quarter make 1 Nail.

4 Nails — — — — 1 Quarter of a Yard.

4 Quarters — — — — 1 Yard.

3 Quarters of a Yard — — 1 Flemish Ell.

5 Quarters of a Yard — — 1 English Ell.

Note, 1. The Yard is used in measuring all sorts of Woollen Cloths, wrought Silks, most Linens, Tape and Gartering.

2. The Ell English is used only in measuring some particular Linens, called Hollands.

3. The Ell Flemish is used in measuring of Tapestry.

E X A M P L E S.

Yds. qr. na.	Ells qr. na.	E.F. qr. na.
17	1	1
11	3	1
16	1	2
19	3	1
17	1	2
12	3	3
19	1	1
14	2	3

7. Of LAND-MEASURE.

Q. Which are the Denominations of Land-Measure?

A. 9 Square Feet — — — make 1 Yard.

30 Yards and a Quarter — — — 1 Pole.

40 Poles in Length and 1 in Breadth 1 Rood.

4 Rods — — — — — 1 Acre.

Q. What is the Use of Land-Measure?

A. It gives the Content of any Piece of Ground in Acres:

EXAMPLES.

A. r. p.

17 3 12

11 2 19

14 1 21

16 1 12

17 2 11

13 2 12

11 1 17

26 3 31

A. r. p.

17 1 12

11 2 13

16 3 27

19 1 16

12 3 14

16 1 11

17 3 14

12 1 11

A. r. p.

26 1 36

13 2 22

23 3 13

36 2 28

22 2 33

19 0 19

33 3 16

17 2 24

8. Of LIQUID MEASURE.

Q. How many sorts of Liquid Measure are there?

A. Two: Wine-Measure and Winchester-Measure.

Q. What is meant by Winchester-Measure?

A. It is a particular Measure used for Beer and Ale.

Q. What is the Difference between Wine-Measure and Winchester-Measure?

A. A Gallon of Wine is 231 solid Inches; but a Gallon of Beer or Ale exceeds that Measure by 51 Inches, and is 282 solid Inches.

(1). Of WINE-MEASURE.

Q. Which are the Denominations of Wine-Measure?

A. 2 Pints — — — make 1 Quart.

4 Quarts — — — — 1 Gallon.

10 Gallons — — — — 1 Anchor of Brandy or Rum.

18 Gallons — — — — 1 Runlet.

31½ Gallons — — — — 1 Barrel.

42 Gallons — — — — 1 Tierce.

63 Gallons — — — — 1 Hogshead.

84 Gallons — — — — 1 Puncheon.

2 Hogsheads — — — — 1 Pipe or Butt.

2 Pipes or four Hogsheads 1 Tun.

Q. What

Q. What other Liquors are measured by the Wine Standard?

A. All Brandies, Spirits, Strong Waters, Perry, Cyder, Mead, Vinegar, Hony and Oil.

Note, Milk is also retail'd by this Standard, not by Law, but Custom only.

E X A M P L E S.

T. bds. gls. qts.	Hds. gls. qts.	Tier. gls. qts.
7 1 12 2	27 10 2	27 12 1
6 3 31 3	22 13 3	29 17 3
7 1 41 2	26 11 3	22 11 2
6 2 17 1	29 12 2	27 31 3
7 3 14 3	23 22 0	29 12 1
1 2 19 1	27 32 2	27 11 2
9 1 15 2	29 27 3	26 17 1
3 1 11 2	26 33 2	22 11 3

(2). Of WINCHESTER-MEASURE.

Q. Which are the Denominations of Winchester-Measure?

A. 2 Pints — — — make 1 Quart.

4 Quarts — — — — 1 Gallon.

8 Gallons — — — — 1 Firkin of Ale.

9 Gallons — — — — 1 Firkin of Beer.

2 Firkins — — — — 1 Kilderkin.

4 Firkins — — — — 1 Barrel.

1 Barrel and an Half, or 54 Gals. 1 Hogshead of Beer.

Q. What is the Difference between Ale and Beer Measure?

A. In London only they compute 8 Gallons to the Firkin of Ale, and 32 Gallons to the Barrel; but in all other Parts of England, for Ale, Strong Beer and Small Beer, 34 Gallons are computed to the Barrel, and 8 Gallons and an Half to the Firkin.

Q. What other Commodities are there, that go by the Winchester-Measure?

A. A Barrel of Salmon or Eels is 42 Gallons.

A Barrel of Herrings — 32 Gallons.

A Keg of Sturgeon — 4 or 5 Gallons.

A Firkin of Soap — 8 Gallons.

E X A M P L E S.

E X A M P L E S.

Hds. gls. qts.	B.B. fir. gal.	A.B. fir. gal.
7 12 1	23 3 3	23 1 7
6 17 2	27 2 6	24 2 6
3 21 2	29 3 7	27 1 5
2 11 1	27 2 8	27 3 4
3 17 2	26 1 5	26 3 2
9 12 1	37 1 4	27 1 3
6 17 3	27 1 3	26 2 1
7 3 $\frac{1}{2}$ 2	32 2 2	29 2 0

9. Of D R Y M E A S U R E.

Q. Which are the usual Denominations of Dry Measure?

A. 2 Pints — make 1 Quart.
 2 Quarts — 1 Pottle.
 2 Pottles — 1 Gallon.
 2 Gallons — 1 Peck.
 4 Pecks — 1 Bushel.
 8 Bushels — 1 Quarter of Corn.
 36 Bushels — 1 Chaldron of Coals.

Q. Wherein does London differ from other Places in England in the Coal Measure?

A. In London 36 Bushels make a Chaldron; but in all other Places 32 Bushels make a Chaldron. The Bushel also in Water Measure contains 5 Pecks.

Q. What other Denominations are there in Dry Measure?

A. A Score of Coals — — is 21 Chaldrons.
 A Sack of Coals — — 3 Bushels.
 A Sack of Corn — — 4 Bushels.
 10 Quarters of Corn make 1 Wey.
 12 Wey are — — 1 Laft.
 A Load of Corn — — is 5 Bushels.
 A Cart-load Ditto — — 40 Bushels.

Q. What is the Use of Dry Measure?

A. Dry Measure is applied to all dry Goods, as Corn, Seeds, Fruit, Roots, Sand, Salt, Sea-Coal, Charcoal, Small-coal, Oysters, Muscles and Cockles.

Q. What is the Standard for Dry Measure?

A. The Standard for Dry Measure is a Winchester-Bushel, being 18 Inches and an Half wide throughout, and 8 Inches deep. One Gallon of this Quantity is 268 solid Inches and $\frac{4}{5}$, and consequently is less than an Ale Gallon by $13\frac{1}{3}$ solid Inches.

E X A M P L E S.

Ch.	bu.	p.	Qrs.	bu.	p.	Qrs.	bu.	p.
17	11	3	14	7	2	36	7	3
16	10	2	16	1	1	43	6	2
19	11	1	19	3	2	22	3	3
17	12	3	16	1	1	37	2	2
16	19	3	17	3	2	26	5	2
17	11	1	16	1	1	28	4	3
17	11	3	12	3	1	33	7	0
11	14	1	37	2	3	42	3	2

10. Of T I M E.

Q. Which are the Denominations of Time?

A. 60 Seconds — — — make 1 Minute.

60 Minutes — — — 1 Hour.

24 Hours — — — 1 Day.

7 Days — — — 1 Week.

4 Weeks — — — 1 Month.

13 Months, 1 Day, and 6 Hours, 1 common or Julian Year.

Q. What is a Solar Year?

A. According to the best Computations, a Solar Year is 365 Days, 5 Hours, 48 Minutes, and 57 Seconds.

Q. How is the Year divided by the Kalendar?

A. Thirty Days hath September,
April, June, and November,
All the rest have Thirty-one,
Except February alone,
Which claimeth just Eight and a Score,
But every Leap-Year one more.

E X A M P L E S.

M.	w.	d.	H.	m.	sec.	D.	b.	m.	sec.
14	1	6	17	10	32	17	11	13	16
17	2	5	17	22	21	19	12	16	11
16	1	3	14	21	32	17	12	17	13
19	3	2	4	2	3	14	13	26	31
16	1	1	7	3	1	13	12	11	48
26	2	0	73	26	30	17	16	19	12
13	2	2	22	28	42	13	16	26	51

II. Of MOTION.

Q. Which are the Denominations of Motion in the heavenly Bodies?

A. 60 Seconds make 1 prime Minute.
 60 Minutes — 1 Degree.
 30 Degrees — 1 Sign.
 12 Signs, or 360 Degrees, make the whole great Circle of the Zodiac.

EXAMPLES.

°.	1.	11.	°.	1.	11.
71	10	16	46	17	31
12	11	19	17	36	18
17	16	13	13	11	12
19	11	26	16	19	12
17	48	51	17	12	10
13	12	11	16	12	10
17	16	11	17	19	17
57	16	17	31	26	43

12. Of Things Bought and Sold by the Tale.

Q. Which are the Denominations of Goods accounted by the Tale?

A. 12 Particulars — make 1 Dozen.
 12 Dozen — — 1 Gross.
 12 Gross or 144 Dozen 1 great Gross.

Examples are needless.

Questions to exercise ADDITION.

1. A Man was born in the Year 1702, I demand when he will be 57 Years of Age?
2. There are two Numbers whose Difference is 17, and the lesser Number is 44; What is the greater Number?
3. A Man borrowed a Sum of Money, and paid in Part 12*l.* 10*s.* and the Remainder is 17*l.* 10*s.* I demand the Sum borrowed?
4. A owes me 3 Guineas, B 50*l.* 12*s.* C 104*l.* D three Score and seventeen Pounds, How much is due to me in all?

5. A Man

5. A Man hath 6 Bags of Hops ; the first weighs 2 qrs. 14 lb. and each of the rest weighs 14 lb. more : What Quantity hath he in the Whole ?

6. A Man took an House for 12 Years ; and by Agreement was to pay 100*l.* 10*s.* down ; 190*l.* 4*s.* at the End of six Years ; and 109*l.* 6*s.* at the End of twelve Years. I demand how much the whole Sum was ?

Of SUBTRACTION.

Q. **W**HAT is the Use of Subtraction ?

A. By taking a less Number from a greater, it shews the *Difference* between both.

Q. How many sorts of Subtraction are there ?

A. Two : Simple and Compound.

Of Simple SUBTRACTION.

Q. What is simple Subtraction ?

A. Single or simple Subtraction is the finding a Difference between any two Numbers, whose Signification is the same ; as the Difference between 6 Yards and 4 Yards, is 2 Yards.

Q. How are Numbers to be placed in Subtraction ?

A. With Units under Units, Tens under Tens, &c. as in Addition.

Q. What Rule have you for the Operation of Subtraction in general ?

A. When the lower Number is greater then the upper, take the lower Number from the Number, which you borrow, and to that Difference add the upper Number, carrying one to the next lowest Place.

Q. What Number must you borrow, when the lower Number is greater ?

A. The same, which you stop at in Addition.

Q. How do you prove Subtraction ?

A. By adding the Remainder, and the lesser Line together, which will always be equal to the greater Line. Or,

By subtracting the Remainder from the greater Line, and that Difference will always be equal to the lesser Line.

E X A M P L E S.

	£	Yards.	Miles.	Days.	Months.
From	763	7694	41372	761214	7613471
Take	122	1867	13976	131812	1813126

Diff.

	Hours.	lb.	Crowns.	Shillings.
From	31261812	312617127	71261871	7612641
Take	19879128	173121712	26571914	5910817

Diff.

Of Compound S U B T R A C T I O N.

Q. What is Compound Subtraction?

A. Compound Subtraction produces a Difference between any two Sums of divers Denominations.

I. Of M O N Y.

E X A M P L E S.

	£	s.	d.									
From	14	10	6 $\frac{1}{2}$	36	12	6 $\frac{1}{2}$	76	12	4 $\frac{3}{4}$	31	18	4 $\frac{5}{8}$
Take	3	17	8 $\frac{1}{2}$	37	11	9 $\frac{3}{4}$	17	13	3 $\frac{1}{4}$	16	19	1 $\frac{3}{4}$

Diff.

	£	s.	d.									
Bor.	41	15	3	76	3	4 $\frac{1}{2}$	73	7	6	17	12	1 $\frac{1}{4}$
Paid	14	17	1 $\frac{1}{2}$	13	17	7	19	4	1 $\frac{1}{2}$	14	7	2

Unpaid

	£	s.	d.	£	s.	d.	£	s.	d.	£	s.	d.
Lent	136	17	6 $\frac{1}{2}$	47	17	6	413	11	7 $\frac{3}{4}$	71	18	9
Rec.	76	12	7 $\frac{3}{4}$	19	11	6 $\frac{1}{4}$	171	18	9 $\frac{1}{2}$	17	16	10 $\frac{3}{4}$

Due

Borrowed

	<i>L</i>	<i>s.</i>	<i>d.</i>		<i>L</i>	<i>s.</i>	<i>d.</i>
Borrowed	764	0	0	Lent	800	10	6
	13	1	2 $\frac{1}{2}$		12	11	2 $\frac{1}{4}$
	17	4	1		19	12	6
	16	1	6 $\frac{3}{4}$		17	11	2 $\frac{1}{2}$
Paid at sev- eral Times.	21	2	8	Receiv'd at se- veral Times.	14	11	3
	19	11	10		19	12	2
	26	13	5 $\frac{1}{4}$		14	11	8 $\frac{3}{4}$
	11	19	6 $\frac{1}{2}$		17	16	2 $\frac{1}{4}$
	13	12	2 $\frac{1}{2}$		46	12	7 $\frac{3}{4}$
Paid in all				Receiv'd in all			
Unpaid				Remains due			

2. T R O Y - W E I G H T.

	Oz. dw. gr.	Oz. dw. gr.	Oz. dw. gr.	lb. oz. dw. gr.
From	71 11 12	71 12 18	13 16 12	84 4 11 12
Take	2 10 19	10 4 19	5 19 14	17 10 11 7
Diff.				

3. A V O I R D U P O I S - W E I G H T.

	C. qrs. lb.	lb. oz. dr.	lb. oz. dr.	T. c. qrs. lb.
Bou.	72 1 18	17 2 1	17 10 1	12 1 2 10
Sold	3 1 26	10 13 2	15 14 3	5 3 1 19
Unsold				

4. A P O T H E C A R I E S - W E I G H T.

	3. 3. 3. gr.	3. 3. 3. gr.	lb. 3. 3. 3. gr.
From	65 4 2 10	47 5 1 16	48 3 2 0 19
Take	7 7 2 12	2 1 2 18	10 1 2 2 17
Diff.			

5. L O N G

5. LONG MEASURE.

	Le. m. f. p.	Yd. f. in. b.c.	Le. m. f. p.
From	7 1 3 10	48 0 1 2	6 0 1 3
Take	14 2 5 16	12 0 3 1	17 1 2 20
	<hr/>	<hr/>	<hr/>
Diff.			
	<hr/>	<hr/>	<hr/>

6. CLOTH-MEASURE.

	Yd. qr. na.	E.F. qr. na.	Yds. qrs. na.
Bought	7 1 3 1	5 1 2 2	ADraper bought
Sold	1 9 2 3	1 6 1 1	148 0 0
	<hr/>	<hr/>	<hr/>
Unfold			14 1 2
	<hr/>	<hr/>	17 3 3
			19 1 2
			16 1 1
			17 3 3
	Yd. qr. na.	E. qr. na.	
From	4 7 2 1	1 7 1 2	
Take	1 2 1 2	1 4 4 3	Sold in all
	<hr/>	<hr/>	<hr/>
Diff.			Unfold
	<hr/>	<hr/>	<hr/>

7. LAND-MEASURE.

	A. r. p.	A. r. p.	A. r. p.	A. r. p.
Bought	1 2 1 10	1 7 3 17	2 8 1 7	3 2 0 9
Tilled	5 3 17	1 2 3 23	1 9 1 28	1 6 2 23
	<hr/>	<hr/>	<hr/>	<hr/>
Untilled				
	<hr/>	<hr/>	<hr/>	<hr/>

8. WINE-MEASURE.

	T. bds. gal.	T. bds. gal.	Gals. qts. pts.	Gals. qts. pts.
From	3 2 10	7 2 10	19 2 1	67 1 1
Take	1 3 19	1 2 28	12 1 1	12 3 0
	<hr/>	<hr/>	<hr/>	<hr/>
Diff.				
	<hr/>	<hr/>	<hr/>	<hr/>

9. WINCHESTER-

9. WINCHESTER-MEASURE.

	Hds. gal. qts.	A.B. f. gal.	B.B. f. gal.	Hds. gal. qts.
Bou.	17 10 1	17 2 1	48 1 3	41 2 2
Sold	12 11 2	14 1 3	17 1 7	23 3 3
<i>Unfold</i>	—	—	—	—

10. DRY MEASURE.

	Cb. bu. p.	Cb. bu. p.	Qrs. bu. p.	Qrs. bu. p.
From	17 2 1	40 1 2	19 1 1	26 1 3
Take	10 1 3	16 5 1	12 7 2	19 1 2
<i>Diff.</i>	—	—	—	—

11. TIME.

	D. b. m. sec.	W. d. b. m. sec.	W. d. b. m. sec.
From	41 13 22 12	14 1 10 12 10	17 1 10 12 10
Take	22 16 33 31	10 3 19 48 26	10 2 14 6 15
<i>Diff.</i>	—	—	—

12. MOTION.

	°. f. ".	°. f. ".	°. f. ".
From	48 10 12	47 2 10	62 13 9
Take	19 11 16	12 19 48	49 18 33
<i>Diff.</i>	—	—	—

Questions to exercise SUBTRACTION.

1. A Man was born in the Year 1702; I demand his Age in the Year 1759?
2. There are two Numbers, the greater Number is 61, and the lesser is 44; I demand the Difference?
3. There are two Numbers whose Difference is 17, and the greater Number is 61; I demand the lesser Number?

4. A Man borrowed 30*l.* and paid in Part 12*l.* 10*s.* I demand how much remains unpaid?

5. King *Charles the Martyr*, was beheaded in the Year 1648; how many Years is it since?

6. *A* is indebted to the Brewer the Sum of 109*l.* 10*s.* *B* owes him 94*l.* 4*s.* 10*d.* $\frac{1}{2}$; how much does one owe more than the other?

7. What Sum is that, which taken from 100*l.* leaves 48*l.* 7*s.* 6*d.* $\frac{1}{2}$?

8. There were 4 Bags of Money containing, as follows, *viz.* The first Bag 34*l.* the second Bag 50*l.* the third Bag 100*l.* and the fourth Bag 150*l.* which were to be paid to several Persons; but one of the Bags being lost, there were but 234*l.* paid; I demand which Bag was wanting?

Of MULTIPLICATION.

Q. **W**HAT is Multiplication?

A. It is a short Way of performing several Additions.

Q. How many Parts are there in Multiplication?

A. Three, *viz.*

1. The *Multiplicand*, or Sum to be multiplied.

2. The *Multiplier*, or Sum multiplied by.

3. The *Product*, or Total of the *Multiplicand* as often as there are Units in the *Multiplier*.

Note, The *Multiplicand* and the *Multiplier*, are also called *Factors*; and the *Product*, the *Fact* or *Rectangle*.

Q. How many sorts of Multiplication are there?

A. Two, *viz.* *Simple* and *Compound*.

Of Simple MULTIPLICATION.

Q. What is Simple Multiplication?

A. Simple Multiplication is the multiplying of any two Numbers together, without respect to their Signification; as 7 times 8 is 56.

Note, 1. As Addition and Subtraction of Integers are called Simple Addition, and Simple Subtraction: so should Multiplication and Division of Integers be called Simple Multiplication, and Simple Division; and that only should be called Compound Multiplication, and Compound Division, which hath Numbers of divers Denominations to be either Multiplied, or Divided.

2. The following Table must be learnt perfectly by Heart, before you can proceed any further.

The MULTIPLICATION TABLE.

3 times 3 is	9	5 times 6 is	30	11 times 3 is	33
4	12	7	35	4	44
5	15	8	40	5	55
6	18	9	45	6	66
7	21	6 times 6	36	7	77
8	24	7	42	8	88
9	27	8	48	9	99
4 times 4	16	9	54	12 times 3	36
5	20	7 times 7	49	4	48
6	24	8	56	5	60
7	28	9	63	6	72
8	32	8 times 8	64	7	84
9	36	9	72	8	96
5 times 5	25	9 times 9	81	9	108

C A S E I.

Q. What do you observe in the first Case of Multiplication?

A. That the Factors be placed one under another, in such manner, that Units may stand under Units, Tens under Tens, &c. and then multiply as the Table directs.

E X A M P L E S.

<i>£</i>	Crowns.	Days.	Hours.
47613127	47613174	71261812	71261312
2	3	4	5
—	—	—	—
—	—	—	—
—	—	—	—

Minutes.	Years.	Gallons.	Ounces.
73126184	71312674	31261267	47612312
6	7	8	9
—	—	—	—
—	—	—	—
—	—	—	—

Shillings.	Yards.	Bushels.	Ells.
31261731	76138126	82365243	65423789
11	12	11	12
—	—	—	—
—	—	—	—
—	—	—	—

Q. How do you multiply by any Number between 12 and 20 at one Operation?

A. Multiply by the Figure in Units Place, and as you Multiply, add to the Product of each single Figure that of the Multiplicand, which stands next on the right Hand.

Gallons.	Days.	Months.	lb.
4731217	4713176	4731261	4713761
15	16	17	18
—	—	—	—
—	—	—	—

C A S E 2.

Q. What do you observe in the second Case of Multiplication?

A. 1. When the Multiplier consists of more Figures than one, there must be made as many several Products, as there are Figures contained in the Multiplier.

2. Let the first Figure of every Product be placed exactly under its Multiplier.

3. Add these Products together, and their Sum will be the total Product.

Q. How do you prove Multiplication?

A. Multiplication and Division do mutually prove each other; yet Multiplication may as truly be proved by itself, by inverting the Factors.

E X A M P L E S.

Crowns.	Days.	Weeks.	Pence.
691861	129186	281216	181281
26	98	978	763
—	—	—	—
17988386	12660228	275029248	138317403
—	—	—	—
Ounces.	Yards.	Pints.	Quarts.
269181	261986	812617	281691
4629	7638	43859	76286
—	—	—	—
1246038849	2001049068	35640569003	21489079626
—	—	—	—

Q. What Exception have you to this Case?

A. When these Figures 1 and 1, or 1 and 2, or any other two Figures under 20, happen together in the Multiplier, you may multiply by both at once; as in Case 1.

E X A M P L E S.

Weeks.	Bushels.	Grains.	Leagues.
761312	671612	963458	843126
412	114	912	119
<hr/>	<hr/>	<hr/>	<hr/>
313660544	76563768	878673696	100331994

C A S E 3.

Q. What do you observe in the third Case of Multiplication?

A. 1. Such Factors, as have Cyphers at the Ends, must be set one under another, as if there were no Cyphers.

2. The Cyphers placed at the End of either, or both of the Factors, are to be omitted till the last Product, and then the same Number of Cyphers must be annexed to it.

E X A M P L E S.

Pence.	Hours.	Yards.
476000	180120	461210
170	48100	42100
<hr/>	<hr/>	<hr/>
80920000	8663772000	19416941000

Nails.	Inches.	Barrels.
760000	461200	618010
4800	48000	74210
<hr/>	<hr/>	<hr/>
3648000000	22137600000	45862522100

C A S E 4.

Q. What do you observe in the fourth Case of Multiplication?

A. When Cyphers are placed between the significant Figures in the Multiplier, they must be omitted in the Operation; regard being had to the first Figure of every particular Product, as before.

E X A M P L E S.

Gallons.	Eggs.	Buttons.
128121	128128	246145
72001	70043	60012
<hr/>	<hr/>	<hr/>
9224840121	8974469504	14771653740

C A S E 5.

Q. How do you multiply by the Parts of any Number, instead of the Whole?

A. When the Multiplier is such a Number, that any two Figures, being multiplied together, will make the said Multiplier, it is shorter to multiply the given Number by one of those Figures, and that Product by the other; as 5 times 7 is 35.

E X A M P L E S.

Pounds.	Men.	Soldiers.	Sailors.
764126	764131	461231	461312
35	48	72	36
<hr/>	<hr/>	<hr/>	<hr/>
26744410	36678288	33208632	16607232

Of Compound MULTIPLICATION.

Q. What is Compound Multiplication?

A. When several Numbers of divers Denominations are given to be multiplied by one common Multiplier; this is called Compound Multiplication.

E X A M P L E S.

£ s. d.	lb. oz. dwt. gr.	C. qrs. lb.	lb. oz. dr.
17 3 1 $\frac{1}{4}$	17 5 12 16	43 1 14	17 12 10
2	3	4	5
<hr/>	<hr/>	<hr/>	<hr/>
<hr/>	<hr/>	<hr/>	<hr/>

M. f. p.	Yds. f. in. b.c.	Yds. qr. na.	B.B. fir. gal.
16 4 21	17 2 3 1	16 3 2	17 2 3
6	7	8	9
<hr/>	<hr/>	<hr/>	<hr/>
<hr/>	<hr/>	<hr/>	<hr/>

Cb. b. p.	Da. b. m. sec.	M. w. da.	°. f. "
16 12 3	17 14 14 15	16 3 4	16 11 13
10	12	11	7
<hr/>	<hr/>	<hr/>	<hr/>
<hr/>	<hr/>	<hr/>	<hr/>

Questions to exercise MULTIPLICATION.

1. If one Man's Pay be 3*s.* what must 40 Men have?
2. What is the Product of 76, multiplied by 3 and by 7?
3. There are 124 Men employ'd to finish a Piece of Work, and they are to have 3*l.* each Man; I demand how much they must all have?
4. An Army of 10000 Men, having plunder'd a City, took so much Mony, that, when it was shar'd among them, each Man had 27*l.* I demand how much Mony was taken in all?
5. There were 40 Men concern'd in the Payment of a Sum of Mony, and each Man paid 127*l.* how much was paid in all?
6. If one Foot contains 12 Inches, I demand how many Inches there are in 126 Feet?
7. What is the Product of 769, multiplied by 9 and by 7?

Of DIVISION.

Q. *WHAT is Division?*

A. It is a short Way of performing several *Subtractions*, and shews how oft one Number is contained in another, and what remains.

Q. *How many Parts are there in Division?*

A. Four, *viz.*

1. The *Dividend*, or Sum to be divided.
2. The *Divisor*, or Sum divided by.
3. The *Quotient*, or Answer to the Question.
4. The *Remainder*, which is always less than the *Divisor*, and of the same Name with the *Divided*.

Note, *The Divisor, Dividend, and Quotient are certain; but the Remainder is uncertain, because some Operations in Division have no Remainder.*

Q. *How many sorts of Division are there?*

A. Two; *Simple and Compound.*

Of Simple DIVISION.

Q. *What is Simple Division?*

A. *Simple Division* is, when the *Divisor* and *Dividend* are made choice of, without any regard to their Signification; as, 56 divided by 7, gives 8 for the *Quotient*; or, the Number 7 is contained in 56, eight times.

Q. *How many sorts of Simple Division are there?*

A. Two; *Short Division, and Long Division.*

Of Short DIVISION.

Q. *What is Short Division?*

A. *Short Division* is, when the *Divisor* does not exceed 12.

E X A M P L E S.

Minutes.	Montbs.	Days.
2)71313674(6)31261084(11)7312613107(
3)42310812(7)713126719(12)3812617314(
4)13812612(8)701267131(11)1612798131(
5)61231281(9)126713108(12)1731261712(

Q. How is Division proved?

A. Multiply the *Divisor* and *Quotient* together, and the *Remainder* (if there be any) add to the Product; that *Sum* will be equal to the *Dividend*.

Of Long DIVISION.

C A S E I.

Q. What is Long Division?

A. When the *Divisor* is more than 12, for help of the Memory, we are obliged to multiply the *Quotient Figures* and *Divisor* together, and subtract that Product from the *Dividend*, in order to find out the *Remainder*; which Operation must be continued to every *Quotient Figure*: And this is called *Long Division*.

E X A M P L E S.

Yards.	Shillings.	Pence.
91)71261871(28)71261714(1217)31917312(
82)31712617(19)73126171(3164)12697126(
73)17312618(381)13261714(6128)71217312(
64)47312617(773)31746173(2912)47161231(
55)73181061(937)13189714(33108)91261814(
46)76131714(761)12816171(71216)17131716(
37)31231712(7618)18917312(86257)34175362(

C A S E 2.

Q. What do you observe of Cyphers placed at the End of the *Divisor*?

A. 1. They must be cut off; and the same Places also must be cut off in the *Dividend*.

2. Those Figures, which are cut off in the *Dividend*, must be annexed to the *Remainder* at last.

E X A M P L E S.

Yards.	Crowns.
625 00)712613 12(128 000)73126 071(
426 00)713121 74(412 000)71613 181(

C A S E

C A S E 3.

Q. How do you divide by the Parts of any Number instead of the Whole?

A. When the *Divisor* is such a Number that any two Figures, being multiplied together, will make the said *Divisor*, it is shorter to divide the given Number by one of those Figures, and that *Quotient* by the other; as 5 times 7 is 35.

E X A M P L E S.

Pence.	Crowns.	Pounds.
35)26744410(48)36678288(72)33208632(

Of Compound D I V I S I O N.

Q. What is Compound Division?

A. When several Numbers of divers Denominations are given to be divided by one common *Divisor*; this is called Compound Division.

E X A M P L E S.

l. s. d.	lb. oz. dwt. gr.	T. e. qr. lb.
2)48 12 6 $\frac{1}{2}$ (3)14 10 3 16(4)17 1 1 14(
lb. oz. dr.	M. f. p.	Yds. f. in. b.c.
5)46 12 10(6)38 2 14(7)46 0 10 2(
Yds. qrs. na.	A.B. fir. gal.	Cb. bu. p.
8)16 2 2(9)17 3 2(10)20 13 2(
M. w. d.	D. b. m. sec.	o. ' . " .
11)48 2 2(12)46 16 12 30(12)33 4 11(

Questions to exercise D I V I S I O N.

- If 140 s. be divided amongst 40 Men, how much a-piece?
- If 1596 be divided by 21, what is the *Quotient*?
- There are 124 Men, which have 372 l. how much must each Man have?
- An Army of 19000 Men, having plunder'd a City, took 266000 l. how much must each Man have?
- There were a certain Number of Men concern'd in the Payment of 1272 l. and each Man paid 3 l. I demand the Number of Men?
- What is the *Quotient* of 48447, divided by 9 and by 7?
- If 3264, be divided by 12 and by 4, what is the *Quotient*?
- A certain Man, intending to go a Journey of about 3270 Miles, would compleat the same in 136 Days; I demand how many Miles he must travel each Day?

Of REDUCTION.

Q. **W**HAT is Reduction?

A. Reduction is the bringing or reducing Numbers of one Denomination into other Numbers of another Denomination, but of the same Value.

Q. How are Denominations of any kind reduc'd from one to another?

A. By Multiplication and Division.

Q. When is Multiplication to be used?

A. When great Names are to be brought into small; as Pounds into Shillings, or Days into Hours; and this is called Reduction Descending.

Q. When is Division to be used?

A. When small Names are to be brought into great; as Shillings into Pounds, or Hours into Days; and this is called Reduction Ascending.

Note, Whether you multiply or divide, it must be by as many of the less, as make one of the greater Denomination.

Q. How are Questions in Reduction proved?

A. By varying the Order of them.

Of MONEY.

REDUCTION Descending.

1. In 46*l.* how many Shillings and Pence? Answer,
920*s.* 11040*d.*

$$\begin{array}{r}
 46 l. \\
 - 20 \\
 \hline
 920 s. \\
 - 12 \\
 \hline
 11040 d.
 \end{array}$$

2. In 7*l.* how many Shillings and Pence? Answ.
140*s.* 1680*d.*

3. In 9*l.* how many Shillings, Pence and Farthings? Answ.
180*s.* 2160*d.* 8640*qrs.*

4. In 7*l.* 14*s.* 6*d.* $\frac{1}{4}$, how many Farthings? Answ.
7417*qrs.*

5. In 12 Crowns, how many Shillings and Pence? Answ.
60*s.* 720*d.*

6. In 15*l.* how many Crowns and Shillings? Answ.
60*Cr.* 300*s.*

7. In

7. In 50 Half-Crowns, how many Pence and Farthings? *Ans. 1500 d. 6000 qrs.*

8. In 306 Crowns, how many Half-Crowns and Pence? *Ans. 612 Half-Cr. 18360 d.*

9. Reduce 120 Six-pences, into Three-pences, Pence and Farthings. *Facit, 240 Three-pences, 720 d. 2880 qrs.*

10. Reduce 210 Crowns, into Shillings, Groats and Pence. *Facit, 1050 s. 3150 Groats, 12600 d.*

11. Reduce 86 Pounds into Crowns, Shillings and Groats. *Facit, 344 Cr. 1720 s. 5160 Gr.*

12. How many Shillings and Pence are in 17 Guineas? *Ans. 357 s. 4284 d.*

13. How many Crowns and Six-pences are in 28 Pounds? *Ans. 112 Cr. 1120 Six-pences.*

REDUCTION Ascending.

1. In 11040 d. how many Shillings and Pounds? *Ans. 920 s. 46 l.*

20
12)11040(920(46 l.

2. In 1680 d. how many Shillings and Pounds? *Ans. 140 s. 7 l.*

3. In 8640 qrs. how many Pence, Shillings and Pounds? *Ans. 2160 d. 180 s. 9 l.*

4. In 9417 qrs. how many Pounds? *Ans. 7 l. 14 s. 6 d. $\frac{1}{4}$.*

5. In 720 d. how many Shillings and Crowns? *Ans. 60 s. 12 Cr.*

6. In 300 s. how many Crowns and Pounds? *Ans. 60 Cr. 15 l.*

7. In 6000 qrs. how many Pence and Half-Crowns? *Ans. 1500 d. 50 Half-Cr.*

8. In 18360 d. how many Half-Crowns and Crowns? *Ans. 612 Half-Cr. 306 Cr.*

9. Reduce 2880 qrs. into Pence, Three-pences and Six-pences. *Facit, 720 d. 240 Three-pences, 120 Six-pences.*

10. Reduce 12600 d. into Groats, Shillings and Crowns. *Facit, 3150 Gr. 1050 s. 210 Cr.*

11. Reduce 5160 Groats into Shillings, Crowns and Pounds. *Facit, 1720 s. 344 Cr. 86 l.*

12. How many Shillings and Guineas are in 4284 Pence? *Ans. 357 s. 17 Guineas.*

13. How many Crowns and Pounds are in 1120 Six-pences? *Ans. 112 Cr. 28 l.*

REDUCTION Ascending and Descending.

1. In 720 Shillings, how many Pence and Crowns? Answ. 8640 d. 14*l.* Cr.

720 s.

12

60)8640(144 Crowns.

2. In 120 Shillings, how many Crowns and Half-Crowns? Answ. 24 Cr. 48 Half-Cr.

3. In 60 Crowns, how many Shillings and Pounds? Answ. 300 s. 15*l.*

4. In 612 Half-Crowns, how many Crowns and Pence? Answ. 306 Cr. 18360 d.

5. In 40 Guineas, how many Shillings, Crowns and Pounds? Answ. 840 s. 168 Cr. 42*l.*

6. Reduce 12600 Pence, into Shillings, Groats and Crowns. Facit, 1050 s. 3150 Gr. 210 Cr.

7. Reduce 63 Crowns, into Shillings and Guineas. Facit, 315 s. 15 Guineas.

8. Reduce 70 Moidores into Pounds. Facit, 94*l.* 10*s.*

9. Reduce 12180 Three-pences, into Shillings, Pence and Groats. Facit, 3045 s. 36540 d. 9135 Gr.

10. How many Crowns, Groats and Pounds, are in 1720 s.? Answ. 344 Cr. 5160 Gr. 86*l.*

11. How many Groats, Three-pences and Six-pences, are in 121 Shillings? Answ. 363 Gr. 484 Three-pences, 242 Six-pences.

12. How many Pounds and Crowns, are in 1120 Six-pences? Answ. 28*l.* 112 Cr.

13. How many Crowns, Half-Crowns and Shillings, are in 280*l.* and the Number of each equal? Answ. 658, and 7*s.* over.

14. Four Men brought each 17*l.* 10*s.* value in Gold into the Mint, to be coin'd into Guineas, how many must they have? Answ. 66 Guineas, 14*l.*

15. There are 12 Purses, with each 12 Guineas, how much Sterling is the Sum? Answ. 151*l.* 4*s.*

16. A certain Ground-Tenant was behind with his Landlord for 16 Years Rent, at 5*l.* 10*s.* a Year, how much was the Debt? Answ. 88*l.*

17. There are 34*l.* 17*s.* to be divided among 17 Men, how much is it a-piece? Answ. 2*l.* 1*s.*

18. In 19 Moidores, how many Pounds Sterling? Answ. 25*l.* 13*s.*

Of T R O Y - W E I G H T.

1. In 47 lb. 10 oz. how many Grains? *Ans*w. 275520 gr.
2. In 47 1/28 Grains of Gold, how many lb.? *Ans*w. 8 lb. 2 oz. 3 dwts. 16 gr.
3. In 10 lb. of Silver, how many Spoons, each 5 oz. 10 dwts.? *Ans*w. 21 Spoons, and 90 dwts. over.
4. In 4560 Grains of Gold, how many Tea-Spoons, each half an Ounce? *Ans*w. 19 Tea-Spoons.
5. In 47 Salvers, each 20 oz. how many lb.? *Ans*w. 78 lb. 4 oz.
6. How many Porringers, each 11 oz. are in 19 lb. 10 oz. 11 dwts. of Silver? *Ans*w. 21 Porringers, and 151 dwts. over.
7. A Goldsmith having 3 Ingots of Silver, each weighing 27 oz. was minded to make them into Spoons of 2 oz. Cups of 5 oz. Salts of 1 oz. and Snuff-Boxes of 2 oz. and to have an equal Number of each; the Question is, what was that Number? *Ans*w. 8, and 1 oz. over.
8. In 17 Ingots of Silver, each 27 oz. 10 dwts. how many Grains? *Ans*w. 224400 gr.

Of AVOIRDUPOIS-WEIGHT.

Q. Which are the Allowances usually made, in Avoirdupois great Weight, to the Buyer?

A. They are *Tare*, *Trett*, and *Cloff*.

Q. What is *Tare*?

A. *Tare* is an Allowance made to the *Buyer*, for the Weight of the *Box*, *Bag*, *Vessel*, or whatever else contains the Goods bought; and is either,

1. At so much per *Bag*, *Barrel*, *Box*, &c.
2. At so much per *Cent.* Or,
3. At so much in the *Gross Weight*, called *Invoice Tare*.

Q. What is *Trett*?

A. *Trett* is an Allowance, made by the Merchant to the *Buyer*, of 4 lb. in 104 lb. for *Waste* and *Dust*, in some sorts of Goods.

Note, If an Allowance be made both for *Tare* and *Trett*, in the same *Parcel of Goods*; the *Tare* is first to be deducted, and that *Remainder* is called *Suttle Weight*.

Q. What is *Cloff*?

A. *Cloff* is an Allowance of 2 lb. Weight to the *Citizens of London*, on every Draught above 3 C. Weight, on some sorts of Goods; as *Galls*, *Madder*, *Sumac*, *Argol*, &c.

Q. What

Q. What are these Allowances called beyond the Seas ?

A. They are called the Courtesies of London ; because they are not practised in any other Place.

Q. What is Gross Weight ?

A. Gross is the Weight of any sort of Merchandise, and that which contains it, being weighed both together.

Q. What is Neat Weight ?

A. Neat is the pure Weight of the Goods, after all Allowances are deducted.

Note 1. Raw, Long, Short, China, Morea-Silk, &c. are weighed by a great Pound of 24 oz. But Ferret, Filosella, Sleeve-Silk, &c. by the common Pound of 16 oz.

2. To bring great Pounds into common, multiply by 3, and divide by 2.

3. To bring common Pounds into great, multiply by 2, and divide by 3.

C A S E I.

1. In 7 C. 3 qrs. 10 lb. how many Oz. and Drams ?

*Ans*w. 14048 oz. 224768 dr.

2. In 3 Tons of Iron, how many C. qrs. and lb. ? *Ans*w. 60 C. 240 qrs. 6720 lb.

3. In 14048 oz. how many C. ? *Ans*w. 7 C. 3 qrs. 10 lb.

4. In 6720 lb. of Iron, how many Tons ? *Ans*w. 3 Tons.

5. In 461 great Pounds of Morea-Silk, how many Oz. and Drams ? *Ans*w. 11064 oz. 177024 dr.

6. In 40426 Drams of Silk, how many great Pounds ? *Ans*w. 105 great Pounds, 6 oz. 10 dr.

7. In 3 lb. of Cinnamon, how many Parcels, each 12 oz. ? *Ans*w. 4 Parcels.

8. In 470 Parcels of Sugar, each 26 lb. how many C. ? *Ans*w. 109 C. 0 qrs. 12 lb.

9. In 672 great Pounds of Silk, how many common Pounds ? *Ans*w. 1008 common lb.

10. In 480 common Pounds of Silk, how many great Pounds ? *Ans*w. 320 great lb.

11. In 8 Hogsheads of Tobacco, each weighing Neat 7 C. $\frac{1}{2}$, how many Pounds ? *Ans*w. 6720 lb.

12. In 17 Pigs of Lead, each weighing 4 C. $\frac{3}{4}$, how many Fother, at 19 C. $\frac{1}{2}$? *Ans*w. 4 Fother, 2 C. 3 qrs.

13. In 712 C. of Lead, how many Fother ? *Ans*w. 36 Fother, 10 C.

14. In 17 C. 1 qr. 6 lb. of Sugar, how many Parcels, each 17 lb. ? *Ans*w. 114 Parcels.

C A S E 2.

Of T A R E and T R E T T, &c.

Q. When the Tare is at so much per Barrel, Bag, &c. how is the Neat Weight found?

A. Multiply the Number of the said Barrels, Bags, &c. by the Tare, and subtract that Product from the Gross; the Remainder is the Neat.

Note 1. The Table of Allowances for Tare, in the Book of Rates, says;

	For CYPRUS and SMYRNA Silk,	lb.
Bales	about or above 300 lb.	16
	from 300 to 200	14
	from 200 downwards	12
Hhds.	For VIRGINIA Tobacco,	lb.
	5 C. and upwards.	100
	from 5 to 4 C.	90
	from 4 to 3 C.	80
	under 3 C.	70

Sugar from INDIA.

In Casks and Canisters	Tare	$\frac{1}{6}$
In Chests and Casks from St. Thome		$\frac{1}{5}$

Oil from C A N D I A,

Tare 29 lb. per Barrel.

2. 7 lb. $\frac{1}{2}$ of Oil make a Gallon; therefore to reduce Pounds into Gallons, multiply by 2, and divide by 15.

E X A M P L E S.

1. In 16 Hogsheads of Tobacco, each 5 C. 1 qr. 19 lb. Gross, Tare per Hogshead 100 lb. how much Neat Weight?
Answ. 72 C. 1 qr. 20 lb.

C. qr. lb.

5 1 19

4 by the Parts.

16		21	2	20
100				4
—	4 C. qr. lb.			
28)1600(57	14 1 4			
	4			
		Gross	86	2 24
		Tare	14	1 4
		Neat	72	1 20

2. In 70 Bales of Smyrna Silk, each 317 lb. Gross, Tare per Bale 16 lb. how many lb. Neat? Answ. 21070 lb. Neat.

3. In

3. In 14 Hogsheads of Tobacco, weighing Gross 89 C. 3 qrs. 17 lb. Tare per Hogshead 100 lb. how much Neat Weight ? *Answe.* 77 C. 1 qr. 17 lb.

4. What is the Neat Weight of 30 Bales of *Cyprus Silk*, each weighing 249 lb. Gross, Tare per Bale 14 lb. *Answe.* 7050 lb.

C A S E 3.

Q. When the Tare is at so much per Cent. how is the Neat Weight found ?

A. When the Tare is an aliquot Part or Parts of the C. Weight ; divide the whole Gross by the said Part or Parts, that the Tare is of an C. Weight, and the Quotient thence arising, gives the Tare of the Whole ; which subtract from the whole Gross, the Remainder is Neat.

*Note, 1. Figs, Almonds, Argol, &c. - - - 14 lb.
Caroteels, Butts of Currans, &c. 16
Oil in uncertain Casks, &c. - - - 18 } per Cent.*

2. Whatever Part the given Tare is of an C. Weight ; the same must the whole Tare be of the given Gross Weight.

E X A M P L E S.

1. What is the Neat Weight of 12 Barrels of Argol, Gross 48 C. 3 qrs. 12 lb. Tare 14 lb. per Cent.? *Answe.* 42 C. 3 qrs.

$$\begin{array}{r}
 \text{lb.} \quad \text{C. qrs. lb.} \\
 14 = \frac{1}{8} 48 \quad 3 \ 12 \text{ Gross.} \\
 \quad \quad \quad 6 \quad 0 \ 12 \text{ Tare.} \\
 \hline
 \quad \quad \quad 42 \quad 3 \quad 0 \text{ Neat.}
 \end{array}$$

2. In 12 Butts of Currans, each 7 C. 1 qr. 10 lb. Gross, Tare per Cent. 16 lb. how much Neat Weight ? *Answe.* 75 C. 1 qr. 26 lb. 14 oz.

3. What is the Neat Weight of 30 Barrels of Figs, each 2 C. 3 qrs. Gross, Tare per Cent. 14 lb.? *Answe.* 72 C. 21 lb.

Note, When the Tare is not the aliquot Part or Parts of an C. Weight, then multiply the Pounds Gross by the Tare per Cent. given ; and that Product divide by 112, the Quotient is the whole Tare, which subtract from the Gross ; the Remainder is Neat.

4. What is the neat Produce of 20 Barrels of Anchovies, each Gross 33 lb. Tare per Cent. 10 lb. *Answe.* 601 lb. 2 oz.

5. What is the neat Produce of 17 Barrels of Pot-Ash, each Gross 203 lb. Tare 10 lb. per Cent. *Answe.* 3142 lb. 14 oz.

C A S E 4.

Q. When the Tare is at so much in the whole Gross Weight; how is the Neat Weight found?

A. Subtract the Tare from the Gross, and the Remainder is Neat.

E X A M P L E S.

1. What is the Neat Weight of 38 Hogsheads of Tobacco, weighing Gross 201 C. 3 qrs. 12 lb. Tare in the Whole 3140 lb.
Answ. 173 C. 3 qrs. 8 lb.

2. What is the Neat Weight of 3 Hogsheads of Tobacco, weighing as follows, *viz.*

	C. qrs. lb.	lb.
N ^o . 1 —	3 1 2	80
2 —	3 2 1	80
3 —	5 1 12	100

Answ. 9 C. 3 qrs. 7 lb.

C A S E 5.

Q. How is the Neat Weight found, when Trett is allowed with Tare?

A. Divide the Pounds Suttle by 26, the Quotient is the Trett, which subtract from the Suttle, the Remainder is Neat.

E X A M P L E S.

1. In 8 C. 3 qrs. 20 lb. Gross, Tare 38 lb. Trett 4 lb. per 104 lb. how many lb. Neat? Answ. 925 lb. Neat.

2. In 177 C. 0 qr. 22 lb. Gross, Tare 9 lb. per Cent. Trett 4 lb. per 104 lb. how many C. Weight Neat? Answ. 156 C. 2 qrs. 22 lb.

3. In 17 Chests of Sugar, weighing 120 C. 2 qrs. Gross, Tare 176 lb. Trett 4 lb. per 104 lb. how many C. Weight Neat? Answ. 114 C. 1 qr. 12 lb.

Note, There are other Allowances, not so common; such as Break, which is at so much per Barrel, Bag, &c. and Damage, which is so much in the Whole, but they are very easy.

Of APOTHECARIES-WEIGHT.

1. In 12 lb. 1 3. 2 3. 0 3. 1 gr. how many Grains? Answ. 69721 Grains.

2. In 69721 Grains, how many 3. 3. and lb.? Answ. 12 lb. 1 3. 2 3. 0 3. 1 gr.

Of LONG MEASURE.

1. In 70 Miles, how many Furlongs and Poles? Answ. 560 Furlongs, 22400 Poles.

2. In 40 Yards, how many Feet, Inches and Barly-corns? Answ. 120 Feet, 1440 Inches, 4320 Barly-corns.

3. In 5 Miles, how many Barly-corns? Answ. 950400 Barly-corns.

4. How

4. How many Barly-corns in a Mile? *Ans. 190080 Barly-corns.*

5. How many Barly-corns will reach round the Globe of the Earth, which is 360 Degrees, and each Degree 69 Miles and an Half? *Ans. 4755801600 Barly-corns.*

6. In 15840 Yards, how many Miles and Leagues? *Ans. 9 Miles, 3 Leagues.*

7. In 4 Leagues, how many Yards? *Ans. 21120 Yards.*

8. How many times doth the Wheel, which is 18 Feet 6 Inches round, turn between *London* and *York*, which is 150 Miles? *Ans. 42810 times, and 180 Inches over.*

9. In 4000 Inches, how many Yards? *Ans. 111 Yds. 4 In.*

Of CLOTH-MEASURE.

1. In 14 Yards, how many Quarters and Nails? *Ans. 56 Qrs. 224 Nails.*

2. In 17 Yds. 1 qr. 2 na. how many Nails? *Ans. 278 Nails.*

3. In 4712 Nails, how many Yards? *Ans. 294 Yds. 2 qrs.*

4. In 47128 Nails of Holland, how many Pieces, each 12 Yards? *Ans. 245 Pieces, 5 Yards, 2 Quarters.*

5. In 4 Pieces of Cloth, each 14 Yards, how many Quarters and Nails? *Ans. 224 Qrs. 896 Nails.*

6. In 10 Bales of Cloth, each 10 Pieces, each 12 Yards, how many Yards? *Ans. 1200 Yards.*

7. In 7000 Nails of Holland, how many Ells? *Ans. 350 Ells.*

8. Reduce 42 Ells into Quarters and Nails. *Facit 210 Qrs. 840 Nails.*

Of LAND-MEASURE.

1. In 40 Acres, how many Rods and Perches? *Ans. 160 Rods, 6400 Perches.*

2. In 17 A. 3 r. 10 p. how many Perches? *Ans. 2850 Pers.*

3. Reduce 2850 Perches into Acres. *Facit, 17 A. 3 r. 10 p.*

4. If a Piece of Ground contains 24 Acres, and an Inclosure of 17 Acres 3 Rods be taken out of it, how many Perches are there in the Remainder? *Ans. 1000 Perches.*

5. One Field contains 7 Acres, another 10 Acres, and a third 12 Acres, 1 Rood, how many Shares of 76 Perches each, are contained in the Whole? *Ans. 61 Shares, and 44 Perches over.*

Of LIQUID MEASURE.

1. In 17 Gallons, how many Quarts and Pints? *Ans. 68 Qts. 136 Pints.*

2. In 10 Barrels of Beer, how many Gallons and Quarts? *Ans. 360 Gals. 1440 Qts.*

3. In

3. In 4 Barrels of Ale, how many Gallons ? *Ans. 128 Gals.*
4. In 72 Hogsheads of Beer, how many Barrels ? *Ans. 108 Bar.*
5. In 91 Barrels of Beer, how many Hogsheads ? *Ans. 60 Hds. 36 Gals.*
6. If a Back contains 30 Barrels of Beer, how many Gallons doth it hold ? *Ans. 1080 Gals.*
7. In 4 Tuns of Oil, how many Hogsheads, Gallons, and Quarts ? *Ans. 16 Hds. 1008 Gals. 4032 Qts.*
8. In 3 Hogsheads of Brandy, how many half Anchors ? *Ans. 37 half Anchors, 4 Gals.*
9. In 1712 Gallons of Wine, how many Hogsheads ? *Ans. 27 Hds. 11 Gals.*
10. If a Vintner be desirous to draw off a Pipe of Canary into Bottles, containing Pints, Quarts, and two Quarts, and of each an equal Number, how many must he have ? *Ans. 144 of each Sort.*

Of D R Y M E A S U R E.

1. In 40 Quarters of Wheat, how many Bushels and Pecks ? *Ans. 320 Bush. 1280 Pecks.*
2. Reduce 1280 Pecks of Wheat into Quarters. *Facit, 40 Qrs.*
3. In 30 Chaldron of Coals, each 36 Bushels, how many Pecks ? *Ans. 4320 Pecks.*
4. Reduce 7094 Pecks of Coals into Chaldrons. *Facit 49 Chal. 9 Bush. 2 Pecks.*

Of T I M E.

1. In 121812 Seconds, how many Hours ? *Ans. 33 Hrs. 50 Min. 12 Sec.*
2. Reduce 41 Weeks into Days, Hours, and Minutes. *Facit, 287 Days, 6888 Hrs. 413280 Min.*
3. Reduce 413280 Minutes into Weeks. *Facit, 41 Weeks.*
4. How many Days have passed since the Birth of Christ, to Christmas 1743 ? *Ans. 636630 Days, 18 Hours.*
5. How many Seconds in a Year, allowing it to be 365 Days, 6 Hours ? *Ans. 31557600 Seconds.*
6. From March 2, to November 19 following (inclusive) how many Days ? *Ans. 263 Days.*

Of M O T I O N.

1. In half a Year's Time the Sun makes his Progress thro' 6 Signs of the Zodiac, how many Degrees, Minutes, and Seconds, doth that amount to ? *Ans. 180 Degrees, 10800 Min. 648000 Sec.* Of

Of the SINGLE RULE of THREE.

Q. **H**OW many Parts are there in the Rule of Three?

A. Two : Single or Simple, and Double or Compound.

Q. By what is the single Rule of Three known?

A. By three Terms, which are always given in the Question to find a Fourth.

Q. Are any of the Terms given to be reduced from one Denomination to another?

A. If any of the given Terms be of several Denominations, they must be reduced into the lowest Denomination mentioned.

Q. What do you observe concerning the first and third Terms?

A. They must be of the same Name and Kind.

Q. What do you observe concerning the fourth Term?

A. It must be of the same Name and Kind with the Second.

Q. What do you observe of the three given Terms taken together?

A. That the two first are a Supposition, the last is a Demand.

Q. How is the third Term known?

A. It is known by these, or the like Words, *What cost?* *How many?* *How much?*

Q. How many Sorts of Proportion are there?

A. Two : Direct and Inverse.

I. Of DIRECT PROPORTION.

Q. What is Direct Proportion?

A. Direct Proportion is when more requires more, or less requires less.

Q. What do you mean by more requires more, and less requires less?

A. More requires more is when the third Term is greater than the first ; and therefore requires the fourth Term to be greater than the second in the same Proportion : And less requires less is when the third Term is less than the first ; and therefore requires the fourth Term to be less than the second in the like Proportion.

Q. How is the fourth Term in Direct Proportion found?

A. By multiplying the second and third Terms together, and dividing that Product by the first Term.

Q. What Proportion does the fourth Number bear to any other?

A. It bears the same Proportion to the Second, as the Third does to the First.

Q. How do you prove Questions in the Rule of Three Direct?

A. By changing their Order?

EXAMPLES.

EXAMPLES.

1. If 3 Oz. of Silver cost 17s. what will 48 Oz. cost?
Answ. 13*l.* 12*s.*

$$\begin{array}{r} Oz. \quad s. \quad Oz. \\ 3 : 17 :: 48 \\ \quad \quad \quad 17 \\ \hline 3)816(272(13 \quad 12 \end{array}$$

2. If 3 lb. of Ginger cost 3 s. what cost 26 lb.? *Answe.* 1 l. 6s.
3. If 2 oz. of Silk cost 2 s. 6 d. what cost 7 lb.? *Answe.* 7 l.
4. If 1 Gallon of Ale cost 8 d. what cost 36 Gallons?
Answe. 1 l. 4s.
5. If 1 lb. of Sugar cost 4 d. $\frac{1}{2}$, what cost 48 lb.? *Answe.* 18 s.
6. If 1 lb. of Sugar cost 4 d. what cost 1 C.? *Answe.* 1 l. 17 s. 4 d.
7. If an C. of Sugar cost 2 l. 12 s. what cost 1 lb.?
Answe. 5 d. 2 qrs. $\frac{3}{12}$.
8. If 1 Gallon of Beer cost 4 d. what cost a Barrel? *Answe.* 12 s.
9. If 1 Pair of Stockings cost 2 s. 3 d. what cost 19 Dozen
Pair? *Answe.* 25 l. 13 s.
10. If 19 Dozen Pair of Shoes cost 25 l. 13 s. what cost 1
Pair? *Answe.* 2 s. 3 d.
11. Bought a Firkin of Butter, containing 56 lb. for 18 s.
8 d. what is that per lb.? *Answe.* 4 d.
12. Sold 3 C. Weight of Tobacco, at 18 d. per lb. what
is the Price of the Whole? *Answe.* 25 l. 4 s.
13. Bought 19 Chaldrons of Coals, at 29 s. 6 d. per Chal-
drone, what come they to? *Answe.* 28 l. 0 s. 6 d.
14. If 1 lb. of Sugar cost 9 d. what cost 17 C. 2 qrs.?
Answe. 73 l. 10 s.
15. If 1 oz. of Silver cost 5 s. 6 d. what is the Price of a
Tankard that weighs 1 lb. 10 oz. 13 dwts. 4 gr.? *Answe.*
6 l. 3 s. 9 d. 2 qrs. $\frac{9}{480}$.
16. If 1 lb. of Tobacco cost 15 d. what cost 3 bbds. weighing
together 15 C. 1 qr. 19 lb.? *Answe.* 107 l. 18 s. 9 d.
17. If a Yard of Cloth is worth 14 s. what is the Worth of
5 Pieces, each 19 Yards? *Answe.* 66 l. 10 s.
18. If an Ell of Holland cost 4 s. 6 d. what is the Value
of 5 Pieces, each 12 Ells? *Answe.* 13 l. 10 s.
19. If a Bushel of Coals cost 10 d. how many Chaldrons
for 100 l.? *Answe.* 66 Chal. 24 Bush.
20. How many Quarters of Corn for 40 Guineas, at 4 s.
per Bushel? *Answe.* 26 Qrs. 2 Bush.

21. If a Man's Yearly Income be 300*l.* what is it *per Day*? *Ans.* 16*s.* 5*d.* 1*qr.* $\frac{1}{3} \frac{5}{6} \frac{5}{3}$.

22. If a Man spend 7 *Pence per Day*, how much is that in a Year? *Ans.* 10*l.* 12*s.* 11*d.*

23. If a Pint of Wine cost 10*d.* what cost 3 *bbds.*? *Ans.* 6*l.*

24. If a Pipe of Canary cost 40*l.* how much is that *per Pint*? *Ans.* 9*d.* 2*qrs.* $\frac{9}{10} \frac{6}{5} \frac{3}{3}$.

25. Bought 12 Pieces of Cloth, each 12 Yards, at 10*s.* 6*d.* *per Yard*, what come they to? *Ans.* 75*l.* 12*s.*

26. What cost 120 Yards of Cloth, at 3*s.* *per Yard*? *Ans.* 18*l.*

27. A Merchant bought 4 Pieces of Holland, each 12 Ells, for 7*l.* 10*s.* what did 1 Ell cost? *Ans.* 3*s.* 1*d.* $\frac{1}{2}$.

28. A Grocer bought 3 *bbds.* of Sugar, each 10*C.* 3*qrs.* 12*lb.* Gross, Tare 26*lb.* per *bbd.* at 2*d.* $\frac{1}{2}$ per *lb.* I demand what the 3 *bbds.* came to? *Ans.* 37*l.* 3*s.* 9*d.*

29. How much must I pay for the Carriage of 10*C.* $\frac{1}{2}$ at the Rate of 1*d.* $\frac{1}{2}$ *per lb.*? *Ans.* 7*l.* 7*s.*

30. If 6 Horses eat up 21 Bushels of Oats in a Week's Time, how many Bushels will serve 20 Horses the same time? *Ans.* 70 *Bush.*

31. If a Family of 10 Persons spend 3 Bushels of Malt in a Month, how many Bushels will serve them, when they are 30 in Family? *Ans.* 9 *Bush.*

32. If an Ingot of Silver weighs 36*oz.* 10*dwts.* what is it worth, at 5*s.* *per oz.*? *Ans.* 9*l.* 2*s.* 6*d.*

33. How many Yards of Lace for 100*l.* at 3*s.* 6*d.* *per Yard*? *Ans.* 57*l* Yds. $\frac{1}{4} \frac{8}{2}$.

34. If a Merchant hath owing to him 1000*l.* and his Debtor doth agree to Pay him for every Pound, 12*s.* 6*d.* I demand how much he must pay in all? *Ans.* 625*l.*

35. A Goldsmith sold a Tankard for 10*l.* 12*s.* at the Rate of 5*s.* 4*d.* *per oz.* I demand the Weight of it? *Ans.* 39*oz.* 15*dwts.*

36. A Man bought a Piece of Cloth for 16*l.* 10*s.* at 15*s.* *per Yard*, how many Yards did it contain? *Ans.* 22 Yds.

37. If 1*C.* Weight of Cheese cost 37*s.* 4*d.* what is that *per lb.*? *Ans.* 4*d.*

38. Coals at 33*s.* *per Chaldron*, how much *per Bushel*? *Ans.* 11*d.*

39. What cost 49392 Cafe-Knives, at 4*s.* 4*d.* *per Dozen*? *Ans.* 891*l.* 16*s.*

40. If

40. If a Gentleman has an Estate of 245*l.* 10*s.* a Year, how much may he spend one Day with another, to lay up 60 Guineas at the Year's end? *Answ.* 10*s.* per Day.

41. If 17*C.* 3*qrs.* 17*lb.* of Tobacco, cost 133*l.* 13*s.* 4*d.* what cost 1*oz.*? *Answ.* 1*d.*

42. If 1*C.* Weight of Lead cost 15*s.* 11*d.* what cost 5 Pother? *Answ.* 77*l.* 11*s.* 10*d.* $\frac{1}{2}$.

43. When the Tun of Wine cost 42*l.* what cost 1 Quart? *Answ.* 10*d.*

44. At a Noble per Week, how many Months Board may I haye for 50*lb.*? *Answ.* 37 Months, 2 Weeks.

45. What cost a Pack of Wool, weighing 2*C.* 1*qr.* 19*lb.* at 8*s.* 6*d.* per Stone? *Answ.* 8*l.* 4*s.* 6*d.* 1*qr.* $\frac{1}{4}$ ^{lb.}

46. What is Cheese per *C.* Weight, at 3*d.* $\frac{1}{2}$ per *lb.*? *Answ.* 1*l.* 12*s.* 8*d.*

47. If a Yard of Cambric cost 12*s.* what cost 4 Pieces, each 20 Yards? *Answ.* 48*l.*

48. If a Yard of Broad Cloth cost 18*s.* what cost 5 Pieces, each 20 Yards? *Answ.* 90*l.*

49. If Lead be sold for 1*d.* $\frac{1}{2}$ per *lb.* what is 3*C.* Weight worth? *Answ.* 2*l.* 2*s.*

50. If Coffee be sold for 8*d.* $\frac{1}{4}$ per *oz.* what is 6*G.* Weight worth? *Answ.* 369*l.* 12*s.*

2. Of INVERSE PROPORTION.

Q. What is Inverse Proportion?

A. Inverse Proportion is when more requires less, or less requires more.

Q. What is meant by more requires less, and less requires more?

A. More requires less, is when the third Term is greater than the first, and requires the fourth Term to be less than the second: And less requires more is when the third Term is less than the first, and requires the fourth Number to be greater than the second.

Q. How is the fourth Term in Inverse Proportion found?

A. By multiplying the first and second Terms together, and dividing that Product by the third Term.

Q. What Proportion does the fourth Term bear to any of the rest?

A. It bears such Proportion to the Second, as the First does to the Third.

EXAMPLES.

E X A M P L E S.

1. If 48 Men can build a Wall in 24 Days, how many Men can do the same in 192 Days? *Answ. 6 Men.*

2. If I lent my Friend 100*l.* for 6 Months (allowing the Month to be 30 Days) how long ought he to lend me 1000*l.* to requite my Kindness? *Answ. 18 Days.*

3. If 100*l.* in 12 Months gain 6*l.* Interest, what Principal will gain the same in 8 Months? *Answ. 150*l.**

4. If a Footman perform a Journey in 3 Days, when the Days are 16 Hours long, how many Days will he require of 12 Hours long, to go the same Journey in? *Answ. 4 Days.*

5. How many Yards of Matting, that is half Yard wide, will cover a Room that is 18 Feet wide, and 30 Feet long? *Answ. 120 Yards.*

6. If 28*s.* will pay for the Carriage of an C. Weight, 150 Miles; how far may 6 C. Weight be carried for the same Money? *Answ. 25 Miles.*

7. How much in length, that is 3 Inches broad, will make a Foot square? *Answ. 48 Inches.*

8. If 15 Shillings-worth of Wine will serve 46 Men, when the Tun is worth 12*l.* how many Men will the same 15 Shillings-worth suffice, when the Tun is worth but 8*l.*? *Answ. 69 Men.*

9. If when the Price of a Bushel of Wheat is 6*s.* 3*d.* the Penny-Loaf will weigh 9*oz.* what must the Penny-Loaf weigh, when Wheat is at 4*s.* 6*d.* the Bushel? *Answ. 12*oz.* 10*dwts.**

10. Suppose 800 Soldiers were placed in a Garison, and their Provisions were computed sufficient for 2 Months; how many Soldiers must depart, that the Provisions may serve them 5 Months? *Answ. 480 Men.*

11. There is a Cistern having a Cock, which will empty it in 12 Hours; I demand how many Cocks, of the same Capacity, there must be to empty it in a Quarter of an Hour? *Answ. 48 Cocks.*

12. There was a certain Building, rais'd in 8 Months, by 120 Workmen, but the same being demolish'd, it is required to be rebuilt in 2 Months; I demand how many Men must be employed about it? *Answ. 480 Men.*

13. A Piece of Tapestry is 3 Ells Flemish wide, and 4 Ells Flemish long; and it is required to be lined with something that is but 3 Quarters of a Yard wide; I demand how many Yards there must be to complete the Lining? *Answ. 9 Yards.*

Of PRACTICE.

Q. **W**HAT is Practice?

A. It is a short Way of finding the Value of any Quantity of Goods, by the given Price of one Integer.

Q. How do you prove Questions in Practice?

A. By the single Rule of Three Direct: Or Practice may be proved by itself, by varying the Parts.

The TABLES.

s. d.	l. s. d.	l. s. d.	C. wt. lb.
$\frac{1}{2}$ is 6	$\frac{1}{2}$ is 10	0	$\frac{1}{2}$ is 56
$\frac{1}{3}$ 4	$\frac{1}{3}$ 6 8	$\frac{1}{5}$ 1 3	$\frac{1}{4}$ 28
$\frac{1}{4}$ 3	$\frac{1}{4}$ 5 0	$\frac{1}{6}$ 1 0	$\frac{1}{7}$ 16
$\frac{1}{5}$ 2	$\frac{1}{5}$ 4 0	$\frac{1}{8}$ 0 8	$\frac{1}{9}$ 14
$\frac{1}{6}$ 1 $\frac{1}{2}$	$\frac{1}{6}$ 3 4	$\frac{1}{10}$ 0 6	$\frac{1}{12}$ 8
$\frac{1}{7}$ 1	$\frac{1}{7}$ 2 6	$\frac{1}{12}$ 0 4	$\frac{1}{15}$ 7
	$\frac{1}{10}$ 2 0	$\frac{1}{20}$ 0 3	
	$\frac{1}{12}$ 1 8	$\frac{1}{20}$ 0 2	

CASE I.

Q. What must be done with the Price of an Integer, when it is less than a Penny?

A. Find the aliquot Parts of that Price contain'd in a Penny, which must be Divisors to the given Sum; that is, if the Price be a Farthing, say a Farthing is the fourth of a Penny, and set it thus, $\left| \frac{1}{4} \right| \frac{1}{4} \right|$. If the Price be a Halfpenny, then say, a Halfpenny is the half, thus, $\left| \frac{1}{2} \right| \frac{1}{2} \right|$. If it is three Farthings, then say, a Halfpenny is the half of a Penny, and a Farthing is the Fourth of a Penny, thus, $\left| \frac{1}{2} \right| \frac{1}{4} \right|$.

Q. What do you observe concerning these Columns?

A. The first Column contains the Money, and the other the Parts.

Note 1. When there are more aliquot Parts than one, their Quotients must be added together, and the Sum, if the first aliquot Part be taken from a Penny, will be Pence; if it be taken from a Shilling, will be Shillings; or if it be taken from a Pound, will be Pounds.

2. It is, frequently, better to take Parts of Parts, than Parts of the whole Price; and then the three Farthings above-mentioned may as well be taken thus, $\left| \frac{1}{2} \right| \left| \frac{1}{2} \right|$ that is, a Halfpenny is the half of a Penny, and a Farthing is the half of a Halfpenny.

E X A M P L E S.

$\frac{3}{4}$	$\frac{1}{4}$	7612 at $\frac{3}{4}$
12		1903
20		1518
		71. 18s. 7d.
$\frac{1}{2}$	$\frac{1}{2}$	6812 at $\frac{1}{2}$
12		3406
20		2813 10
		14l. 3s. 10d.
$\frac{1}{2}$	$\frac{1}{2}$	4712 at $\frac{3}{4}$
$\frac{1}{4}$	$\frac{1}{2}$	2356
		1178
12		3534
20		2914 6
		14l. 14s. 6d.

1280 at $\frac{1}{4}$
Facit 1l. 6s. 8d.
7672 at $\frac{1}{2}$
Facit 15l. 19s. 8d.
9180 at $\frac{3}{4}$
Facit 28l. 13s. 9d.

C A S E 2.

Q. What must be done with the Price of an Integer, when it is less than a Shilling?

A. Find the aliquot Parts of that Price contain'd in a Shilling, which must be Divisors to the given Sum. Or thus,

If the given Price be not the aliquot Part of a Shilling, then first take some Part of it that is an aliquot Part; and for the remaining Part of the Price, let it be taken out of the foregoing Part or Parts, and then add the Quotients together as before; the Total will be the Answer in Shillings.

E X A M P L E S.

1	$\frac{1}{2}$	7612 at 1 d.
20		6314
		31l. 14s. 4d.
1	$\frac{1}{2}$	8612 at 1 d. $\frac{1}{4}$
$\frac{1}{4}$	$\frac{1}{4}$	717 8
		179 5
20		8917 1
		44l. 17s. 1 d.

6812 at 1 d.
Facit 28l. 7s. 8d.
1861 at 1 d. $\frac{1}{4}$
Facit 9l. 13s. 10d. $\frac{1}{4}$
4121 at 1 d. $\frac{1}{2}$
Facit 25l. 15s. 1 d. $\frac{1}{2}$

1861 at 1 d. $\frac{3}{4}$
Facit 13 l. 11 s. 4 d. $\frac{3}{4}$
4761 at 2 d.
Facit 39 l. 13 s. 6 d.
6181 at 2 d. $\frac{1}{4}$
Facit 57 l. 18 s. 11 d. $\frac{1}{4}$
1218 at 2 d. $\frac{1}{2}$
Facit 12 l. 13 s. 9 d.
8012 at 2 d. $\frac{3}{4}$
Facit 91 l. 16 s. 1 d.
7612 at 3 d.
Facit 95 l. 3 s.
6128 at 3 d. $\frac{1}{4}$
Facit 82 l. 19 s. 8 d.
6180 at 3 d. $\frac{1}{2}$
Facit 90 l. 2 s. 6 d.
7812 at 3 d. $\frac{3}{4}$
Facit 122 l. 1 s. 3 d.
8120 at 4 d.
Facit 135 l. 6 s. 8 d.
7000 at 4 d. $\frac{1}{4}$
Facit 123 l. 19 s. 2 d.

6001 at 4 d. $\frac{1}{2}$
Facit 112 l. 10 s. 4 d. $\frac{1}{2}$
7121 at 4 d. $\frac{3}{4}$
Facit 140 l. 18 s. 8 d. $\frac{1}{4}$
7181 at 5 d.
Facit 149 l. 12 s. 1 d.
8121 at 5 d. $\frac{1}{4}$
Facit 177 l. 12 s. 11 d. $\frac{1}{4}$
6128 at 5 d. $\frac{1}{2}$
Facit 140 l. 8 s. 8 d.
6100 at 5 d. $\frac{3}{4}$
Facit 146 l. 2 s. 11 d.
1000 at 6 d.
Facit 25 l.
7610 at 6 d. $\frac{1}{4}$
Facit 198 l. 3 s. 6 d. $\frac{1}{2}$
1218 at 6 d. $\frac{1}{2}$
Facit 32 l. 19 s. 9 d.
6000 at 6 d. $\frac{1}{4}$
Facit 168 l. 15 s.
7101 at 7 d.
Facit 207 l. 2 s. 3 d.
1001

1001 at 7 d. $\frac{1}{4}$ Facit 30 l. 4 s. 9 d. $\frac{1}{4}$ 4100 at 7 d. $\frac{1}{2}$

Facit 128 l. 2 s. 6 d.

6120 at 7 d. $\frac{3}{4}$

Facit 197 l. 12 s. 6 d.

7100 at 8 d.

Facit 236 l. 13 s. 4 d.

6100 at 8 d. $\frac{1}{2}$

Facit 209 l. 13 s. 9 d.

8000 at 8 d. $\frac{1}{2}$

Facit 283 l. 6 s. 8 d.

6000 at 8 d. $\frac{3}{4}$

Facit 218 l. 15 s.

9000 at 9 d.

Facit 337 l. 10 s.

4121 at 9 d. $\frac{1}{4}$ Facit 158 l. 16 s. 7 d. $\frac{1}{4}$ 6100 at 9 d. $\frac{1}{2}$

Facit 241 l. 9 s. 2 d.

5918 at 9 d. $\frac{3}{4}$ Facit 240 l. 8 s. 4 d. $\frac{1}{2}$

8121 at 10 d. *

Facit 338 l. 7 s. 6 d.

6712 at 10 d. $\frac{1}{4}$

Facit 286 l. 13 s. 2 d.

1002 at 10 d. $\frac{1}{2}$

Facit 43 l. 16 s. 9 d.

4680 at 10 d. $\frac{3}{4}$

Facit 209 l. 12 s. 6 d.

1260 at 11 d.

Facit 57 l. 15 s.

6121 at 11 d. $\frac{1}{4}$ Facit 286 l. 18 s. 5 d. $\frac{1}{4}$ 1234 at 11 d. $\frac{1}{2}$

Facit 59 l. 2 s. 7 d.

2345 at 11 d. $\frac{3}{4}$ Facit 114 l. 16 s. 1 d. $\frac{1}{4}$ 100 at 11 d. $\frac{3}{4}$

Facit 4 l. 17 s. 11 d.

* Note, When the Price of an Integer is 10 d. annex a Cypher to the given Number, and divide by 12 and by 20.

C A S E 3.

Q. What must be done with the Price of an Integer, when it is greater than a Shilling, but less than two Shillings?

A. Let the Part or Parts be taken only with so much of the given Price as is more than one Shilling; that is, if the Price be $14d. \frac{1}{2}$, take the Parts only with $2d. \frac{1}{2}$, and let the given Quantity stand for Shillings, which must be added with the rest; and the Total will be the Answer in Shillings.

E X A M P L E S.

$\frac{1}{4}$	$\frac{1}{4}$	486 at $12d.\frac{1}{4}$
12		$121 \frac{1}{2}$
		$101 \frac{1}{2}$
210		$49161 \frac{1}{2}$
		$24l. 16s. 1d.\frac{1}{2}$
$\frac{1}{2}$	$\frac{1}{2}$	486 at $12d.\frac{1}{2}$
12		243
		203
210		5063
		$25l. 6s. 3d.$
		7612 at $12d.\frac{1}{4}$
		Facit 388l. 10s. 7d.
		1216 at $12d.\frac{1}{2}$
		Facit 63l. 6s. 8d.
		1216 at $12d.\frac{3}{4}$
		Facit 64l. 12s.
		6121 at $13d.$
		Facit 331l. 11s. 1d.

1281	at $13d.\frac{1}{4}$
Facit	$70l. 14s. 5d.\frac{1}{4}$
6100	at $13d.\frac{1}{2}$
Facit	$343l. 2s. 6d.$
1210	at $13d.\frac{3}{4}$
Facit	$69l. 6s. 5d.\frac{1}{2}$
1210	at $14d.$
Facit	$70l. 11s. 8d.$
1271	at $14d.\frac{1}{4}$
Facit	$75l. 9s. 3d.\frac{3}{4}$
6120	at $14d.\frac{1}{2}$
Facit	$369l. 15s.$
1210	at $14d.\frac{3}{4}$
Facit	$74l. 7s. 3d.\frac{1}{2}$
1260	at $15d.$
Facit	$78l. 15s.$

1612 at 15 d. $\frac{1}{4}$	4560 at 18 d.
Facit 102 l. 8 s. 7 d.	Facit 342 l.
1210 at 15 d. $\frac{1}{2}$	5670 at 18 d. $\frac{3}{4}$
Facit 78 l. 2 s. 11 d.	Facit 431 l. 3 s. 1 d. $\frac{1}{2}$
7612 at 15 d. $\frac{3}{4}$	6789 at 18 d. $\frac{1}{2}$
Facit 499 l. 10 s. 9 d.	Facit 523 l. 6 s. 4 d. $\frac{1}{2}$
6100 at 16 d.	7890 at 18 d. $\frac{3}{4}$
Facit 406 l. 13 s. 4 d.	Facit 616 l. 8 s. 1 d. $\frac{1}{2}$
7121 at 16 d. $\frac{1}{4}$	8900 at 19 d.
Facit 482 l. 3 s. 0 d. $\frac{1}{4}$	Facit 704 l. 11 s. 8 d.
1218 at 16 d. $\frac{1}{2}$	9000 at 19 d. $\frac{3}{4}$
Facit 83 l. 14 s. 9 d.	Facit 721 l. 17 s. 6 d.
8100 at 16 d. $\frac{3}{4}$	9876 at 19 d. $\frac{1}{2}$
Facit 565 l. 6 s. 3 d.	Facit 802 l. 8 s. 6 d.
4128 at 17 d.	8765 at 19 d. $\frac{3}{4}$
Facit 292 l. 8 s.	Facit 721 l. 5 s. 8 d. $\frac{3}{4}$
1230 at 17 d. $\frac{1}{4}$	7120 at 20 d. $\frac{1}{4}$
Facit 88 l. 8 s. 1 d. $\frac{1}{2}$	Facit 600 l. 15 s.
2340 at 17 d. $\frac{1}{2}$	6543 at 20 d. $\frac{1}{2}$
Facit 170 l. 12 s. 6 d.	Facit 558 l. 17 s. 7 d. $\frac{1}{2}$
3450 at 17 d. $\frac{3}{4}$	5432 at 20 d. $\frac{3}{4}$
Facit 255 l. 3 s. 1 d. $\frac{1}{2}$	Facit 469 l. 12 s. 10 d.

4321 at 21 d.	6700 at 22 d. $\frac{1}{2}$
Facit 378 l. 1 s. 9 d.	Facit 628 l. 2 s. 6 d.
3210 at 21 d. $\frac{1}{4}$	6812 at 22 d. $\frac{3}{4}$
Facit 284 l. 4 s. 4 d. $\frac{1}{2}$	Facit 645 l. 14 s. 5 d.
2100 at 21 d. $\frac{1}{2}$	1210 at 23 d.
Facit 188 l. 2 s. 6 d.	Facit 115 l. 19 s. 2 d.
1000 at 21 d. $\frac{3}{4}$	1800 at 23 d. $\frac{1}{4}$
Facit 90 l. 12 s. 6 d.	Facit 174 l. 7 s. 6 d.
1090 at 22 d. *	6760 at 23 d. $\frac{1}{2}$
Facit 99 l. 18 s. 4 d.	Facit 661 l. 18 s. 4 d.
9010 at 22 d. $\frac{1}{4}$	9990 at 23 d. $\frac{3}{4}$
Facit 835 l. 6 s. 0 d. $\frac{1}{2}$	Facit 988 l. 11 s. 10 d. $\frac{1}{2}$

* Note, When the Price of an Integer is 22 d. annex a Cypher to the given Number, and divide by 12 (as at 10 d.) then add both Lines together; the Sum will be the Total in Shillings.

C A S E 4.

Q. What must be done with the Price of an Integer, when it is any even Number of Shillings under 20, as 6 s. 8 s. &c.

A. Multiply the given Quantity by half of the Price, and double the first Figure of the Product for Shillings, and the rest of the Product will be Pounds.

E X A M P L E S.

486 at 2 s.	7612 at 2 s.
1	Facit 761 l. 4 s.
48 l. 12 s.	1286 at 4 s.
769 at 4 s.	Facit 257 l. 4 s.
2	
153 l. 16 s.	D. 4 7612

7618 at 6 s.	171 at 14 s.
Facit 2285 l. 8 s.	Facit 119 l. 14 s.
191 at 8 s.	171 at 16 s.
Facit 76 l. 8 s.	Facit 136 l. 16 s.
180 at 10 s. *	712 at 18 s.
Facit 90 l.	Facit 640 l. 16 s.

* Note, When the Price of an Integer is 10 s. you may take half of the given Integers, and it is done; and the Remainder (If there be any) will be 10 Shillings.

C A S E 5.

Q. What must be done with the Price, of an Integer, when it is any odd Number of Shillings under 20, as 3 s. 5 s. &c.

A. Multiply the given Integers by the Price, and that Product divide by 20, the Quotient will be the Answer.

E X A M P L E S.

121 at 1 s.	121 at 11 s.
Facit 6 l. 1 s.	Facit 66 l. 11 s.
121 at 3 s.	600 at 13 s.
Facit 18 l. 3 s.	Facit 390 l.
471 at 5 s. *	190 at 15 s.
Facit 117 l. 15 s.	Facit 142 l. 10 s.
860 at 7 s.	121 at 17 s.
Facit 301 l.	Facit 102 l. 17 s.
612 at 9 s.	100 at 19 s.
Facit 275 l. 8 s.	Facit 95 l.

* Note, When the Price of an Integer is 5 s. the Work may be done at once, because 5 s. is the fourth Part of a Pound.

C A S E

C A S E 6.

Q. What must be done with the Price of an Integer, when it is Shillings and Pence?

A. 1. If the Shillings and Pence be the aliquot Part of a Pound, it may be done at once, as 6s. 8d. is the third of a Pound.

E X A M P L E S.

12 at 6s. 8d.	21 at 2s. 6d.
Facit 4l.	Facit 2l. 12s. 6d.
69 at 3s. 4d.	96 at 1s. 8d.
Facit 11l. 10s.	Facit 8l.

2. If the Shillings and Pence be not the aliquot Part of a Pound, or if there be Shillings, Pence, and Farthings, multiply the given Quantity by the Shillings, and take Parts with the rest, and add them together; the Sum will be the Answer in Shillings.

E X A M P L E S.

3 $\frac{1}{4}$	126 at 9s. 3d.	70 at 7s. 4d. $\frac{3}{4}$
	9	Facit 25l. 17s. 8d. $\frac{1}{2}$
	1134	55 at 4s. 8d. $\frac{1}{2}$
	31 6	Facit 12l. 18s. 11d. $\frac{1}{2}$
20	116 5 6	77 at 10s. 6d. $\frac{1}{4}$
	58l. 5s. 6d.	Facit 40l. 10s. 1d. $\frac{1}{4}$
	86 at 6s. 10d.	12 at 13s. 10d. $\frac{1}{2}$
	Facit 29l. 7s. 8d.	Facit 8l. 6s. 6d.
	10 at 12s. 4d.	17 at 17s. 4d. $\frac{1}{4}$
	Facit 6l. 3s. 4d.	Facit 14l. 15s. 0d. $\frac{1}{4}$
	30 at 4s. 9d.	46 at 7s. 3d. $\frac{3}{4}$
	Facit 7l. 2s. 6d.	Facit 16l. 16s. 4d. $\frac{1}{2}$
	73 at 7s. 6d.	
	Facit 27l. 7s. 6d.	

C A S E 7.

Q. What must be done with the Price of an Integer, when it is Pounds only?

A. Multiply the given Integers by the Price, the Product will be the Answer.

E X A M P L E S.

72 at 5 l.	19 at 4 l.
Facit 360 l.	Facit 76 l.
64 at 3 l.	46 at 7 l.
Facit 192 l.	Facit 322 l.

C A S E 8.

Q. What must be done with the Price of an Integer, when it is Pounds and Shillings?

A. Multiply the Integers given, by the Pounds ; then proceed with the Shillings, if the Number be even, according to Case 4 ; but if the Shillings be odd, according to Case 5, and add them together ; the Total will be the Answer.

E X A M P L E S.

26 at 4 l. 8 s.	48 at 7 l. 10 s.
4	
104	
10 8	
114 l. 8 s.	Facit 360 l.
49 at 3 l. 7 s.	26 at 11 l. 14 s.
7	
210	
3 4 1 3	Facit 304 l. 4 s.
1 7 3	
1 4 7	
1 6 4 l. 3 s.	15 at 4 l. 13 s.
36 at 5 l. 13 s.	Facit 69 l. 15 s.
	17 at 9 l. 15 s.
Facit 203 l. 8 s.	Facit 165 l. 15 s.
	16 at 3 l. 6 s.
	Facit 52 l. 16 s.

C A S E

C A S E 9.

Q. What must be done with the Price of an Integer, when it is Pounds, Shillings, and Pence?

A. 1. If the Shillings and Pence be the aliquot Parts of a Pound, multiply the given Integers by the Pounds, and divide by the aliquot Parts: those Numbers so found out, being added together, will be the Sum required.

E X A M P L E S.

47 at 3 l. 3 s. 4 d.	17 at 2 l. 6 s. 8 d.
Facit 148 l. 16 s. 8 d.	Facit 39 l. 13 s. 4 d.
20 at 4 l. 13 s. 4 d.	30 at 1 l. 2 s. 6 d.
Facit 93 l. 6 s. 8 d.	Facit 33 l. 15 s.

2. If the Shillings and Pence be not the aliquot Parts of a Pound, or if there be Shillings, Pence and Farthings given with the Pounds, then reduce the Pounds and Shillings into Shillings, and multiply the given Integers by the said Shillings; next take Parts with the rest of the Price, and add them together as before.

E X A M P L E S.

3 $\frac{1}{4}$ 1 2 0 at 4 l. 7 s. 3 d. $\frac{1}{2}$	21 at 5 l. 14 s. 7 d. $\frac{1}{4}$
	8 7 20
	1 1 4 4 0 87
$\frac{1}{2}$ $\frac{1}{8}$ 3 0	
	5
2, 1 0 4 7 1 5	
	5 2 3 l. 15 s.
14 at 2 l. 10 s. 6 d.	46 at 3 l. 19 s. 8 d. $\frac{1}{2}$
Facit 35 l. 7 s.	Facit 183 l. 6 s. 7 d.

Q. What other Ways have you of answering Questions in this Case?

A. 1. When the Number of Integers does not exceed 12, multiply the Price by the Integers, as in Compound Multiplication, the Product will be the Answer.

2. When the Number of Integers does exceed 12, multiply the Price by the Parts instead of the Whole. Or,

3. You

3. You may multiply the *Price* by the whole Number of *Integers*. Thus,

58361 *Hbds.* of *Tobacco*, at 48*l.* 12*s.* 9*d.* per *Hbd.*

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>Memorandum.</i>
48	12	9	
	58361		
48	12	9	
2918	5	0	16 6
14591	5	0	18 3 2 6
389100	0	0	2 0
2431875	0	0	3 9 17 6 15 0 10 0
2838533	2	9	

Q. How is it wrought?

A. Multiply by the several Figures in the *Multiplier*, as in *Compound Multiplication*, but with this Difference, that the *Products* of the *Shillings* and *Pence*, multiplied by the 6, 3, 8, and 5, must be placed by themselves in a *Memorandum*, and the *Products* of the *Pounds* by the same Figures, placed as in *Simple Multiplication*. Thus,

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>Memor.</i>
48	12	9	
	58361		
1 Product	48	12	9
2	- - - - -	291	16 6
3	- - - - -	145	18 3
4	- - - - -	389	2 0
5	- - - - -	243	3 9

Then to fill up the *Blanks* in the *second Product*, take half of the 16*s.* in the *Memorandum*, which is 8, and set it in the *Units Place* of the *Pounds*. Annex a *Cypher* to the 6*d.* which makes 60*d.* or 5*s.* place this under the *Shillings*, and the Line is done with; there being no *Pence* remaining.

For the *Blanks* in the *third Product*, take half of the 18*s.* in the *Memorandum*, and put it in the *Tens Place* of the *Pounds*. Annex a *Cypher* to the 3*d.* which makes 30*d.* or 2*s.* 6*d.* this put in the *second Memorandum*. Then take half of the 2*s.* in this new *Memorandum*, and put it in the *Units Place* of the *Pounds*. Annex a *Cypher* to the 6*d.* in the new *Memorandum*, which makes 60*d.* or 5*s.* put this in the *Place of Shillings*, and this Line is finished, there being no *Pence* remaining.

For the Blanks in the *fourth Product*, take half of the 2*s.* in the first *Memorandum*, and put it in the *Hundreds Place* of the *Pounds*; and because there remains nothing, nor is there any *Pence* in the *Memorandum*, therefore fill up the other *Blanks* with *Cyphers*, and the Line is finished.

For the *Blanks* in the *fifth Product*, take half of the 3*s.* in the first *Memorandum*, and put it in the *Thousands Place* of the *Pounds*; then because there is one remaining, put that in the *second Memorandum*. Annex a *Cypher* to the 9*d.* which makes 90*d.* or 7*s.* 6*d.* put this to the former 1, and it makes 17*s.* 6*d.* take half of the 17*s.* and put it in the *Hundreds Place* of the *Pounds*; then because there is 1 remaining, put that in the *third Memorandum*. Annex a *Cypher* to the 6*d.* and it makes 60*d.* or 5*s.* put this to the 1 in the *third Memorandum*, and it makes 15*s.* take half of the 15*s.* and put it in the *Tens Place* of the *Pounds*; then because there remains 1, put it in the *fourth Memorandum*, and since there are no *Pence* in the *third Memorandum* to put a *Cypher* to, let a *Cypher* be annexed to the 1 in the *last Memorandum*, which makes 10*s.* take half of this 10*s.* and put it in the *Units Place* of the *Pounds*; then because there are no *Pence* in the *Memorandum*, neither is there any thing remaining of the 10, therefore fill up the other *Blanks* with *Cyphers*, and the Line is compleated: Add all together, and their *Sum* is the *Total Product* of the *Whole*.

1. s. d.	Memorandum.
7000 Hbds of Wines, at 17 14 8 per Hbd.	1. 2. 3.
7000	s. d. s. d. s. d.
124133 6 8	2 8 6 8 6 8

Note, 1. To fill up the Blanks in the *Pounds* of the *Second*, *Third*, &c. *Products*, always take half of the *Shillings* in the *Memorandum*; and if 1 remains, make a new *Memorandum* of it.

2. Always annex a *Cypher* to the *Pence*, and whatever *Number* of *Shillings* they make, put them to the 1 in the new *Memorandum*, and so on till all the *Blanks* in the *Pounds* are filled up: If there be any *Pence* yet remaining in the *Memorandum*, put a *Cypher* to them, and what *Shillings* and *Pence* they make, let them be put in the *Shillings* and *Pence Place* in the *Product*.

3. All the Examples in this Case, and Case 8, may serve here instead of others.

C A S E 10.

Q. What must be done with the Price of an Integer, when both that and the Quantity given are of several Denominations?

A. Multiply the Price by the Integers; and take Parts with the Parts of the Integer.

E X A M P L E S.

C. grs. lb.	l. s.			l. s. d.		
32 3 16 of Tobacco, at 4 12 per C.wt.	Facit 59 6 1½ +					
	12	12	12			
	55 4					
	2 6					
	1 3					
	0 13	1½	+			
				59	6	1½ +

C. grs. lb.	l.	s.	d.	l.	s.	d.
12 2 14 of Tobacco, at 3 14	0	per C.		Facit 46	14	3
17 3 19 of Sugar, at 2 2	6	per C.		Facit 38	1	6½
4 1 16 of Soap, at 3 12	0	per C.		Facit 15	16	3½
10 0 12 of Tallow, at 1 19	6	per C.		Facit 19	19	2½
5 1 0 of Tobacco, at 2 17	0	per C.		Facit 14	19	3
4 3 0 of Sugar, at 2 18	6	per C.		Facit 13	17	10½
7 0 19 of Sugar, at 3 16	0	per C.		Facit 27	4	10½
5 2 10 of Tobacco, at 2 18	6½	per C.		Facit 16	7	2½
7 1 14 of Tobacco, at 3 15	9½	per C.		Facit 27	18	9½
9 2 26 of Tallow, at 4 10	4½	per C.		Facit 43	19	6

Of I N T E R E S T.

Q. *HOW* many kinds of Interest are there?
 A. Two: *Simple* and *Compound*.

Of Simple I N T E R E S T.

Q. *What is Simple Interest?*
 A. *Simple Interest* is the *Profit* allow'd in the lending or forbearance of any Sum of Mony for some determin'd Space of Time.
 Q. *What is the Principal?*
 A. *The Principal* is any Sum of Mony lent, for which *Interest* is to be received.

Q. *What is the Rate per Cent.?*
 A. It is a certain *Sum* agreed on between the *Lender* and the *Borrower*, to be paid for every 100 *Pounds*, for the Use of the *Principal*, which according to the *Laws of England*, ought not to be above 5*l.* for the Use of 100*l.* for one Year, and 10*l.* for the Use of 100*l.* for two Years; and so on for any Sum of Mony, in Proportion to the Time proposed.

Q. *What*

Q. What is the Amount ?

A. It is the Principal and Interest added together.

Q. What other Things is Interest applicable to ?

A. It is applied to Commission or Provision, Brokage, Storage, and Insurance, which have no respect to Time.

C A S E I.

Q. How do you find the Interest of any given Sum for a Year ?

A. Multiply the Principal by the Rate per Cent. and divide that Product by 100, the Quotient is the Interest required.

Q. How do you find the Interest of any given Sum for several Years ?

A. Multiply the Interest for one Year, by the Number of Years given in the Question ; the Product will be the Answer.

E X A M P L E S.

1. If 100*l.* in one Year's Time yield 5*l.* Interest ; what will 486*l.* yield in the same Time ? *Answe.* 24*l.* 6*s.*

$$\begin{array}{r}
 1. \\
 486 \\
 \hline
 5 \\
 \hline
 24 \mid 30 \\
 \quad \quad \quad 20 \\
 \hline
 \quad \quad \quad 6 \quad 00
 \end{array}$$

2. What is the Interest of 220*l.* for a Year, at 4 per Cent. per Ann. ? *Answe.* 8*l.* 16*s.*

3. What is the Interest of 76*l.* for 2 Years, at 5 per Cent. per Ann. ? *Answe.* 7*l.* 12*s.*

4. What is the Amount of 400*l.* for 12 Years, at 6 per Cent. per Ann. ? *Answe.* 688*l.*

Of Factors Allowances, commonly called Commission or Provision.

Q. What is Commission or Provision ?

A. It is an Allowance from Merchants to their Factors or Agents beyond Sea, in the buying or selling of any sort of Goods ; and is a certain Rate per Cent. according to the Custom of the Country where the Factor resides.

E X A M P L E S.

5. My Factor sends me Word, that he has bought Goods to the Value of 500*l.* 13*s.* 6*d.* upon my Account ; I demand what his Commission comes to, at $3\frac{1}{2}$ per Cent. *Answe.* 17*l.* 10*s.* 5*d.* 2*qrs.* $\frac{68}{100}$.

6. My

6. My Correspondent has disbursed upon my Account, the Sum of 1009*l.* 18*s.* what must he demand for his Commission, when I allow him $2\frac{1}{4}$ per Cent.? *Answ.* 22*l.* 14*s.* 5*d.* 1*gr.* $\frac{84}{100}$.

7. Suppose I allow my Correspondent $1\frac{3}{4}$ per Cent. for Provision; what may he demand on the Disbursement of 704*l.* 15*s.* 4*d.*? *Answ.* 12*l.* 6*s.* 8*d.* $\frac{2}{100}$.

C A S E 2.

Q. How do you find the Interest of any Sum for $\frac{1}{4}$, $\frac{1}{2}$, or $\frac{3}{4}$ of a Year, beside the Number of Years given in the Question?

A. For $\frac{1}{4}$ of a Year, take a fourth Part of the Interest for one Year; for $\frac{1}{2}$ a Year, take half of the Interest for one Year; for $\frac{3}{4}$ of a Year, take the Parts compounded of $\frac{3}{4}$, and add them to the Interest for the rest of the Time; the Sum will be the Interest required.

E X A M P L E S.

1. What is the Interest of 200*l.* for 3 Years and $\frac{3}{4}$, at 5 per Cent. per Annum? *Answ.* 37*l.* 10*s.*

200	$\frac{1}{2}$	$\frac{1}{2}$	10
5			3
1000			—
			30
	$\frac{1}{4}$	$\frac{1}{2}$	5
			2 10
			37 10

2. What is the Interest of 468*l.* 12*s.* 4*d.* for 1 Year and $\frac{3}{4}$, at 6 per Cent. per Annum? *Answ.* 49*l.* 4*s.* 1*d.*

3. What is the Interest of 112*l.* 10*s.* 4*d.* for 5 Years and $\frac{1}{2}$, at 6 per Cent. per Annum? *Answ.* 37*l.* 2*s.* 6*d.*

4. What is the Interest of 468*l.* for 4 Years and $\frac{1}{4}$, at 6 per Cent. per Annum? *Answ.* 119*l.* 6*s.* 8*d.* $\frac{3}{4}$.

5. What is the Interest of 1000*l.* for 2 Years $\frac{3}{4}$, at 4 per Cent. per Annum? *Answ.* 110*l.*

Of B R O K A G E.

Q. What is Brokage?

A. It is an Allowance made to Persons called *Brokers*, at a certain Rate per Cent. for finding Customers, and selling to them the Goods of other Men, whether Strangers or Natives.

Q. How do you find the Brokage of any Sum?

A. Divide the given Sum by 100, and take Parts from the Quotient with the Rate per Cent.

E X A M P L E S.

E X A M P L E S.

6. What is the Brokage of 709 l. 14 s. 6 d. at 4 s. per Cent.?
Ans. 1 l. 8 s. 0 d. $\frac{1}{4}$.

<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>l.</i>	<i>s.</i>	<i>d.</i>
7	00	14	4	$\frac{1}{3}$	$7 \ 0 \ 1\frac{1}{2}$
20					
—					
0	14		1	8	$0\frac{1}{4}$
12					
—					
1	74				
4					
—					
2	69				

7. What may a Broker demand for Brokage, when he sells Goods to the Value of 500 l. 10 s. 7 d. and I allow him 7 s. per Cent.? *Ans. 1 l. 15 s. 0 d. $\frac{1}{4}$.*

8. Suppose I employ a Broker, who sells Goods to the Value of 909 l. 14 s. 10 d. what is the Brokage at 6 s. 6 d. per Cent.? *Ans. 2 l. 19 s. 1 d. $\frac{1}{4}$.*

Note, If the Brokage should be 1 l. or more per Cent. the Operation will be the same with that in Factors Allowances.

C A S E 3.

Q. How is the Interest of any Sum found, when the Rate per Cent. is $\frac{1}{4}$, $\frac{1}{2}$, or $\frac{3}{4}$, more than the Pounds given in the said Rate?

A. Multiply the Principal by the Pounds, in the Rate per Cent. as before; and let the Parts for $\frac{1}{4}$, $\frac{1}{2}$, or $\frac{3}{4}$, be taken from the Principal, and added to that Product; then proceed according to Case 1 or 2.

E X A M P L E S.

1. What is the Interest of 400 l. for 2 Years, at $5\frac{1}{2}$ per Cent. per Annum? *Ans. 44 l.*
2. What is the Interest of 120 l. for a Year, at $4\frac{1}{2}$ per Cent. per Annum? *Ans. 5 l. 8 s.*
3. What is the Amount of 690 l. for 3 Years, at $4\frac{1}{4}$ per Cent. per Annum? *Ans. 777 l. 19 s. 6 d.*
4. What is the Amount of 120 l. 10 s. for 2 Years and an Half, at $4\frac{3}{4}$ per Cent. per Annum? *Ans. 134 l. 16 s. 1 d. $\frac{3}{4}$.*
5. What is the Interest of 300 l. for 5 Years and 3 Quarters, at $3\frac{3}{4}$ per Cent. per Annum? *Ans. 64 l. 13 s. 9 d.*

C A S E 4.

Q. How do you find the Interest of any Sum, for a certain Number of Weeks?

A. As 52 Weeks

Are to the Interest of the given Sum for a Year:

So are the Weeks given,

To the Interest required.

E X A M P L E S.

1. What is the Interest of 400*l.* for a Week, at 5 per Cent. per Annum? Answ. 7*s.* 8*d.* 1*qr.* $\frac{1}{2}$.

2. What is the Interest of 126*l.* 12*s.* for 16 Weeks, at 4*1\frac{1}{2}* per Cent. per Annum? Answ. 1*l.* 15*s.* 0*d.* 2*qr.* $\frac{3}{4}$.

3. What is the Amount of 500*l.* for 20 Weeks, at 3*1\frac{1}{2}* per Cent. per Annum? Answ. 506*l.* 14*s.* 7*d.* 1*qr.* $\frac{2}{3}$.

C A S E 5.

Q. How is the Principal found, when the Amount, Time, and Rate per Cent. are given?

A. As the Amount of 100*l.* at the Rate and Time given
Is to 100*l.*

So is the Amount given

To the Principal required.

E X A M P L E S.

1. What Principal being put to Interest for 9 Years, at 5 per Cent. per Annum, will amount to 725*l.*? Answ. 500*l.*

2. What Principal being put to Interest for 7 Years, will amount to 793*l.* 12*s.* at 4 per Cent. per Annum? Answ. 620*l.*

3. What Sum being put to Interest, will amount to 520*l.* 16*s.* in 8 Years, at 3 per Cent. per Annum? Answ. 420*l.*

C A S E 6.

Q. How is the Rate per Cent. found, when the Amount, Time and Principal are given?

A. 1. As the Principal

Is to the Interest for the whole Time:

So is 100*l.*

To its Interest for the same Time.

2. Divide the Interest, last found, by the Time, and the Quotient will be the Rate per Cent.

E X A M P L E S.

1. At what Rate of Interest per Cent. will 500*l.* amount to 725*l.* in 9 Years Time? Answ. 5 per Cent.

2. At what Rate of Interest per Cent. will 620*l.* amount to 793*l.* 12*s.* in 7 Years? Answ. 4 per Cent.

3. At

3. At what Rate of Interest per Cent. will 420*l.* amount to 520*l.* 16*s.* in 8 Years? *Ans.* 3 per Cent.

C A S E 7.

Q. How is the Time found, when the Principal, Amount, and Rate per Cent. are given?

A. As the Interest of the Principal for 1 Year at the given Rate Is to one Year: So is the whole Interest To the Time required.

E X A M P L E S.

1. In what Time will 500*l.* amount to 725*l.* at 5 per Cent. per Annum? *Ans.* 9 Years.

2. In what Time will 620*l.* amount to 793*l.* 12*s.* at 4 per Cent. per Annum? *Ans.* 7 Years.

3. In what Time will 420*l.* amount to 520*l.* 16*s.* at 3 per Cent. per Annum? *Ans.* 8 Years.

Q. How are the Questions in the foregoing Cases proved?

A. Cases 1, 5, 6 and 7 do exactly prove each other, by varying the Questions; yet all of them except Case 5; and the 1st, 2d, 5th, 6th, and 7th, Questions in Case 1; and the 6th, 7th, and 8th, in Case 2, may as truly be answered by the Double Rule of Three; of which more hereafter.

Note. 1. The 1st, 2d, 5th, 6th, and 7th, Questions in Case 1; and the 6th, 7th, and 8th, in Case 2, are to be proved by the Single Rule of Three.

2. Case 5, cannot be answered by the Double Rule of Three, because the Principal is not known in the Question, and therefore there can be no Deduction of it from the Amount, to know the Interest, which must first be done.

Of Simple Interest for Days.

Q. How do you find the Interest for any Number of Days?

A. Multiply the Pence of the Principal by the Days, and by the Rate of Interest for a Dividend, and 365 by 100 for a Divisor, the Quotient will be the Answer in Pence.

Q. How are the following Questions proved?

A. As 365 Days

Are to the Interest of the given Sum for a Year:

So is the Time proposed

To the Interest required.

E X A M P L E S.

1. What is the Interest of 120*l.* for 126 Days, at 4 per Cent. per Annum? *Ans.* 1*l.* 13*s.* 1*d.* 2*qrs.* $\frac{258}{365}$.

2. What is the Interest of 126*l.* for 145 Days, at 6 per Cent. per Annum? *Ans.* 3*l.* 0*s.* 0*d.* 3*qrs.* $\frac{57}{365}$.

3. What

3. What is the Interest of 100*l.* from June 1, 1743, to March 9, 1744, which is Leap Year, at 5 per Cent. per Annum? *Ans.* 3*l.* 17*s.* 6*d.* 1*qr.* $\frac{235}{365}$.

4. What is the Interest of 200*l.* from August 14, to December 19 following, at 6 per Cent. per Annum? *Ans.* 4*l.* 4*s.* 1*d.* 3*grs.* $\frac{325}{365}$.

5. What is the Interest of 10*l.* for 25 Days, at 5 per Cent. per Annum? *Ans.* 8*d.* $\frac{80}{365}$.

6. What is the Interest of 40*l.* for 40 Days, at 4 per Cent. per Annum? *Ans.* 3*s.* 6*d.* $\frac{30}{365}$.

See more of Simple Interest in Decimals.

Of Compound INTEREST.

Q. What is Compound Interest?

A. Compound Interest is that which arises from any Principal, and its Interest put together, as the Interest still becomes due; and for that Reason it is called Interest upon Interest, or Compound Interest.

Q. Is it lawful to let out Money at Compound Interest?

A. No: Yet in purchasing of Annuities, or Pensions, and Leases in Reversion, it is very usual to allow Compound Interest to the Purchaser for his Ready-Money; and therefore it is very necessary to understand it. [See more of this in Decimals.]

Q. How do you find the Compound Interest of any given Sum for any Number of Years.

A. 1. Find the Amount of the given Sum by Simple Interest, for the first Year, which is the Principal for the second Year: then find the Amount of that Principal for the second Year, and that is the Principal for the third Year; and so on for any Number of Years given.

2. Subtract the given Sum from the last Amount, and the Remainder is the Compound Interest required.

E X A M P L E S.

1. What Sum will 450*l.* amount to in 3 Years, at 5 per Cent. per Annum, Compound Interest? *Ans.* 520*l.* 18*s.* 7*d.* $\frac{1}{2}$.

2. What will 400*l.* amount to in 4 Years, at 6 per Cent. per Annum, Compound Interest? *Ans.* 504*l.* 19*s.* 9*d.* $\frac{1}{4}$.

3. What will 480*l.* amount to in 6 Years, at 5 per Cent. per Annum, Compound Interest? *Ans.* 643*l.* 4*s.* 10*d.* $\frac{1}{2}$.

4. What will 500*l.* amount to in 4 Years, at 4*1*/*4* per Cent. per Annum, Compound Interest? *Ans.* 590*l.* 11*s.* 5*d.* $\frac{1}{2}$.

5. What is the Compound Interest of 400*l.* 10*s.* at 3*1*/*2* per Cent. per Annum for 3 Years? *Ans.* 43*l.* 10*s.* 9*d.* $\frac{1}{2}$.

Of REBATE or DISCOUNT.

Q. **W**HAT is Rebate or Discount?

A. *Rebate or Discount* is when a Sum of Money due at any Time to come, is satisfied by paying so much present Money, as being put out to *Interest*, would amount to the given Sum in the same space of Time.

Q. How is the Operation perform'd?

A. 1. As 12 Months

Are to the Rate per Cent. :

So is the Time proposed

To a fourth Number.

2. Add that fourth Number to 100*l.*

3. As that Sum

Is to the fourth Number :

So is the given Sum

To the Rebate.

4. Subtract the Rebate from the given Sum, and the Remainder is the present Worth. Or thus,

3. As that Sum

Is to 100*l.* :

So is the given Sum

To the present Payment.

4. Subtract the present Worth from the given Sum, and the Remainder is the Rebate.

Q. How do you prove Questions in Rebate?

A. Find the Amount of the present Payment at the Time and Rate per Cent. given, and that will be equal to the given Sum.

E X A M P L E S.

1. What is the Rebate of 795*l.* 11*s.* 2*d.* for 11 Months, at 6 per Cent.? *Answ.* 41*l.* 9*s.* 5*d.* 3*qrs.* $\frac{1572}{2532}$.

2. What is the present Worth of 161*l.* 10*s.* for 19 Months, at 5 per Cent.? *Answ.* 149*l.* 13*s.* 0*d.* $\frac{3}{4}$.

3. Sold Goods for 795*l.* 11*s.* 2*d.* to be paid 4 Months hence, what is the present Worth, at $3\frac{1}{2}$ per Cent.? *Answ.* 786*l.* 7*s.* 8*d.* $\frac{1}{4}$.

4. What is the present Worth of 4000*l.* payable in 9 Months, at $4\frac{3}{4}$ per Cent.? *Answ.* 3862*l.* 8*s.* 0*d.* $\frac{1}{2}$.

5. How much Ready-Mony for a Note of 18*l.* due 15 Months hence, at 5 per Cent.? *Answ.* 16*l.* 18*s.* 10*d.*

6. Suppose 810*l.* were to be paid 3 Months hence, allowing 5 per Cent. Discount, what must be paid in Hand? *Answ.* 800*l.*

7. If

7. If a Legacy of 1000*l.* is left me *July 24, 1743,* to be paid on the *Christmas-Day* following; what must I receive, when I allow 6 per Cent. for present Payment? *Answe.* 975*l.* 3*s.* 1*d.*

8. Being obliged by a Bond bearing Date *August 29, 1743,* to pay next *Midsummer* 326*l.* what must I pay down, if they allow Discount after the Rate of 8 per Cent.? *Answe.* 305*l.* 16*s.* 6*d.* $\frac{1}{4}$.

9. Sold Goods for 312*l.* to be paid at two 3 Months, (that is, half at 3 Months, and the other half at 3 Months after that) what must be discounted for present Payment, at 5 per Cent.? *Answe.* 5*l.* 14*s.* 7*d.*

10. Sold Goods for 300*l.* to be paid at three two Months, (that is one-third at 2 Months, one-third at 4 Months, and one-third at 6 Months) what must be discounted for present Payment, at 4 per Cent.? *Answe.* 3*l.* 18*s.* 9*d.*

11. What is the present Worth of 100*l.* at 5 per Cent. payable at two 4 Months? *Answe.* 97*l.* 11*s.* 4*d.* $\frac{1}{2}$.

12. I would know the present Worth of 150*l.* payable at three 4 Months, at 5 per Cent. Discount? *Answe.* 145*l.* 3*s.* 9*d.* $\frac{1}{4}$.

13. What is the present Worth of 200*l.* at 4 per Cent. payable as follows, *viz.* 100*l.* at 2 Months; 50*l.* at 3 Months; and 50*l.* at 5 Months? *Answe.* 198*l.* 0*s.* 6*d.*

Of EQUATION of PAYMENTS;

The common Way.

Q. **W**HAT is Equation of Payments?

A. When several Sums of Mony, to be paid at different Times, are reduced to one mean Time for the Payment of the Whole, without Loss to Debtor, or Creditor, this is called *Equation of Payments.*

Q. Wherein may the Debtor or Creditor be said to suffer Loss, when the Debt is paid?

A. 1. When one *mean Time* is assigned for the Payment of the whole Debt, and the Mony is not paid till sometime afterwards; then the *Debtor* suffers *Loss* by paying not only the *Principal*, or Sum due, but also the *Interest* of that Sum for the Time of Forbearance, at 3, 4, or more per Cent. as they shall agree. Likewise if the Mony be paid before it is due, then the *Creditor* suffers *Loss*, by allowing so much per Cent. by Agreement, for the Time of *prompt Payment.*

2. The

2. The *Loss* to either Party, may be in reducing the several Times of Payment to one, which is not the true equated *Time*; and then if the *Payment* be made after the true *Time*, the *Creditor* suffers *Loss*, because he receives no *Interest* for it: If the *Time* agreed on be before the true *Time*, then the *Debtor* suffers *Loss*, because he receives no *Interest* for his early *Payment*.

Q. *How is the Operation wrought?*

A. Multiply each *Payment* by its *Time*, and divide the *Sum* of all the *Products* by the whole *Debt*, the *Quotient* is the *equated Time*.

E X A M P L E S.

1. *A* owes *B* 100*l.* whereof 50*l.* is to be paid at 2 Months, and 50*l.* at 4 Months; but they agree to reduce them to one *Payment*; when must the *Whole* be paid? *Ans*w. 3 Months.

2. A Merchant hath owing him 300*l.* to be paid as follows; 50*l.* at 2 Months, 100*l.* at 5 Months, and the rest at 8 Months; and it is agreed to make one *Payment* of the *Whole*; I demand when that *Time* must be? *Ans*w. 6 Months.

3. *F* owes to *H* 1000*l.* whereof 200*l.* is to be paid present, 400*l.* at 5 Months, and the rest at 10 Months, but they agree to make one *Payment* of the *Whole*; I demand the *equated Time*? *Ans*w. 6 Months.

4. *K* is indebted to *L* a certain *Sum*, which is to be discharged at 4 several *Payments*, that is, $\frac{1}{4}$ at 2 Months, $\frac{1}{4}$ at 4 Months, $\frac{1}{4}$ at 6 Months, and $\frac{1}{4}$ at 8 Months; but they agreeing to make but one *Payment* of the *Whole*, the *equated Time* is therefore demanded? *Ans*w. 5 Months.

5. *H* bought of *X* a *Quantity* of *Goods* upon *Trust*, for which *H* was to pay $\frac{1}{3}$ of the *Debt* every 3 Months, till the *Whole* was discharged; but they afterwards agreed to pay the *Whole* at one *equated Time*; the *Time* is demanded? *Ans*w. 6 Months.

6. *W* owes *Z* a *Sum* of *Mony*, which is to be paid, $\frac{1}{4}$ present, $\frac{1}{4}$ at 4 Months, and the rest at 8 Months, what is the *equated Time* for the *Whole*? *Ans*w. 3 Months.

7. *P* owes *Q* 420*l.* which will be due 6 Months hence; but *P* is willing to pay him 60*l.* now, provided he can have the rest forborn a longer *Time*: It is agreed on; the *Time* of *Forbearance* therefore is required? *Ans*w. 7 Months.

Note, This Question is in *Reverse Proportion*. See more of this Rule in *Decimals*.

Of

Of B A R T E R.

Q. **W**HAT is Barter?

A. Barter is the Exchanging of one Commodity for another, and informs Merchants so to proportion their Quantities, as that neither may sustain Loss.

Q. How do^l you prove Questions in Barter?

A. By changing the Order of them.

E X A M P L E S.

1. How much Sugar, at 9 d. per lb. must be given in Barter for 6 C. $\frac{1}{2}$ of Tobacco, at 14 d. per lb.? Answ. 10 C. 0 qr. 12 lb. $\frac{4}{9}$.

2. What Quantity of Tea, at 10 s. per lb. must be given in Barter for 1 C. of Chocolate, at 4 s. per lb.? Answ. 44 lb. 12 oz. $\frac{8}{15}$.

3. How much Rice, at 28 s. per C.wt. must be bartered for 3 C. $\frac{1}{2}$ of Raisins, at 5 d. per lb.? Answ. 5 C. 3 qrs. 9 lb. $\frac{112}{335}$.

4. A and B bartered: A had 5 C. of Sugar, at 6 d. per lb. which he gave to B for a Quantity of Cinnamon, at 10 s. 8 d. per lb. I demand how much Cinnamon B gave A? Answ. 26 lb. 4 oz.

5. B deliver'd 3 Hbds. of Brandy, at 6 s. 8 d. per Gallon, to C for 126 Yards of Cloth; what was the Cloth per Yard? Answ. 10 s.

6. A and B bartered: A had 12 C. of Sugar, worth 4 d. per lb. for which B gave him 1 C. $\frac{3}{4}$ of Cinnamon; I demand how B rated his Cinnamon per lb.? Answ. 27 d. $\frac{84}{196}$.

7. A hath Linen-Cloth, worth 20 d. an Ell Ready-Mony; but in Barter he will have 2 s. B hath broad Clothe, worth 14 s. 6 d. per Yard ready Mony; at what Price ought the broad Cloth to be rated in Barter? Answ. 17 s. 4 d. 3 qrs. $\frac{4}{20}$ per Yard.

8. A and B. barter: A hath 41 C.wt. of Hops, at 30 s. per C. for which B giveth him 20 l. in Mony, and the rest in Prunes, at 5 d. per lb. I demand how many Prunes B gave A besides the 20 l.? Answ. 17 C. 3 qrs. 4 lb.

9. C. hath Candles, at 6 s. per Dozen ready Mony; but in Barter he will have 6 s. 6 d. per Dozen: D hath Cotton, at 9 d. per lb. ready Mony; I demand what Price the Cotton must be at in Barter; also how much Cotton must be bartered for 100 Dozen of Candles? Answ. The Cotton is 9 d. 3 qrs. per lb. in Barter; and 7 C. 0 qr. 16 lb. of Cotton must be given for 100 Dozen of Candles.

Of LOSS and GAIN.

Q. **W**HAT is Loss and Gain?

A. Loss and Gain is a Rule which teaches Merchants what they shall gain or lose in the Sale of their Goods, having the Price that they bought them for, and the Price for which they are to be sold both known.

Q. How are the following Questions proved?

A. Let them be varied.

E X A M P L E S.

1. Bought 18 C. of Cheese, at 28s. per C. which I sell out again at 3d. $\frac{1}{2}$ per lb. what is the Profit in the Whole? *Answe.* 4l. 4s.

2. If I buy Deals in at 20d. a-piece, and sell them again at 17d. what shall I lose by 120 Dozen? *Answe.* 18l.

3. Hats bought at 4s. a-piece, and sold again at 4s. 9d. what is the Profit in laying out 100l.? *Answe.* 18l. 15s.

4. Bought 19 Fother of Lead, at 14s. per C. what is gained by the Whole, sold out at 4d. per lb.? *Answe.* 432l. 5s.

5. Bought 60 Reams of Paper, at 15s. per Ream, what is the Loss in the whole Quantity, at 4 per Cent.? *Answe.* 1l. 16s.

6. Bought 7 Tuns of Wine, at 17l. per Hhd. which I sell again at 1s. per Pint; I demand the whole Gain, and the Gain per Cent.? *Answe.* 229l. 12s. whole Gain; and 48l. 4s. 8d. 1 qr. $\frac{4}{7} \frac{2}{16}$ the Gain per Cent.

7. If I sell 500 Deals at 15d. a-piece, and 9l. per Cent. Loss; what do I lose in the whole Quantity? *Answe.* 2l. 16s. 3d.

8. Bought 3 Oxen for 24l. 10s. which I sell again for 2s. per Stone, what ought the 3 Oxen to weigh together; the Hides and Offal being the only clear Gain? *Answe.* 245 Stone.

9. A Draper bought 100 Yards of broad Cloth, for which he gave 56l. I desire to know how he must sell it per Yard, to gain 19l. in the Whole? *Answe.* 15s. per Yard.

10. A Draper bought 100 Yards of broad Cloth for 56l. I demand how he must sell it per Yard, to gain 15l. in laying out 100l.? *Answe.* 12s. 10d. 2 qrs. $\frac{2}{100}$.

Of FELLOWSHIP.

Q. **H**OW many sorts of Fellowship are there?

A. Two: Single and Compound.

Of SINGLE FELLOWSHIP.

Q. What is Single Fellowship?

A. Single Fellowship is when the Stocks of each Partner continue for an equal Term of Time.

Q. What is the Rule?

*A. As the Sum of the several Stocks
Is to the Total Gain or Loss :
So is each Man's Share in Stock
To his Share of the Gain or Loss.*

Q. How is this Rule proved?

A. Add all the Shares together, and the Sum will be equal to the given Gain or Loss.

Note, This Way of proving Fellowship, will not hold good always: For if an Error should be committed in the Beginning of the Work, and carried on thro' the whole Operation, yet the same will prove, tho' each Man's Share of the Gain or Loss assigned him by that Operation, be either more or less than his true Share. The most exact Method, then, that I would propose, tho' something more tedious, is to change the Order of the Question, and put each Man's Share of the Gain or Loss in the Place of his Stock first laid out, and make the Sum of the Stocks stand in the Place of the whole Gain or Loss; and then it will be

*As the Total Gain or Loss
Is to the Sum of the several Stocks :
So is each Man's Share of the Gain or Loss
To his particular Share in Stock.*

Q. What else doth this Rule belong to beside Fellowship?

A. By it the Estate of a Bankrupt may be divided among his Creditors: Also Legacies may be adjusted, when there is a Deficiency of Effects.

E X A M P L E S.

1. *A* and *B* were Sharers in a Parcel of Merchandise, in the Purchase of which, *A* laid out 3*l.* and *B* 7*l.* and the Commodity being sold, they find their clear Gain amount to 25*s.* what Part of it must each Man have? *Answ. A must have 7*s.* 6*d.* and B. 17*s.* 6*d.**

2. *A, B, and C*, trading together, gain'd 120*l.* which is to be shared according to each Man's Stock; *A* put in 140*l.* *B* 300*l.* and *C* 160*l.* what is each Man's Share? *Answ. A 28*l.* B 60*l.* C. 32*l.**

3. Three Merchants trading to *Virginia*, lost Goods to the Value of 800*l.* Now if *A*'s Stock was 1200*l.* *B*'s 4800*l.* and *C*'s 2000*l.* what Sum did each Man lose? *Answ. A lost 120*l.* B 480*l.* C 200*l.**

4. Three Merchants traded together, and they put into one common Stock 1000*l.* each Man, and gained 600*l.* how much must each Man have? *Answ. 200*l.* each Man.*

5. Four Men traded with a Stock of 800*l.* and they gain'd in two Years Time twice as much, and 40*l.* over; *A*'s Stock was 140*l.* *B*'s 260*l.* *C*'s 300*l.* I demand *D*'s Stock, and what each Man gain'd by Trading? *Answ. D's Stock was 100*l.* and A gain'd 287*l.* B 533*l.* C. 615*l.* and D 205*l.**

6. *A,*

6. *A, B, and C*, trading to *Guinea* with 480*l.* 680*l.* and 840*l.* in three Years Time did gain 1010*l.* how much is each Man's Share of the Gain? *Ans*w. *A* 242*l.* 8*s.* *B* 343*l.* 8*s.* *C* 424*l.* 4*s.*

7. *A, B, and C*, freighted a Ship from the *Canaries* to *England*, with 108 Tuns of Wine, of which *A* had 48; *B* 36; *C* 24; but by reason of bad Weather, they were obliged to cast 45 Tuns overboard; how much must each Man sustain of the Loss? *Ans*w. *A* 20 Tuns, *B* 15 Tuns, *C* 10 Tuns.

8. A Merchant is indebted to *S* 70*l.* to *T* 400*l.* to *V* 140*l.* 12*s.* 6*d.* but upon his Decease, his Estate is found to be worth no more than 409*l.* 14*s.* how must it be divided among his Creditors? *Ans*w. *S* must have 46*l.* 19*s.* 3*d.* 3*qrs.* $\frac{141750}{146550}$.

T - - - 268 7 7 1 $\frac{77250}{146550}$.

V - - - 94 7 0 2 $\frac{74100}{146550}$.

9. If the Money and Effects of a Bankrupt amount to 1400*l.* 14*s.* 6*d.* and he is indebted to *A* 742*l.* 12*s.* to *B* 641*l.* 19*s.* 8*d.* and to *C* 987*l.* 19*s.* 9*d.* how must it be divided among them? *Ans*w. *A* must have 438*l.* 8*s.* 4*d.* 1*qr.* $\frac{303527}{569417}$.

B - - - 379 0 3 3 $\frac{158361}{569417}$.

C - - - 583 5 9 3 $\frac{107529}{569417}$.

Of COMPOUND FELLOWSHIP.

Q. What is Compound Fellowship?

A. Compound Fellowship is when the Stocks continue an unequal Term of Time.

Q. What is the Rule?

- A. 1. Multiply each Man's Stock and Time together.
2. Add the several Products, thence arising, together.
3. As the Sum of those Products

Is to the whole Gain or Loss:

So is each Product

To its Share of the Gain or Loss.

Q. How is this Rule proved?

A. As in Single Fellowship.

E X A M P L E S.

1. Three Merchants traded together: *A* put in 120*l.* for 9 Months; *B* 100*l.* for 16 Months; and *C* 100*l.* for 14 Months; and they gain'd 100*l.* how must it be divided? *Ans*w. *A* must have 26*l.* 9*s.* 4*d.* 3*qrs.* $\frac{3120}{4680}$.

B - - - 39 4 3 3 $\frac{240}{4680}$.

C - - - 34 6 3 1 $\frac{720}{4680}$.

2. Three Merchants join in Trade: *A* put in 400*l.* for 9 Months; *B* 680*l.* for 5 Months; *C* 120*l.* for 12 Months; but by Misfortune lost Goods to the Value of 500*l.* what must each Man sustain of the Loss? *Answ.*

<i>A</i>	must	lose	213 <i>l.</i>	5 <i>s.</i>	4 <i>d.</i>	3 <i>grs.</i>	$\frac{2840}{8440}$
<i>B</i>	-	-	201	8	5	0	$\frac{2840}{8440}$
<i>C</i>	-	-	85	6	1	3	$\frac{6200}{8440}$

3. *A, B, and C*, hold a Pasture in common, for which they pay 20*l.* per Annum. In this Pasture *A* had 40 Oxen for 76 Days; *B* had 36 Oxen for 50 Days; and *C* had 50 Oxen for 90 Days. I demand what Part every of these Tenants ought to pay of the 20*l.* *Answ.* *A* ought to pay 6*l.* 10*s.* 2*d.* 1*gr.* $\frac{2340}{9340}$.

<i>B</i>	-	-	3	17	1	0	$\frac{2000}{9340}$
<i>C</i>	-	-	9	12	8	2	$\frac{5000}{9340}$

Of the DOUBLE RULE of THREE.

Q. *By what is the Double Rule of Three known?*

A. By five Terms, which are always given in the Question to find a Sixth.

Q. *In what Proportion is the Sixth Term to be found?*

A. If the Proportion is *Direct*; the *Sixth Term* must bear such Proportion to the *Fourth* and *Fifth*, as the *Third* bears to the *First* and *Second*: But if the Proportion is *Inverse*, then the *Sixth Term* must bear such Proportion to the *Fourth* and *Fifth*, as the *First* bears to the *Second* and *Third*, or as the *Second* bears to the *First* and *Third*.

Note. It is to be observed here, as in the Single Rule of Three, that *Direct Proportion* is when more requires more, or less requires less; and *Inverse Proportion* is when more requires less, or less requires more.

Q. *What do you observe concerning the Five given Terms?*

A. That the *three first Terms* are a *Supposition*; the *two last* are a *Demand*.

Q. *How must the Numbers given in the Question be stated?*

A. By two *Single Rules of Three*: Or otherwise, thus,

1. Let the *Principal Cause of Loss or Gain, Interest or Decrease, Action or Passion*, be put in the *first Place*.

2. Let that which betokeneth *Time, distance of Place, and the like*, be put in the *second Place*; and the remaining one in the *third Place*.

3. Place the other *two Terms* under their like in the *Supposition*.

4. If the *Blank* falls under the *third Term*, multiply the *first* and *second Terms* for a *Divisor*, and the other *Three* for a *Dividend*.

5. If

5. If the Blank falls under the *first* or *second Term*, multiply the *third* and *fourth Terms* for a *Divisor*, and the other *Three* for a *Dividend*; and the *Quotient* will be the *Answer*.

Note, *When the Blank falls under the third Term, the Proportion is Direct; but when it falls under the first or second Term, the Proportion is Inverse.*

Q. *How are the following Questions proved?*

A. Let them be varied; or else work the same Questions by two *Single Rules of Three*.

E X A M P L E S.

1. If 7 Men can reap 84 Acres of Wheat in 12 Days; how many Men can reap 100 Acres in 5 Days? *Answ. 20 Men.*

2. If 7 *Qrs.* of Malt are sufficient for a Family of 7 Persons for 4 Months; how many *Qrs.* are enough for 46 Persons 10 Months? *Answ. 115 Qrs.*

3. If 8 Reapers have 3*l. 4s.* for 4 Days Work; how much will 48 Men have for 16 Days Work? *Answ. 76*l. 16s.**

4. If 10 Bushels of Oats be enough for 18 Horses 20 Days; how many Bushels will serve 60 Horses 36 Days? *Answ. 60 Bush.*

5. If a Footman travel 240 Miles in 12 Days, when the Days are 12 Hours long; how many Days may he travel 720 Miles in, of 16 Hours long? *Answ. 27 Days.*

6. If 56*lb.* of Bread will be sufficient for 7 Men, 14 Days; how much Bread will serve 21 Men 3 Days? *Answ. 36*lb.**

7. If 700*l.* in half a Year, raise 14*l.* Interest; how much will 400*l.* raise in 5 Years? *Answ. 80*l.**

8. If 30*s.* be the Hire of 8 Men for 3 Days; how many Days must 20 Men work for 15*l.*? *Answ. 12 Days.*

9. If 4 Reapers have 24*s.* for 3 Days Work; how many Men will earn 4*l. 16s.* in 16 Days? *Answ. 3 Men.*

10. An Usurer put out 86*l.* to receive Interest for the same; and when it had continued 8 Months, he receiv'd for Principal and Interest 88*l. 17s. 4d.* I demand at what Rate *per Cent.* *per Annum* he received Interest? *Answ. 5*l. per Cent.**

11. What is the Interest of 200*l.* for 3 Years and $\frac{3}{4}$, at 5 *per Cent. per Annum?* *Answ. 37*l. 10s.**

12. What is the Interest of 400*l.* for a Week, at 5 *per Cent. per Annum?* *Answ. 7*s. 8*d. 1*qr. $\frac{1}{2}$****

13. What is the Interest of 120*l.* for 126 Days, at 4 *per Cent. per Annum?* *Answ. 1*l. 13*s. 1*d. 2*qr. $\frac{2}{3} \frac{5}{8}$*****

Note, *The Rule for working Questions in Simple Interest for Days, p. 67.*
is taken from this Rule, as appears by this last Example.

Of CONJOIN'D PROPORTION.

Q. What is Conjoin'd Proportion?

A. Conjoin'd Proportion is when the *Coin*, *Weights*, or *Measures* of several Countries are compared in the same Question; or it is a linking together of many *Proportions*.

C A S E 1.

Q. When it is required to know how many of the first sort of Coin, Weight or Measure, mentioned in the Question, are equal to a given Number of the last; how must the Question be answered?

A. 1. Place the Numbers alternately, beginning at the *left Hand*; and let the last Number stand on the *left Hand*.

2. Multiply the *first Rank* continually for a *Dividend*, and the *second* for a *Divisor*.

Q. How is Conjoin'd Proportion proved?

A. Make as many *Single Rules of Three* as the Nature of the Question requires.

E X A M P L E S.

1. If 100 lb. English make 95 lb. Flemish; and 19 lb. Flemish 25 lb. at Bolonia; how many lb. English are equal to 50 lb. at Bolonia? Answ. 40 lb. English.

2. If 25 lb. at London be 22 lb. at Nurenburgh; 88 lb. at Nurenburgh 92 lb. at Hamburg; 46 lb. at Hamburg 49 lb. at Lyons; how many lb. at London are equal to 98 lb. at Lyons? Answ. 100 lb.

3. If 6 Braces at Leghorn, make 3 Ells English; 5 Ells English 9 Braces at Venice; how many Braces at Leghorn will make 45 Braces at Venice? Answ. 50 Braces at Leghorn.

4. If 3 Ells English make 6 Braces at Leghorn; and 150 Braces at Leghorn 135 Braces at Venice; how many Ells English are equal to 27 Braces at Venice? Answ. 15 Ells English.

C A S E 2.

Q. When it is required to know how many of the last sort of Coin, Weight or Measure, mention'd in the Question, are equal to a given Number of the first; how must the Question be answered?

A. 1. Place the Numbers alternately, as in *Case 1*, but let the last Number stand on the *right Hand*.

2. Multiply the *second Rank* for a *Dividend*, and the *first* for a *Divisor*.

E X A M P L E S.

1. If 10 lb. at London make 9 lb. at Amsterdam; 90 lb. at Amsterdam 112 lb. at Thoulouse; how many lb. at Thoulouse are equal to 50 lb. at London? Answ. 56 lb. at Thoulouse.

2. If 20 Braces at Leghorn be equal to 10 Vares at Lisbon; 40 Vares at Lisbon to 80 Braces at Lucca; how many Braces at Lucca are equal to 100 Braces at Leghorn? Answ. 100 Braces at Lucca.

Of EXCHANGE.

Q. **W**HAT is Exchange?

A. Exchange is the giving of the *Mony, Weight, or Measure* of one Country, for the like Value in *Bills, Mony, Weight, or Measure* of another Country.

Q. *What is the Course of Exchange?*

A. It is the *Value of Mony agreed on among Merchants.*

Q. *Is the Course of Exchange always the same?*

A. No: The *Course of Exchange* raises or falls almost every Day, according as *Mony* is plenty or scarce; or according to the *Time* allowed for *Payment* of the *Mony* in *Exchange*, and then the *Value* is said to be above or under *Par*.

Q. *What is the Par of Exchange?*

A. It is the *intrinsic Value of any Foreign Mony compared with Sterling Mony.*

Q. *How are Questions in Exchange proved?*

A. By changing the Order of them.

C A S E I.

Q. *What Places does London exchange with in Dollars, or Pieces of Eight of Mexico?*

A. With *Madrid*, and *Cadiz* in *Spain*; and with *Genoa*, and *Leghorn* in *Italy*.

Q. *How do they keep their Accompts in Spain?*

A. In *Rials* and *Marvadies*.

Note, 372 *Mervadies* make 1 *Rial.*

3 *Rials* - - - 1 *Piece of Eight.*

Q. *How do they keep their Accompts in Italy?*

A. In *Livres*, *Sols*, and *Deniers*.

Note, 12 *Deniers* make 1 *Sol.*

20 *Sols* - - - 1 *Livre.*

5 *Livres* - - - 1 *Piece of Eight at Genoa.*

6 *Livres* - - - 1 *Piece of Eight at Leghorn.*

E X A M P L E S.

1. What is the Amount of 63 *l.* *Sterling* in *Pieces of Eight*, at 56 *d.* per *Piece*? *Answ.* 270 *Pieces of Eight.*

2. A Factor hath sold Goods at *Cadiz* for 1468 *Pieces of Eight*, at 4*s.* 6*d.* 2*qrs.* per *Piece*; how much *Sterling* is the *Sum*? *Answ.* 333 *l.* 7*s.* 2*d.*

C A S E 2.

Q. What Place does London exchange with in Ducats ?
 A. With Venice in Italy.

Note, 6 Solidi make 1 Gros.

24 Grosses - - 1 Ducat.

E X A M P L E S.

1. There are 2000 Ducats, at 4s. 4d. each, remitted to London to be paid in Pounds Sterling ; what is the Amount ?
Answe. 433 l. 6s. 8d.

2. A Bill of 100 l. Sterling is remitted to Venice to be paid in Ducats, at 4s. 4d. each ; what is the Amount ? *Answe.* 461 $\frac{2}{3}$ $\frac{8}{3}$ Ducats.

3. A Traveller would exchange 233 l. 16s. 8d. Sterling for Venice Ducats, at 4s. 9d. per Ducat ; how many must he have ?
Answe. 984 $\frac{3}{7}$ $\frac{2}{7}$.

C A S E 3.

Q. What Place does London exchange with for French Crowns ?

A. With Paris, Lyons, Rouen, &c. in France.

Q. How do they keep their Accompts in France ?

A. In Livres, Sols, and Deniers.

Note, 12 Deniers make 1 Sol.

20 Sols - - - - 1 Livre.

3 Livres - - - 1 Crown.

E X A M P L E S.

1. A Bill of 200 l. is remitted to Paris by a Merchant in London ; what is the Value in French Crowns, at 4s. 6d. each ?
Answe. 888 $\frac{4}{5}$ $\frac{8}{5}$ Crowns.

2. There are 800 French Crowns, at 4s. 6d. each, remitted to London by a Merchant in Paris ; what is the Value in Pounds Sterling ? *Answe.* 180 l. Sterling.

C A S E 4.

Q. What Places does London exchange with for Mill-Reas ?

A. With Oporto and Lisbon, &c. in Portugal, and with the Island of Madeira.

Q. How do they keep their Accompts in Portugal ?

A. In Reas.

Note, 1000 Reas make 1 Mill-Rea.

E X A M P L E S.

1. If a Bill is drawn from Lisbon of 1432 Mill-Reas, at 6s. 8d. per Piece ; how much English Money is that Bill ? *Answe.* 477 l. 6s. 8d.

2. If a Bill be drawn from London of 1333 l. 6s. 8d. Sterling ; how much is it at Lisbon in Mill-Reas, at 6s. 8d. each ?
Answe. 4000 Mill-Reas.

C A S E

C A S E 5.

Q. What Place does London exchange with for Duccatoons ?
A. With Florence in Italy.

E X A M P L E S.

1. A Bill of 120 Duccatoons is remitted from Florence, at 53d. each ; what is the Value in Pounds Sterling ? *Answe.* 26*l.* 10*s.*

2. A Bill of 220*l.* 16*s.* 8*d.* is drawn from London ; what is the Value at Florence in Duccatoons, at 53*d.* each ? *Answe.* 1000 Duccatoons.

C A S E 6.

Q. What Place does London exchange with for Florins ?
A. With Frankfort in Germany.

E X A M P L E S.

1. If 247*l.* 18*s.* 4*d.* Sterling, be remitted to Frankfort, what is the Value in Florins, at 59*d.* $\frac{1}{2}$? *Answe.* 1000 Florins.

2. If 100 Florins, at 59*d.* $\frac{1}{2}$ each, be remitted from Frankfort to London ; what is the Value in Pounds Sterling ? *Answe.* 24*l.* 15*s.* 10*d.*

C A S E 7.

Q. What Place does London exchange with by the Pound Flemish or Pound Sterling ?

A. With Antwerp, Brussels, Amsterdam, Rotterdam, and all Parts of the Spanish and United Provinces. Also with Hamburg in Germany.

Q. How do they keep their Accompts in these Places ?

A. Some in Pounds, Shillings, and Pence, as in England ; and others in Guilders, Stivers, and Pennies.

Note, 16 Pennies make 1 Stiver.

20 Stivers - - - 1 Guilder. Also,

6 Stivers - - - 1 Shilling.

6 Guilders - - - 1 Pound Flemish.

E X A M P L E S.

1. Being desirous to remit to my Correspondent at London the Sum of 2000*l.* 12*s.* 6*d.* Flemish, to dispose of according to my Order ; Exchange at 34*s.* 6*d.* Flemish, per Pound Sterling ; how much Money Sterling shall I be Creditor for, in the City of London aforesaid ? *Answe.* 1159*l.* 15*s.* 7*d.* 3*qrs.* $\frac{126}{474}$.

2. My Correspondent in England gives me Notice, that he has disbursed in Merchandise upon my Account, the Sum of 1000*l.* Sterling ; what Sum must I answer for that in Holland, the Course of Exchange being at 33*s.* 4*d.* Flemish for one Pound Sterling ? *Answe.* 1666*l.* 13*s.* 4*d.* Flemish.

Note, When the Course of Exchange is at 33*s.* 4*d.* Flemish for 1 Pound Sterling, then to bring Flemish Money into English Money, multiply the Flemish Money by 3, and divide that Product by 5, the Quotient will give Pounds Sterling. And the Contrary.

3. My Correspondent in *Rotterdam* sends me Word, that he has disbursed upon my Account, the Sum of 3060 Guilders and 15 Stivers; what Sum must I answer for that at *London*, the Course of Exchange being at 37s. 9d. Flemish per Pound Sterling? *Answ.* 270*l.* 5*s.* 3*d.* 2*qrs.* $\frac{138}{453}$.

Note, A Stiver is 2d. Flemish, and a Guilder 40d.

4. A Merchant delivered at *London* 120*l.* Sterling, to receive 147*l.* Flemish, in *Amsterdam*; how much was 1*l.* valued at in Flemish Mony? *Answ.* 1*l.* 4*s.* 6*d.*

C A S E 8.

Of the Comparison of WEIGHTS and MEASURES.

E X A M P L E S.

1. If 112*lb.* at *London* make 99*lb.* at *Lisbon*; how many *lb.* at *London* are equal to 1049*lb.* at *Lisbon*? *Answ.* 1186*lb.* $\frac{74}{99}$.

2. If 112*lb.* at *London* make 98*lb.* at *Roan*; how many *lb.* at *Roan* are equal to 1000*lb.* at *London*? *Answ.* 875*lb.*

3. If 100 Ells *English* make 108 Braces at *Venice*; how many Ells *English* are equal to 1000 Braces at *Venice*? *Answ.* 925 Ells $\frac{100}{108}$.

4. If 100 Ells at *London* make 145 Ells at *Vienna*; how many Ells at *Vienna* are equal to 10 Ells at *London*? *Answ.* 14 Ells $\frac{1}{2}$.

Of ALLIGATION.

Q. HOW many kinds of Alligation are there?

A. Two: *Alligation Medial*, and *Alligation Alternate*.

Of ALLIGATION MEDIAL.

Q. What is Alligation Medial?

A. *Alligation Medial* is when the Quantities and Prices of several Things are given to find the mean Price of the Mixture compounded of those Things.

Q. What is the Rule?

A. As the whole Composition

Is to its Total Value:

So is any Part of the Composition

To its mean Price.

Q. How is Alligation Medial proved?

A. Find the Value of the whole Mixture at the mean Rate; and if it agrees with the Total Value of the several Quantities, at their respective Rates, the Work is right.

E X A M P L E S.

E X A M P L E S.

1. A Farmer mingled 19 Bushels of Wheat, at 6*s.* per Bushel, and 40 Bushels of Rye, at 4*s.* per Bushel, and 12 Bushels of Barly, at 3*s.* per Bushel together; I demand what a Bushel of this Mixture is worth? *Ans.* 4*s.* 4*d.* 1*qr.* $\frac{4}{7}\frac{1}{2}$.
2. A Farmer mingled 20 Bushels of Oats, at 2*s.* per Bushel, and 30 Bushels of Beans, at 2*s.* per Bushel, and 20 Bushels of Peas, at 3*s.* per Bushel together; I demand the Worth of a Bushel of this Mixture? *Ans.* 2*s.* 3*d.* 1*qr.* $\frac{5}{7}$.
3. A Vintner mingled 5 Gallons of Canary, at 8*s.* per Gallon, and 6 Gallons of Malaga, at 7*s.* per Gallon, and 4 Gallons of white Wine, at 6*s.* per Gallon together; I demand what a Gallon of this Mixture is worth? *Ans.* 7*s.* 0*d.* 3*qr.* $\frac{1}{2}$.
4. A Grocer mingled 2*C.* of Sugar, at 56*s.* per *C.* and 1*C.* at 43*s.* per *C.* and 2*C.* at 50*s.* per *C.* together; I demand the Price of 3*C.* of this Mixture? *Ans.* 7*l.* 13*s.*
5. An Alehouse-keeper mixed 3 sorts of Ale together, *viz.* 12 Gallons at 6*d.* per Gallon, 16 Gallons at 7*d.* per Gallon, and 21 Gallons at 9*d.* per Gallon; I demand what 1 Gallon of this Mixture is worth? *Ans.* 7*d.* 2*qr.* $\frac{2}{4}\frac{2}{9}$.
6. A Refiner having 5*lb.* of Silver Bullion of 8*oz.* fine, 10*lb.* of 7*oz.* fine, and 15*lb.* of 6*oz.* fine, would melt all together; I demand what Fineness 1*lb.* of this Mass shall be? *Ans.* 6*oz.* 13*dwts.* 8*gr.* fine.
7. A Mint-master hath 3*lb.* weight of Gold of 22 Carrats fine, and 3*lb.* of 20 Carrats fine; I demand what Fineness an *oz.* of this Mixture will bear? *Ans.* 21 Carrats fine.
8. An Hostler mixing Provender for his Horses, would put in a Quantity of Beans, at 5*s.* per Bushel, with the like Quantity of Oats at 3*s.* 6*d.* per Bushel; I demand the Price of a Bushel of this Mixture? *Ans.* 4*s.* 3*d.*
9. A Maltster hath severall sorts of Malt, *viz.* one sort at 4*s.* 6*d.* another at 4*s.* and a third at 3*s.* 6*d.* per Bushel, and he would mix an equal Quantity of each together; I demand the Price of a Bushel of this Mixture? *Ans.* 4*s.*
10. A Brewer hath severall sorts of Ale, *viz.* one sort of 20*s.* per Barrel; another at 25*s.* a third at 30*s.* and a fourth at 35*s.* per Barrel; and he would mix an equal Quantity of each together; I demand the Price of a Barrel, and also of a Gallon of this Mixture? *Ans.* 27*s.* 6*d.* per Barrel; and 10*d.* 1*qr.* $\frac{8}{3}\frac{1}{2}$ per Gallon.

Of ALLIGATION ALTERNATE.

Q. What is Alligation Alternate?

A. Alligation Alternate is, when the Rates of several Things are given to find such Quantities of them, as are necessary to make a Mixture, which may bear a certain Rate propounded.

Q. How are the Rates, or Prices of the given Things to be ordered?

A. 1. They must be placed one over the other, and the propounded Price of the Composition against them; thus,

2. Link the several Rates together, in such sort, that one greater than the *mean Rate* may be coupled to another which is *less*.

3. Take the *Differences* between the *mean Rate*, and the several *Prices*, and place them each against his Yoke-Fellow: And for the rest, observe the following Cases.

C A S E I.

Q. When the Prices of the several Things together with the mean Rate of the Mixture are given, without any Quantity, to find how much of each Ingredient is required to compose the Mixture; how must the Operation be wrought?

A. Take the *Differences* between each *Price*, and the *mean Rate*, and set them Alternately, and they will be the Quantities required.

Q. How are the Operations in this and the following Cases proved?

A. They are all proved by *Alligation Medial*.

E X A M P L E S.

1. How much Rye at 4*s.* per Bushel, Barly at 3*s.* per Bushel, and Oats at 2*s.* per Bushel, will make a Mixture worth 2*s.* 6*d.* per Bushel? Answ. 6 Bushels of Rye, 6 Bushels of Barly, and 24 Bushels of Oats.

2. How many Raifins of the Sun, at 7*d.* per lb. and Malaga-Raifins, at 4*d.* per lb. may be mixed together, for 6*d.* per lb? Answ. 2 lb. of Raifins of the Sun, and 1 lb. of Malaga-Raifins.

Note, Questions in this Rule do frequently admit of an infinite variety of Answers, and all in whole Numbers; as in this last Example; where tho' 2 and 1 do answer the Question, yet any other two Numbers will as truly do the like, that are in the same Proportion.

For 2 : 1 :: $\left\{ \begin{array}{l} 4 : 2 \\ 6 : 3 \\ 8 : 4 \\ 16 : 8 \\ 40 : 20, \text{ &c. without end.} \end{array} \right.$

3. A Grocer would mix three sorts of Sugar together, *viz.* one sort at 10*d.* per *lb.* another at 7*d.* and another at 6*d.* how much of each sort must he take, that the whole Mixture may be sold for 8*d.* per *lb.*?

	lb.	d. per lb.
<i>Answ.</i>	3 at 10	
	2 at 7	
	2 at 6	

4. A Maltster hath several sorts of Malt, *viz.* one sort at 4*s.* per Bushel, another at 3*s.* 6*d.* a third at 3*s.* and a fourth at 2*s.* per Bushel; and he is desirous to mix so much of each sort together, that the Whole may be sold at 2*s.* 6*d.* per Bushel; I demand how much he must take of each sort?

	Bush.	s.	d. per Bush.
<i>Answ.</i>	6 at 4	0	
	6 at 3	6	
	6 at 3	0	
	36 at 2	0	

5. A Druggist hath several sorts of Tea, *viz.* one sort at 12*s.* per *lb.* another at 11*s.* a third at 9*s.* and a fourth at 8*s.* per *lb.* I demand how much of each sort he must mix together, that the whole Quantity may be afforded at 10*s.* per *lb.*?

	lb.	s. p. lb.	lb.	s. p. lb.	lb.	s. p. lb.
1 <i>Answ.</i>	2 at 12		2 <i>Answ.</i>	3 at 12	3 <i>Answ.</i>	1 at 12
	1 at 11			2 at 11		2 at 11
	1 at 9			2 at 9		2 at 9
	2 at 8			3 at 8		1 at 8

	lb.	s. p. lb.	lb.	s. p. lb.	lb.	s. p. lb.
4 <i>Answ.</i>	1 at 12		5 <i>Answ.</i>	3 at 12	6 <i>Answ.</i>	2 at 12
	3 at 11			1 at 11		3 at 11
	3 at 9			3 at 9		1 at 9
	1 at 8			2 at 8		3 at 8

7 *Answ.* 3 *lb.* of each Sort.

Note, These Seven Answers arise from as many different Ways of linking the Rates of the Simples together.

6. How much Alloy must I mix with Bullion of 10 *oz.* fine to abase the same to 8 *oz.* fine? *Answ.* To every 8 *oz.* of Bullion of 10 *oz.* fine, put 2 *oz.* of Alloy, and that will abase it to 8 *oz.* fine.

C A S E 2.

Of Alternation Partial.

Q. When the Rates of all the Things, the Quantity of but one of them, and the mean Rate of the whole Mixture are given to find the several Quantities of the rest, in Proportion to the Quantity given; how are these Quantities found?

A. Take the Differences between each Price and the mean Rate, and place them alternately; as in Case 1. Then say, As the Difference of the same Name with the Quantity given Is the rest of the Differences severally: So is the Quantity given To the several Quantities required.

E X A M P L E S.

1. A Man being determined to mix 10 Bushels of Wheat at 4s. per Bushel, with Rye at 3s. with Barly at 2s. and with Oats at 1s. per Bushel; I demand how much Rye, Barly, and Oats, must be mixed with the 10 Bushels of Wheat, that the Whole may be sold for 28d. per Bushel?

	B.	p.	B.
1 Answ.	{ 2	2 of Rye	{ 40 of Rye
	{ 5	0 of Barly	{ 50 of Barly
	{ 12	2 of Oats	{ 20 of Oats
	B.		B.
3 Answ.	{ 8	of Rye	{ 10 of Rye
	{ 10	of Barly	{ 14 of Barly
	{ 14	of Oats	{ 14 of Oats
	B.	p.	B.
5 Answ.	{ 12	2 of Rye	{ 2 of Rye
	{ 5	0 of Barly	{ 14 of Barly
	{ 17	2 of Oats	{ 10 of Oats
	B.		B.
7 Answ.	{ 50	of Rye	{ 50 of Rye
	{ 70	of Barly	{ 70 of Barly
	{ 20	of Oats	{ 20 of Oats

2. A Man being determin'd to mix 12 Bushels of Oats, at 18d. per Bushel, with Barly at 2s. 6d. with Rye at 3s. and with Wheat at 4s. per Bushel; I demand how much Barly, Rye, and Wheat, must be mixed with the 12 Bushels of Oats, that it may bear the Price of 22d. per Bushel? Answ. 1 Bushel of each sort.

3. A Man

3. A Man being determined to mix 12 Bushels of Oats, at 18 d. per Bushel, with Barly at 2 s. 6 d. with Rye at 3 s. and with Wheat at 4 s. per Bushel; I demand how much Barly, Rye, and Wheat, must be mixed with the 12 Bushels of Oats, that the Whole may bear the Price of 2 s. 9 d. per Bushel?

1 Answ. $\left\{ \begin{array}{l} B. \\ 60 \text{ of Barly} \\ 60 \text{ of Rye} \\ 12 \text{ of Wheat} \end{array} \right.$

2 Answ. $\left\{ \begin{array}{l} B. \\ p. \\ 2 \quad 1\frac{9}{15} \text{ of Barly} \\ 2 \quad 1\frac{9}{15} \text{ of Rye} \\ 12 \quad 0 \text{ of Wheat} \end{array} \right.$

3 Answ. $\left\{ \begin{array}{l} B. \\ 10 \text{ of Barly} \\ 10 \text{ of Rye} \\ 12 \text{ of Wheat} \end{array} \right.$

4 Answ. $\left\{ \begin{array}{l} B. \\ 72 \text{ of Barly} \\ 72 \text{ of Rye} \\ 12 \text{ of Wheat} \end{array} \right.$

5 Answ. $\left\{ \begin{array}{l} B. \\ 2 \text{ of Barly} \\ 12 \text{ of Rye} \\ 10 \text{ of Wheat} \end{array} \right.$

6 Answ. $\left\{ \begin{array}{l} B. \\ p. \\ 14 \quad 1\frac{9}{15} \text{ of Barly} \\ 2 \quad 1\frac{9}{15} \text{ of Rye} \\ 14 \quad 1\frac{9}{15} \text{ of Wheat} \end{array} \right.$

7 Answ. 12 Bushels of each sort.

4. A Man being determin'd to mix 12 Bushels of Oats at 18 d. per Bushel, with Barly at 2 s. 6 d. with Rye at 3 s. and with Wheat at 4 s. per Bushel; I demand how much Barly, Rye, and Wheat must be mixed with the 12 Bushels of Oats, that the whole Quantity may bear the Price of 3 s. 6 d. per Bushel?

Answ. $\left\{ \begin{array}{l} B. \\ 12 \text{ of Barly} \\ 12 \text{ of Rye} \\ 84 \text{ of Wheat} \end{array} \right.$

5. A Man intends to mix 28 Bushels of Oats at 18 d. per Bushel, with Barly at 2 s. 6 d. with Rye at 3 s. and with Wheat at 4 s. I would know how much Barly, Rye and Wheat, ought to be added to the 28 Bushels of Oats, that the whole Quantity may be afforded at 2 s. per Bushel? Answ. 4 Bushels of each sort.

6. A Farmer would mix 27 Bushels of Peas at 18 d. per Bushel, with Oats at 28 d. and with Beans at 30 d. per Bushel, that the whole Quantity may bear the Price of 20 d. per Bushel; I demand how much Oats and Beans must be mixed with the 27 Bushels of Peas? Answ. 3 Bushels of each sort.

CASE 3.
Of Alternation Total.

Q. When the Rates of the several Things, the Quantity to be compounded, and the mean Rate of the whole Mixture are given, to find how much of each sort will make up that Quantity; how are those Quantities discovered?

A. Place the Differences between the several Prices, and the mean Rate, alternately, as in Case 1. Then say,

As the Sum of the Differences

Is to the whole Composition:

So is the Difference of each Rate

To the Quantity of the same Rate.

E X A M P L E S.

1. A Grocer hath 4 sorts of Sugar, viz. at 8 d. per lb. at 6 d. per lb. at 4 d. per lb. and at 2 d. per lb. and he would have a Composition of an C.wt. worth 5 d. per lb. I demand how much of each sort he must take?

	lb.	d. p. lb.		lb.	d. p. lb.
1 Answ.	42	at 8	2 Answ.	14	at 8
	14	at 6		42	at 6
	14	at 4		42	at 4
	42	at 2		14	at 2
—			—		
112			112		

	lb.	oz.	dr.	d. p. lb.		lb.	oz.	dr.	d. p. lb.
3 Answ.	28	0	0	at 8	4 Answ.	37	5	5 $\frac{4}{12}$	at 8
	37	5	5 $\frac{4}{12}$	at 6		9	5	5 $\frac{4}{12}$	at 6
	9	5	5 $\frac{4}{12}$	at 4		37	5	5 $\frac{4}{12}$	at 4
	37	5	5 $\frac{4}{12}$	at 2		28	0	0	at 2
—					—				
112 0 0					112 0 0				

	lb.	oz.	dr.	d. p. lb.		lb.	d. p. lb.	
5 Answ.	11	3	3 $\frac{2}{10}$	at 8	6 Answ.	32	at 8	
	44	12	12 $\frac{8}{10}$	at 6		24	at 6	
	44	12	12 $\frac{8}{10}$	at 4		24	at 4	
	11	3	3 $\frac{2}{10}$	at 2		32	at 2	
—				—				
112 0 0				112				

7 Answ. 28 l. of each sort.

2. A

2. A Vintner hath 4 sorts of Wine, *viz.* Canary at 10 s. per Gallon, Malaga at 8 s. Rhenish at 6 s. and Oporto at 4 s. and he is minded to make a Composition of 60 Gallons, worth 9 s. per Gallon; I demand how much of each sort he must have?
Answ. 45 Gals. of Canary, and 5 Gals. of each other sort.

3. A Brewer hath 3 sorts of Ale, *viz.* at 10 d. at 8 d. and at 6 d. per Gallon; and he would have a Composition of 30 Gallons, worth 7 d. per Gallon; I demand how much of each sort he must have?

	Gals.	d. p. Gallon.
	5	at 10
	5	at 8
<i>Answ.</i>	20	at 6
		<u>30</u>

4. A Goldsmith hath several sorts of Gold, *viz.* some of 24 Carrats fine, some of 22 Carrats, and some of 18 Carrats fine; and he would have compounded of these sorts the Quantity of 60 oz. of 20 Carrats fine; I demand how much of each sort he must take?

	Oz.
	12 at 24 Carrats fine
	12 at 22 Carrats fine
<i>Answ.</i>	36 at 18 Carrats fine
	<u>60</u>

5. A Goldsmith hath Gold of three sorts, *viz.* of 22 Carrats, of 21 Carrats, and of 20 Carrats fine, and he would mix with these so much Alloy, as that the Quantity of 21 oz. may bear 18 Carrats fine; I demand how much of each sort he must take, and how much Alloy?
Answ. 6 oz. of each sort of Gold, and 3 oz. of Alloy.

6. A Druggist had three sorts of Drugs, one was worth 4 s. per lb. another 5 s. and another 8 s. and out of these he made two Parcels, one was 21 lb. at 6 s. per lb. and the other 35 lb. at 7 s. per lb. how much of every sort did he take for each Parcel?

	lb.	s. p. lb.	lb.	s. p. lb.
	6	at 4	5	at 4
	6	at 5	5	at 5
<i>Answ.</i>	9	at 8	25	at 8
	<u>21</u>	at 6 s. per lb.	<u>35</u>	at 7 s. per lb.

Of P O S I T I O N.

Q. **W**HAT is Position or Negative Arithmetic?

A. It discovers the Truth by supposed Numbers.

Q. How many kinds of Position are there?

A. Two: Single and Double.

Of S I N G L E P O S I T I O N.

Q. What is Single Position?

A. It discovers the Truth by only one supposed Number.

Q. How is that supposed Number used?

A. By working with it, as if it was the true Number, in the same Proportion as the Question directs; and if the Result be either too much, or too little, the true Number may be found out by the following Rule, *viz.*

As the Result of the Position

Is to the Position:

So is the given Number

To the Number required.

Q. How do you prove Position?

A. Position both Single and Double is proved by adding the several Sums required, or the several Parts of the Sum required together; and if that Sum agrees with the given Sum, it is right.

E X A M P L E S.

1. Two Men, *A* and *B*, having found a Bag of Money, disputed who should have it: *A* said the half, third, and fourth of the Money, made 130*l.* and if *B* could tell how much was in it, he should have it all, otherwise he should have nothing; I demand how much was in the Bag? *Answ.* 120*l.*

2. *A*, *B*, and *C*, determining to buy together a certain Quantity of Timber, worth 36*l.* agree that *B* shall pay $\frac{1}{3}$ more than *A*, and *C* $\frac{1}{4}$ more than *B*; I demand how much each Man must pay? *Answ.* *A* 9*l.* *B* 12*l.* *C* 15*l.*

3. A Person having about him a certain Number of Crowns, said, if the half, third, and fourth of them were added together, they would make 65 Crowns; I demand how many he had? *Answ.* 60 Crowns.

4. *A* lent *B* a Sum of Money, to be paid at 4 Payments; when 3 of them were made, and *A* came to demand the fourth, *B* would give him no more, except he would tell him how much was paid already; *A* said, the first Payment was a fourth; the second, a fifth; and the third, a sixth of the Sum first lent; and all together made 74*l.* I demand the Sum lent? *Answ.* 120*l.*

5. One

5. One Man carrying a Bag of Mony in his Hand, another asked him, How much was in it: he answered, He could not tell, but the third, fourth, and fifth of it made 94*l.* how much was in the Bag? *Answe.* 120*l.*

6. I have delivered to a Banker, a certain Sum of Mony, to receive of him after the Rate of 6*l.* per Cent. per Annum; and at the end of ten Years, he paid me 500*l.* for Principal and Interest together; I demand the Sum delivered to him at first? *Answe.* 312*l.* 10*s.*

Of DOUBLE POSITION.

Q. *What is Double Position?*

A. It is that which discovers the true Number sought, by making use of *two* supposed Numbers.

Q. *How are those supposed Numbers used?*

A. 1. By working with them as if they were the true Numbers, in the same Proportion as the Question directs. *Pos.* *Er.*

2. The *Results* or *Errors* must be placed against their *Positions*, or supposed Numbers; thus, *40* *28*
36 *19*

3. Multiply them *Cross-wise*.

4. If the *Errors* are *alike*; i. e. both greater, or both less than the given Number, take their *Difference* for a *Divisor*, and the *Difference* of the *Products* for a *Dividend*.

5. If the *Errors* are *unlike*, take their *Sum* for a *Divisor*, and the *Sum* of the *Products* for a *Dividend*; the *Quotient* thence arising will be the *Answer*.

E X A M P L E S.

1. *A, B, and C, would divide 100*l.* between them, so, as that B may have 3*l.* more than A, and C 4*l.* more than B; I demand how much each Man must have?* *Answe.* *A 30*l.* B 33*l.* C 37*l.**

2. A Man lying at the Point of Death, said, He had in a certain Coffer 100*l.* which he bequeathed to 3 of his Friends, after this Manner; The first must have a certain Portion; the second must have twice as much as the first, wanting 8*l.* and the third must have three times as much as the first, wanting 15*l.* I demand how much must each Man have? *Answe.* *The First 20*l.* 10*s.* Second 33*l.* Third 46*l.* 10*s.**

3. *A, B, and C, built an House, which cost 100*l.* of which A paid a certain Sum; B paid 10*l.* more than A; and C paid as much as A and B; I demand each Man's Share in that Charge?* *Answe.* *A paid 20*l.* B 30*l.* C 50*l.**

4. Three

4. Three Persons discoursed together concerning their Ages ; says *A*, I am 20 Years of Age ; says *B*, I am as old as *A*, and half *C* ; and says *C*, I am as old as you both : I demand the Age of each Person ? *Answ.* *A* was 20, *B* 60, *C* 80 Years of Age.

5. A Man lying at the Point of Death, left to his 3 Sons, all his Estate in Money, *viz.* to *F* half, wanting 50*l.* to *G* one third ; and to *H* the rest, which was 10*l.* less than the Share of *G* ; I demand the Sum left, and each Man's Part ? *Answ.* The Sum left was 360*l.* whereof *F* had 130*l.* *G* 120*l.* *H* 110*l.*

6. A certain Man having drove his Swine to the Market, *viz.* Hogs, Sows, and Pigs ; received for them all 50*l.* being paid for every Hog 18*s.* for every Sow 16*s.* for every Pig 3*s.* there were as many Hogs as Sows, and for every Sow there were three Pigs ; I demand how many there were of each sort ? *Answ.* 25 Hogs ; 25 Sows ; 75 Pigs.

7. A surly old Fellow being demanded the Ages of his four Children, answer'd, You may go and look : But if you must needs know ; my first Son was born just 1 Year after I was married to his Mother, who, after his Birth, lived 5 Years, and then died in Child-Bed with my second Son : 4 Years after that I married again, and within 2 Years had my third and fourth Sons at a Birth ; the Sum of whose two Ages is now equal to that of the Eldest : I demand their several Ages ? *Answ.* The first Son was 22 Years old, the second 17, the third 11, and the fourth 11 Years old.

Of COMPARATIVE ARITHMETIC.

Q. **W**HAT is Comparative Arithmetic ?

A. It is such, as Answers Questions by Numbers, having Relation one to another.

Q. Wherein does this Relation consist ?

A. It consists either in Quantity or Quality.

Q. What is Relation of Numbers in Quantity ?

A. It is the Respect that one Number has to another.

Q. How many are the Numbers propounded ?

A. They are always two, the Antecedent and the Consequent.

Q. In what does Relation of Numbers in Quantity consist ?

A. It consists in the Difference, or else in the Rate or Reason that is found between the Terms propounded.

Note. The Difference of any two Numbers is the Remainder ; but the Rate or Reason is the Quotient of the Antecedent divided by the Consequent.

Q. What

Q. What is Relation of Numbers in Quality or Progression?

A. Progression or Proportion is the Respect that the Reason of Numbers have one to another.

Q. How many must the Terms be?

A. Three or more; but never less: Because less than three will not admit of a Comparison of Reasons or Differences.

Of P R O G R E S S I O N.

Q. How many kinds of Progression are there?

A. Two: Arithmetical and Geometrical.

Of A R I T H M E T I C A L P R O G R E S S I O N.

Q. What is Arithmetical Progression?

A. Arithmetical Progression is when several Numbers have equal Differences; as 1, 2, 3, 4, differ by 1; or 2, 4, 6, 8, differ by 2.

Note, 1, If any Number of Terms, differ by Arithmetical Progression, the Sum of the two Extreams will be equal to the Sum of any two Means equally distant from the Extreams. As in 2, 4, 6, 8; where $2 + 8$ are $= 4 + 6 = 10$, and so of any larger Number of Terms.

2. If the Number of Terms be odd, the middlemost supplies the Place of two Terms. As in 1, 2, 3; where $1 + 3$ are $= 2 + 2 = 4$.

C A S E I.

Q. When the two Extreams, and the Number of Terms in any Series of Numbers in Arithmetical Progression are given, and the Sum of all the Terms is required; how is that Sum found?

A. Multiply the Sum of the two Extreams by half the Number of Terms: Or,

Multiply half the Sum of the Extreams by the whole Number of Terms, the Product is the Total of all the Terms.

E X A M P L E S.

1. How many Strokes does the Hammer of a Clock strike in 12 Hours? *Answ. 78.*

2. A Merchant hath sold 100 Yards of superfine Cloth, *viz.* the first Yard for 1*s.* the second for 2*s.* the third for 3*s.* &c. I demand how much he received for the said Cloth? *Answ. 252*l.* 10*s.**

3. Bought 19 Yards of Shalloon, and gave 1*d.* for the first Yard, 3*d.* for the second, 5*d.* for the third, &c. increasing 2*d.* every Yard; I demand what I gave for the 19 Yards? *Answ. 1*l.* 10*s.* 1*d.**

4. A Mercer sold 20 Yards of Silk, at 3*d.* for the first Yard, 6*d.* for the second, 9*d.* for the third, &c. increasing 3*d.* every Yard; I demand what he sold the 20 Yards for? *Answ. 2*l.* 12*s.* 6*d.**

5. A Butcher bought 100 Head of Cattle, *viz.* Oxen, and gave for the first Ox 1 Crown, for the second Ox 2 Crowns, for the third Ox 3 Crowns, &c. I demand what the Cattle cost him? *Answ. 1262*l.* 10*s.**

6. Admit

6. Admit 100 Stones were laid 2 Yards distant from each other in a right Line, and a Basket placed 2 Yards from the first Stone ; I demand how many Miles a Man shall go in gathering them singly into the Basket ? *Ans. 11 Miles, 3 Furlongs, 180 Yards ?*

7. A Merchant sold 1000 Yards of Linen at 2 Pins for the first Yard, 4 for the second, 6 for the third, &c. increasing 2 Pins for every Yard; I demand how much the Linen produced, when the Pins were afterwards sold at 12 for a Farthing? Also, whether the said Merchant gained or lost by the Sale thereof, and how much, supposing the said Linen to have been bought at 6 d. per Yard?

Ans. { The Linen produced 86*l.* 17*s.* 10*d.*
The Merchant gained 61 17 10

CASE 2.

Q. When the two Extreams, and the Number of Terms in any Series of Numbers in Arithmetical Progression are given, and the common Difference of all the Terms in that Series are required; how is that Difference found?

A. Divide the *Difference* between the two *Extreams*, by the Number of *Terms*, less one; the *Quotient* will be the *common Difference*.

EXAMPLES.

1. There are 21 Men, whose Ages are equally distant from each other in Arithmetical Progression ; the Youngest is 20 Years old, and the Eldest is 60 ; I demand the common Difference of their Ages, and the Age of each Man ? *Answ.* The common Difference is 2 Years ; therefore

Years.

60 is the Age of the first Man.

$$60 - 2 = 58 \text{ is the Age of the Second.}$$

$$58 - 2 = 56 \text{ is the Age of the Third.}$$

$$56 - 2 = 54 \text{ is the Age of the fourth, \&c.}$$

2. A Debt is to be discharged at 16 several Payments in Arithmetical Proportion; the first Payment is to be 14*l.* the last 100*l.* what is the whole Debt, and what must each Payment be? *Answ.* The whole Debt is 912*l.* The common Difference is, 5*l.* 14*s.* 8*d.* therefore

14 <i>l.</i>			os.			od.			1st Payment	
14	0	0	5	14	8	19	14	8	2	d
19	14	8	5	14	8	25	9	4	3	d
25	9	4	5	14	8	31	4	0	4	th, &c.

3. A Map

3. A Man is to travel from *York* to a certain Place in 12 Days, and to go but three Miles the first Day, increasing every Day's Journey by an equal Excess, so that the last Day's Journey may be 36 Miles ; what will each Day's Journey be, and how many Miles is the Place, he goes to, distant from *York*? *Answ.* The common Difference is 3 ; therefore

Miles.

3 is the first Day's Journey.

3 + 3 = 6 is the Second.

6 + 3 = 9 is the Third.

9 + 3 = 12 is the Fourth, &c.

The whole Distance is 234 Miles.

4. A running Footman, on a Wager, is to travel from *London* Northward, as follows ; that is to say, he is to go 4 Miles the first Day, and 40 Miles the last Day ; and to go the whole Journey in 10 Days, increasing every Day's Journey by an equal Excess ; I demand the number of Miles he travelled each Day, and the length of the whole Journey ? *Answ.* The common Difference is 4 ; therefore

Miles.

4 is the first Day's Journey.

4 + 4 = 8 is the Second.

8 + 4 = 12 is the Third, &c.

The whole Journey is 220 Miles.

Of GEOMETRICAL PROGRESSION.

Q. What is Geometrical Progression ?

A. When any Rank or Series of Numbers increases by one common Multiplier, or decreases by one common Divisor, those Numbers are continued in Geometrical Progression ; as, 3, 6, 12, 24, increase by the Multiplier 2 ; and 24, 12, 6, 3, decrease by the Divisor 2.

Note, 1. If any Number of Terms be continued in Geometrical Progression, the Product of the two Extreams will be equal to the Product of any two Means equally distant from the Extreams ; as in 3, 6, 12, 24 ; where 3×24 , are = 6×12 = 72 ; and so of any larger Number of Terms.

2. If the Number of Terms be odd, the middlemost supplies the Place of two Terms ; as in 3, 6, 12 ; where 3×12 are = 6×6 = 36.

3. The common Multiplier, and the common Divisor, are called Ratios.

Q. How

Q. How is the Sum of any Series in Geometrical Progression obtained?

A. 1. When all the Terms alone are given; then from the Product of the second and last Terms, subtract the Square of the first Term; that Remainder being divided by the second Term, less the first, will give the Sum of all the Terms.

2. When the two Extreams and the Ratio are only given; then multiply the last Term into the Ratio, and from that Product subtract the first Term; that Remainder divide by the Ratio, less an Unit or 1, the Quotient is the Sum of all the Terms.

Note, 1. As the last Term in a long Series of Numbers is very tedious to come at by continual Multiplication; it would be necessary for the readier finding it out, to have a Series of Numbers in Arithmetical Proportion, called Indices, beginning with an Unit, whose common Difference is One: Also whatever Number of Indices you make choice of, let as many Numbers (in such Geometrical Proportion as is given in the Question) be placed under them.

Thus, $\left\{ \begin{array}{l} 1, 2, 3, 4, 5, 6, 7, \text{ Indices} \\ 2, 4, 8, 16, 32, 64, 128 \text{ Numbers in Geometrical Proportion.} \end{array} \right.$

2. But if the first Term in Geometrical Proportion be different from the Ratio, the Indices must begin with a Cypher.

Thus, $\left\{ \begin{array}{l} 0, 1, 2, 3, 4, 5, 6 \text{ Indices} \\ 1, 2, 4, 8, 16, 36, 64 \text{ Numbers in Geometrical Proportion.} \end{array} \right.$

3. When the Indices begin with a Cypher, the Sum of the Indices made choice of, must always be one less than the Number of Terms given in the Question; because 1 in the Indices stands over the second Term, and 2 in the Indices stands over the third Term, &c.

4. Add any two of these Indices together, and that Sum will directly correspond with the Product of their respective Terms.

5. By the Help of these Indices, and a few of the first Terms in any Series of Geometrical Proportion, any Term whose Distance from the first Term is assigned, tho' it be never so far, may speedily be obtain'd, without producing all the Terms.

E X A M P L E S.

1. A Man bought an Horse, and by Agreement was to give a Farthing for the first Nail, two for the Second, four for the Third, &c. there were 4 Shoes, and 8 Nails in each Shoe: I demand what the Horse was worth at that Rate? Answ. 4473924 l. 5 s. 3 d. 3 qrs.

2. A Merchant sold 15 Yards of Sattin, the first Yard for 1s. the second for 2 s. the third for 4 s. the fourth for 8 s. I demand the Price of the 15 Yards? Answ. 1638 l. 7 s.

3. A Draper sold 20 Yards of superfine Cloth, the first Yard for 3 d. the Second for 9 d. the Third for 27 d. &c. in triple Proportion Geometrical; I demand the Price of the Cloth? Answ. 21792402 l. 10 s.

4. A Gold-

4. A Goldsmith sold 1 lb. of Gold, at a Farthing for the first Ounce, a Penny for the Second, 4d. for the Third, &c. in quadruple Proportion Geometrical; I demand what he sold the Whole for; also how much he gained by the Sale thereof, supposing he gave for it 4*l.* per Ounce?

Ans. { He sold it for 5825*l.* 8*s.* 5*d.* 1*qr.*
And gained 5777 8 5 1

5. A crafty Servant agreed with a Farmer (ignorant in Numbers) to serve him 12 Years, and to have nothing for his Service but the Produce of a Wheat-Corn for the first Year; and that Product to be sowed for the second Year; and so on from Year to Year, until the End of the said Time; I demand the Worth of the whole Produce; supposing the Increase to be but in a tenfold Proportion, and sold out at 4*s.* per Bushel? *Ans.* 452112*l.* 4*s.* rejecting Remainders.

Note 1. 7680 Wheat or Barly-Corns are supposed to make a Pint, and 64 Pints a Bushel.

2. If the first Term in any Series, be either greater or less than the Ratio, (except Unity) then multiply any two Terms together, and their Product divide by the first Term; that Quotient will exactly correspond with the Sum of their Indices, as in the following

E X A M P L E S.

6. A Thresher worked 20 Days at a Farmer's, and received for the first Day's Work, 4 Barly-Corns; for the second, 12 Barly-Corns; for the third, 36 Barly-Corns; and so on in triple Proportion Geometrical; I demand what the 20 Days Labour came to, supposing the whole Quantity to be sold for 2*s.* 6*d.* per Bushel? *Ans.* 1773*l.* 7*s.* 6*d.* rejecting Remainders.

7. A Merchant sold 30 Yards of fine Velvet, trimmed with Gold very curiously, at 2 Pins for the first Yard, 6 Pins for the second, 18 Pins for the third, &c. in triple Proportion Geometrical; I demand how much the Velvet produced, when the Pins were afterwards sold at 100 for a Farthing; also, whether the said Merchant gained or lost by the Sale thereof, and how much, supposing the said Velvet to have been bought at 50*l.* per Yard.

Ans. { The Velvet produced 2144699292*l.* 13*s.* 0*d.* $\frac{1}{2}$
The Merchant gained 2144697792 13 0 $\frac{1}{2}$

Of P E R M U T A T I O N.

Q. What is Permutation?

A. Changing the Order of Things.

Q. How do you find all the Variations, any Number of Things is capable of going through?

A. Multiply all the given Terms one into another continually; the last Product is the Number of Changes required.

E X A M P L E S.

1. I demand how many Changes may be rung upon twelve Bells ; and also how long they would be in ringing but once over, supposing 24 Changes might be rung in one Minute, and the Year to contain 365 Days, 6 Hours ? *Answ. The Number of Changes is 479001600, and the Time is 37 Years, 49 Weeks, 2 Days, 18 Hours.*

2. Seven Gentlemen that were travelling, met together by chance, at a certain Inn upon the Road, where they were so well pleased with their Host, and each others Company, that in a Frolic, they offer'd him 30l. to stay at that Place so long as they, together with him, could sit every Day at Dinner in a different Order : The Host thinking that they could not sit in many different Positions, because there were but a few of them, and that himself would make no considerable Alteration, he being but one ; imagin'd that he should make a good Bargain ; and readily (for the sake of a good Dinner and better Company) enter'd into an Agreement with them, and so made himself the eighth Person : I demand how long they staid at the said Inn, and how many different Positions they sat in ? *Answ. The Number of Positions were 40320 ; and the Time that they staid was 110 Years, and 142 Days ; allowing the Year to consist of 365 Days, 6 Hours.*

Note, There is one Thing in Progression, and in Varying the Order of Things, which is well worth our Observation ; and that is the Power of Numbers, which is surprisingly great, and beyond common belief ; and is no way conceivable by a common Practitioner, hardly by a very good Artist ; it being not so much against Reason as above it. The first Example in Geometrical Progression, discovers what a prodigious Sum of Money a Horse fold after that manner would produce, viz. no less than Four Millions four hundred seventy three thousand nine hundred and twenty-four Pounds ; whereas if the same Horse had been sold at the same Rate, and but a fourth Part of the Nails, he would have brought to his Owner no more than 5s. 3d. $\frac{3}{4}$. The second Example in changing the Order of Things, does likewise discover the Impossibility of the Innkeeper's performing his Promise ; and in both the Simplicity of two Men, who thinking they have got very good Bargains, do instead thereof, find themselves severe Sufferers. And altho' at the first Appearance, each Question seems to produce but a meer Trifle ; yet upon a mature Consideration, there would not be found a Man in the Kingdom, able to purchase the one, or long liv'd enough to stand to the Agreement with the other. Hence observe the great Possibility of a Man's being impos'd on in this way, by Sharpers, without a careful Examination into the Affair, before any Contract is made.

T H E



THE Schoolmasters Assistant.

PART II.

Of VULGAR FRACTIONS.

Of Fractions in general.

Q. *What is a Fraction?*

A. It is a broken Number ; and signifies the Part or Parts of a whole Number.

Q. *How many kinds of Fractions are there?*

A. Two : *Vulgar* and *Decimal*.

Of NOTATION of VULGAR FRACTIONS.

Q. *What is a Vulgar Fraction?*

A. Any two Numbers placed thus $\frac{1}{2}$, make a *Vulgar Fraction*.

Q. *What is the upper Number of a Fraction called?*

A. It is called *Numerator* ; and is the Remainder after Division.

Q. *What is the lower Number called?*

A. It is called *Denominator* ; and notes any Whole divided into Parts ; and is the Divisor in Division.

Q. *How many sorts of Vulgar Fractions are there?*

A. Three : *Proper*, *Improper*, and *Compound*.

Q. *What is a Proper Fraction?*

A. When the *Numerator* is less than the *Denominator*, as $\frac{1}{2}$.

Q. *How far may a proper Fraction be express'd?*

A. Without end ; as $\frac{1}{2}$ may be called $\frac{2}{4}$ or $\frac{3}{6}$ or $\frac{4}{8}$, &c. but the lowest Term $\frac{1}{2}$ is always desired.

Q. *What is an improper Fraction?*

A. When the *Numerator* is greater than the *Denominator*, as, $\frac{5}{2}$.

Q. *What is a compound Fraction?*

A. It is the Fraction of a Fraction ; as, $\frac{1}{2}$ of $\frac{2}{3}$, &c.

Of REDUCTION of VULGAR FRACTIONS.

CASE I.

Q. *How are Vulgar Fractions reduced to a common Denominator?*

A. 1. Multiply each *Numerator* into all the *Denominators* but its own, for a new *Numerator*.

2. Multiply all the *Denominators* for a *common Denominator*.

EXAMPLES.

1. Reduce $\frac{3}{8}$ and $\frac{5}{8}$ to a common Denominator. *Facit* $\frac{24}{48}$ and $\frac{30}{48}$.
2. Reduce $\frac{7}{5}$, $\frac{9}{10}$ and $\frac{11}{12}$ to a common Denominator.
Facit $\frac{840}{960}$, $\frac{864}{960}$ and $\frac{880}{960}$.
3. Reduce $\frac{6}{10}$, $\frac{4}{8}$, $\frac{5}{9}$ and $\frac{6}{7}$ to a common Denominator.
Facit $\frac{3024}{5040}$, $\frac{2520}{5040}$, $\frac{560}{5040}$ and $\frac{4320}{5040}$.
4. Reduce $\frac{4}{9}$, $\frac{7}{11}$, $\frac{7}{9}$ and $\frac{1}{2}$ to a common Denominator.
Facit $\frac{616}{1386}$, $\frac{882}{1386}$, $\frac{1188}{1386}$ and $\frac{693}{1386}$.
5. Reduce $\frac{6}{9}$, $\frac{2}{7}$, $\frac{1}{3}$ and $\frac{7}{8}$ to a common Denominator.
Facit $\frac{1008}{1512}$, $\frac{432}{1512}$, $\frac{504}{1512}$ and $\frac{1123}{1512}$.
6. Reduce $\frac{4}{5}$, $\frac{1}{2}$, $\frac{5}{6}$ and $\frac{2}{8}$ to a common Denominator.
Facit $\frac{384}{480}$, $\frac{240}{480}$, $\frac{400}{480}$ and $\frac{120}{480}$.

CASE 2.

Q. How do you reduce a Vulgar Fraction to its lowest Term?

A. 1. Find a common Measure by dividing the lower Term by the upper; and that Divisor by the Remainder following, till nothing remain: The last Divisor is the common Measure.

2. Divide both Parts of the Fraction by the common Measure, and the Quotient will make the Fraction required.

Note 1. If the common Measure happen to be 1, the given Fraction is already in its lowest Term.

2. When a Fraction hath Cyphers at the right Hand, it may be abbreviated, by cutting them off; thus, $\frac{7}{9}10$.

3. This Case will prove Case 1.

EXAMPLES.

1. Reduce $\frac{48}{56}$ to its lowest Term. *Facit* $\frac{6}{7}$.
2. Reduce $\frac{72}{94}$ to its lowest Term. *Facit* $\frac{36}{47}$.
3. Reduce $\frac{84}{170}$ to its lowest Term. *Facit* $\frac{42}{85}$.
4. Reduce $\frac{60}{125}$ to its lowest Term. *Facit* $\frac{12}{25}$.
5. Reduce $\frac{182}{196}$ to its lowest Term. *Facit* $\frac{13}{14}$.
6. Reduce $\frac{458}{184}$ to its lowest Term. *Facit* $\frac{117}{296}$.

CASE 3.

Q. How is a mixt Number reduced to an improper Fraction?

A. 1. Multiply the whole Number into the Denominator of the Fraction.

2. To the Product, add the Numerator for a new Numerator.

3. Let its Denominator, be the Denominator given.

Note. To express a whole Number Fraction-wise, put 1 for its Denominator.

EXAMPLES.

EXAMPLES.

1. Reduce $12\frac{15}{17}$ to an improper Fraction. *Facit* $\frac{219}{17}$.
2. Reduce $19\frac{12}{18}$ to an improper Fraction. *Facit* $\frac{354}{18}$.
3. Reduce $16\frac{18}{100}$ to an improper Fraction. *Facit* $\frac{1618}{100}$.
4. Reduce $12\frac{19}{36}$ to an improper Fraction. *Facit* $\frac{691}{36}$.
5. Reduce $100\frac{19}{59}$ to an improper Fraction. *Facit* $\frac{5919}{59}$.
6. Reduce $79\frac{12}{19}$ to an improper Fraction. *Facit* $\frac{1513}{19}$.

CASE 4.

Q. *How is an improper Fraction reduced to its proper Terms?*
 A. Divide the upper Term by the lower.

Note, This Case, and Case 3, prove each other.

EXAMPLES.

1. Reduce $12\frac{15}{17}$ to its proper Terms. *Facit* $12\frac{15}{17}$.
2. Reduce $8\frac{5}{17}$ to its proper Terms. *Facit* $8\frac{5}{17}$.
3. Reduce $2\frac{30}{48}$ to its proper Terms. *Facit* $2\frac{30}{48}$.
4. Reduce $56\frac{9}{17}$ to its proper Terms. *Facit* $56\frac{9}{17}$.
5. Reduce $1\frac{6}{7}$ to its proper Terms. *Facit* $1\frac{6}{7}$.
6. Reduce $3\frac{3}{7}$ to its proper Terms. *Facit* $3\frac{3}{7}$.

CASE 5.

Q. *How do you reduce a compound Fraction to a single one?*
 A. 1. Multiply all the Numerators for a new Numerator.
 2. Multiply all the Denominators for a new Denominator.

EXAMPLES.

1. Reduce $\frac{1}{2}$ of $\frac{2}{3}$ of $\frac{3}{4}$ to a single Fraction. *Facit* $\frac{5}{24}$.
2. Reduce $\frac{7}{8}$ of $\frac{4}{6}$ of $\frac{9}{10}$ to a single Fraction. *Facit* $\frac{252}{480}$.
3. Reduce $\frac{12}{14}$ of $\frac{5}{6}$ of $\frac{1}{2}$ to a single Fraction. *Facit* $\frac{60}{168}$.
4. Reduce $\frac{5}{9}$ of $\frac{4}{8}$ of $\frac{3}{4}$ to a single Fraction. *Facit* $\frac{60}{288}$.
5. Reduce $\frac{2}{3}$ of $\frac{3}{4}$ of $\frac{4}{5}$ to a single Fraction. *Facit* $\frac{24}{60}$.
6. Reduce $\frac{1}{2}$ of $\frac{8}{9}$ of $\frac{6}{7}$ to a single Fraction. *Facit* $\frac{48}{126}$.

CASE 6.

Q. *How do you reduce the Fraction of one Denomination to the Fraction of another, but greater, retaining the same Value.*

A. 1. Reduce the given Fraction to a compound Fraction, by comparing it with all the Denominations between it, and that Denomination, which you would reduce it to.

2. Reduce that compound Fraction to a single one, by Case 5.

E X A M P L E S.

1. Reduce $\frac{5}{6}$ of a Penny to the Fraction of a Pound. *Facit* $\frac{5}{1440} l.$
2. Reduce $\frac{1}{2}$ of a Farthing to the Fraction of a Shilling. *Facit* $\frac{1}{96} s.$
3. Reduce $\frac{8}{9}$ of an Ounce Troy, to the Fraction of a Pound. *Facit* $\frac{8}{108} lb.$
4. Reduce $\frac{6}{7}$ of a Pound Avoirdupois to the Fraction of a C.wt. *Facit* $\frac{6}{784} C.wt.$
5. Reduce $\frac{9}{13}$ of a Pint of Wine to the Fraction of a bbd. *Facit* $\frac{9}{6532} bbd.$

C A S E 7.

Q. How do you reduce the Fraction of one Denomination to the Fraction of another, but less, retaining the same Value.

A. Multiply the given Numerator, by the Parts of the Denominations between it, and that Denomination you would reduce the Fraction to, for a new Numerator, and place it over the given Denominator.

Note, This Case, and Case 6, prove each other.

E X A M P L E S.

1. Reduce $\frac{5}{1440}$ of a Pound to the Fraction of a Penny. *Facit* $\frac{1200}{1440} = \frac{5}{6} d.$
2. Reduce $\frac{1}{96}$ of a Shilling to the Fraction of a Farthing. *Facit* $\frac{1}{2} qr.$
3. Reduce $\frac{8}{108}$ of a lb. Troy to the Fraction of an Oz. *Facit* $\frac{8}{9} oz.$
4. Reduce $\frac{6}{784}$ of a C.wt. to the Fraction of a Pound. *Facit* $\frac{6}{7} lb.$
5. Reduce $\frac{9}{6532}$ of a bbd. of Wine to the Fraction of a Pint. *Facit* $\frac{9}{13} \text{ Pint.}$

C A S E 8.

Q. How do you reduce Vulgar Fractions from one Denomination to another of the same Value, having the Numerator of the required Fraction given?

*A. As the Numerator of the given Fraction
Is to its Denominator :
So is the Numerator of the intended Fraction
To its Denominator.*

E X A M P L E S.

1. Reduce $\frac{3}{4}$ to a Fraction of the same Value, whose Numerator shall be 15. *Facit* $\frac{15}{20} = \frac{3}{4}.$
2. Reduce $\frac{7}{8}$ to a Fraction of the same Value, whose Numerator shall be 42. *Facit* $\frac{42}{48}.$
3. Reduce $\frac{3}{4}$ to a Fraction of the same Value, whose Numerator shall be 34. *Facit* $\frac{34}{45} \frac{1}{3}.$
4. Reduce $\frac{5}{9}$ to a Fraction of the same Value, whose Numerator shall be 73. *Facit* $\frac{73}{83} \frac{2}{3}.$

Note, From Cases 8 and 9, there arises a new Fraction, which may not improperly be called a mixt Fraction.

C A S E

C A S E 9.

Q. How do you reduce Vulgar Fractions from one Denomination to another of the same Value, having the Denominator of the required Fraction, given?

A. As the Denominator of the given Fraction
Is to its Numerator:
So is the Denominator of the intended Fraction
To its Numerator.

Note, This Case, and Case 8, prove each other.

E X A M P L E S.

1. Reduce $\frac{3}{4}$ to a Fraction of the same Value, whose Denominator shall be 20. *Facit* $\frac{15}{20} = \frac{3}{4}$.
2. Reduce $\frac{7}{8}$ to a Fraction of the same Value, whose Denominator shall be 49. *Facit* $\frac{42}{49} = \frac{7}{8}$.
3. Reduce $\frac{3}{4}$ to a Fraction of the same Value, whose Denominator shall be 46. *Facit* $\frac{34}{46} = \frac{2}{4}$.
4. Reduce $\frac{5}{7}$ to a Fraction of the same Value, whose Denominator shall be $131\frac{2}{3}$. *Facit* $\frac{73}{133} = \frac{5}{7}$.

C A S E 10.

Q. How is a mixt Fraction reduc'd to a single one?

A. 1. When the Numerator is the integral Part; Then
(1.) Multiply it by the Denominator of the fractional Part, and to that Product add the Numerator of the fractional Part, for a new Numerator.
(2.) Multiply the Denominator of the Fraction by the Denominator of the fractional Part of the Numerator, for a new Denominator.

Note, This proves Case 9.

E X A M P L E S.

1. Reduce $4\frac{2}{9}$ to a simple Fraction. *Facit* $\frac{7}{9}$.
2. Reduce $3\frac{4}{5}$ to a simple Fraction. *Facit* $\frac{3}{4}$.
3. Reduce $2\frac{7}{9}$ to a simple Fraction. *Facit* $\frac{157}{387}$.

2. When the Denominator is the integral Part; Then
(1.) Multiply it by the Denominator of the fractional Part, and to that Product add the Numerator of the fractional Part, for a new Denominator.
(2.) Multiply the Numerator of the Fraction by the Denominator of the fractional Part, for a new Numerator.

Note, This proves Case 8.

E X A M P L E S.

1. Reduce $13\frac{2}{3}$ to a simple Fraction. *Facit* $\frac{163}{53}$ $= \frac{5}{3}$.
2. Reduce $4\frac{1}{3}$ to a simple Fraction. *Facit* $\frac{13}{3}$.
3. Reduce $1\frac{7}{12}$ to a simple Fraction. *Facit* $\frac{35}{96} = \frac{5}{14}$.

C A S E I I.

Q. How do you find the proper Quantity of a Fraction in the known Parts of an Integer.

A. Multiply the *Numerator* by the common Parts of the *Integer*, and divide by the *Denominator*.

E X A M P L E S.

1. Reduce $\frac{2}{3}$ of a Pound Sterling to its proper Quantity.
Facit 13s. 4d.
2. Reduce $\frac{18}{43}$ of a Shilling to its proper Quantity. Facit 5d. $\frac{1}{43}$.
3. Reduce $\frac{6}{7}$ of 5l. 9s. to its proper Quantity. Facit 4l. 13s. 5d. $\frac{1}{7}$.
4. Reduce $\frac{12}{16}$ of a lb. Troy to its proper Quantity. Facit 9oz.
5. Reduce $\frac{12}{78}$ of a Tun Weight to its proper Quantity.
Facit 3C. 0qrs. 8lb. 9oz. 13dr. $\frac{42}{78}$.
6. Reduce $\frac{5}{8}$ of a lb. Avoirdupois to its proper Quantity.
Facit 8oz. 14dr. $\frac{2}{9}$.
7. Reduce $\frac{9}{11}$ of 10C. 1qr. 12lb. to its proper Quantity.
Facit 8C. 1qr. 25lb. 1oz. 7dr. $\frac{3}{11}$.
8. Reduce $\frac{4}{7}$ of a Mile to its proper Quantity. Facit 4fur. 125yds. 2feet, 1in. 2bc. $\frac{1}{7}$.
9. Reduce $\frac{9}{10}$ of a Yard to its proper Quantity. Facit 2feet, 8in. 1bc. $\frac{2}{10}$.
10. Reduce $\frac{4}{3}$ of an Ell English to its proper Quantity.
Facit 1 Yard.
11. Reduce $\frac{7}{8}$ of an Acre to its proper Quantity. Facit 1 Rood, 30 Perches.
12. Reduce $\frac{4}{9}$ of a Tun of Wine to its proper Quantity.
Facit 1 bbd. 49galls.
13. Reduce $\frac{7}{8}$ of a Barrel of Beer to its proper Quantity.
Facit 31gall. $\frac{1}{2}$.
14. Reduce $\frac{3}{4}$ of a Chaldron of Coals to its proper Quantity.
Facit 13bush. $\frac{1}{2}$.
15. Reduce $\frac{2}{7}$ of a Quarter of Corn to its proper Quantity.
Facit 2bush. 1peck. $\frac{1}{7}$.
16. Reduce $\frac{7}{13}$ of a Day natural to its proper Quantity.
Facit 12hrs. 55min. 23sec. $\frac{1}{13}$.
17. Reduce $\frac{4}{3}$ of a Month to its proper Quantity. Facit 3wks. 1day, 9hrs. 36min.
18. What is the proper Quantity of $\frac{7}{8}$ of a Yard of Cloth?
Answ. 3qrs. 2na.
19. What is the proper Quantity of $\frac{2}{9}$ of a bbd. of Beer?
Answ. 12gall.
20. What is the proper Quantity of $\frac{3}{16}$ of a Barrel of Ale?
Answ. 6gall.

C A S E

C A S E 12.

Q. How do you reduce any given Quantity to the Fraction of any greater Denomination of the same Kind?

A. 1. Reduce the given Quantity to the lowest Term mentioned for a *Numerator*.

2. Reduce the *integral Part* to the same Term for a *Denominator*, and that will be the *Fraction* required.

Note 1. If there be a Fraction given with the said Quantity, let it be put to the Numerator of the Fraction required.

2. Cases, 11 and 12, prove each other.

E X A M P L E S.

1. Reduce 13 s. 4 d. to the Fraction of a Pound Sterling.

Facit $\frac{160}{240} = \frac{2}{3} l.$

2. Reduce 5 d. $\frac{1}{43}$ to the Fraction of a Shilling. Facit $\frac{1}{43} s$

3. What part of 5 l. 9 s. is 4 l. 13 s. 5 d. $\frac{1}{7}$? Answ. $\frac{6}{7}$.

4. Reduce 9 oz. Troy to the Fraction of a lb. Facit $\frac{9}{16} = \frac{3}{4} lb.$

5. Reduce 3 C. 0 qr. 8 lb. 9 oz. 13 dr. $\frac{42}{78}$ to the Fraction of a Tun. Facit $\frac{12}{78} Tun.$

6. Reduce 8 oz. 14 dr. $\frac{2}{9}$ to the Fraction of a lb. Avoirdupois. Facit $\frac{5}{9} lb.$

7. What part of 10 C. 1 qr. 12 lb. is 8 C. 1 qr. 25 lb. 1 oz. 7 dr. $\frac{3}{11}$? Answ. $\frac{9}{11}$.

8. Reduce 4 fur. 125 yds. 2 feet, 1 in. 2 br. $\frac{1}{7}$ to the Fraction of a Mile. Facit $\frac{4}{7} Mile.$

9. Reduce 2 feet, 8 in. 1 br. $\frac{2}{10}$ to the Fraction of a Yard. Facit $\frac{9}{10} Yard.$

10. Reduce 1 Yard to the Fraction of an Ell. Facit $\frac{4}{5} Ell.$

11. Reduce 1 Rood 30 Poles to the Fraction of an Acre. Facit $\frac{7}{16} Acre.$

12. Reduce 1 bbd. 49 gall. of Wine to the Fraction of a Tun. Facit $\frac{5}{9} Tun.$

13. Reduce 31 gall. $\frac{1}{2}$ of Beer to the Fraction of a Barrel. Facit $\frac{7}{8} Barrel.$

14. Reduce 13 bush. $\frac{1}{2}$ of Coals to the Fraction of a Chaldrone. Facit $\frac{3}{8} Chaldrone.$

15. Reduce 2 bush. 1 peck $\frac{1}{7}$ of Corn to the Fraction of a Quarter. Facit $\frac{2}{7} Quarter.$

16. Reduce 12 hrs. 55 min. 23 sec. $\frac{1}{13}$ to the Fraction of a Day natural. Facit $\frac{7}{13} Day.$

17. Reduce 3 w. 1 d. 9 h. 36 m. to the Fraction of a Month. Facit $\frac{4}{3} Month.$

18. Reduce 3 qrs. 2 na. to the Fraction of a Yard. Facit $\frac{7}{8} Yard.$

19. Reduce

19. Reduce 12 Gallons of Beer to the Fraction of a Hogshead.
 Facit $\frac{1}{16}$ bbd.

20. Reduce 6 Gallons of Ale to the Fraction of a Barrel.
 Facit $\frac{3}{16}$ Barrel.

21. Reduce 13 hrs. 30 min. to the Fraction of a Day.
 Facit $\frac{810}{1440} = \frac{9}{16}$.

Of ADDITION of VULGAR FRACTIONS.

Q. How are Vulgar Fractions added together?

A. 1. Reduce the given Fractions to a common Denominator.
 2. Add all the Numerators together for a new Numerator; under which subscribe the common Denominator.

Note, This Rule is proved by Subtraction, when two Fractions only are given.

E X A M P L E S.

1. Add $\frac{1}{2}$ and $\frac{7}{8}$ together. - - - - - Facit $1\frac{6}{8}$.

2. Add $\frac{7}{10}$ and $\frac{11}{12}$ and $\frac{4}{9}$ together. - - - - - Facit $2\frac{66}{1080}$.

3. Add 19 and $7\frac{1}{2}$ of $\frac{2}{3}$ together. - - - - - Facit $26\frac{2}{6}$.

4. Add $\frac{1}{2}$ of $\frac{7}{8}$ and $\frac{2}{3}$ of $\frac{19}{20}$ together. - - - - - Facit $1\frac{68}{960}$.

5. Add $\frac{1}{3}$ of 95 and $\frac{7}{8}$ of 14 together. - - - - - Facit $43\frac{22}{24}$.

6. Add $\frac{2}{3}$ and $17\frac{1}{2}$ together. - - - - - Facit $18\frac{1}{6}$.

7. Add $12\frac{1}{2}$ and $3\frac{2}{3}$ and $4\frac{3}{4}$ together. - - - - - Facit $20\frac{22}{24}$.

8. Add $6\frac{7}{8}$ of $\frac{9}{10}$ and $\frac{4}{7}$ of $\frac{1}{2}$ and $7\frac{1}{2}$ together. Facit $14\frac{1284}{2240}$.

Note, In order to find the following Facits, the Fractions given must be reduced to their proper Quantities by Case 11, in Reduction, and then added, as in Addition of whole Numbers.

9. Add $\frac{7}{8}$ of a Pound to $\frac{3}{4}$ of a Shilling. Facit 18s. 3d.

10. Add $\frac{3}{4}$ of a Penny to $\frac{1}{2}$ of a Pound. Facit 2s. 3d. 1qr. $\frac{5}{9}$.

11. Add $\frac{1}{2}$ of a lb. Troy to $\frac{1}{2}$ of an Oz. Facit 6oz. 11dwt. 16gr.

12. Add $\frac{4}{7}$ of a Tun to $\frac{9}{10}$ of an C.wt. Facit 12C. 1qr. 8lb. 12oz. 12dr. $\frac{8}{10}$.

13. Add $\frac{3}{4}$ of a Mile to $\frac{7}{10}$ of a Furlong. Facit 6 Fur. 28 Poles.

14. Add $\frac{1}{2}$ of a Yard to $\frac{2}{3}$ of a Foot. Facit 2 feet, 2 in.

15. Add $\frac{1}{3}$ of a Day to $\frac{1}{2}$ of an Hour. Facit 8 hrs. 30 min.

16. Add $\frac{4}{9}$ of a Chaldron to $\frac{7}{8}$ of a Bush. Facit 16 bush. 3 pecks $\frac{1}{2}$.

17. Add $\frac{1}{3}$ of a Week, $\frac{1}{4}$ of a Day, and $\frac{1}{2}$ of an Hour together. Facit 2 days 14 hrs. $\frac{1}{2}$.

18. Add $\frac{2}{3}$ of a Yard, $\frac{3}{4}$ of a Foot, and $\frac{7}{8}$ of a Mile together. Facit 1540 yds. 2f. 9in.

Of SUBTRACTION of VULGAR FRACTIONS.

Q. How are Vulgar Fractions subtracted?

A. 1. Reduce the given Fractions to a common Denominator.
 2. Subtract the lesser Numerator from the greater, and place it over the common Denominator.

3. When

3. When the lower *Fraction* is greater than the upper, subtract the *Numerator* of the lower *Fraction* from the *Denominator*, and to that *Difference* add the upper *Numerator*, carrying one to the *Units Place* of the lower whole Number.

Note, This Rule is proved by Addition.

E X A M P L E S.

1. From $\frac{11}{12}$ take $\frac{3}{4}$. - - - Facit $\frac{108}{448}$.
2. From $\frac{97}{100}$ take $\frac{3}{7}$. - - - Facit $\frac{379}{700}$.
3. From $96\frac{1}{3}$ take $14\frac{3}{7}$. - - - Facit $81\frac{19}{21}$.
4. From 96 take $\frac{3}{5}$. - - - Facit $95\frac{2}{5}$.
5. From $\frac{1}{3}$ of 76 take $\frac{3}{4}$ of 21. Facit $9\frac{1}{2}$.
6. From $\frac{109}{110}$ take $\frac{1}{2}$ of $\frac{2}{3}$ of $\frac{3}{4}$. Facit $\frac{1956}{2640}$.
7. From $71\frac{1}{2}$ take $\frac{17}{12}$. - - - Facit $70\frac{23}{38}$.
8. From $14\frac{1}{4}$ take $\frac{2}{3}$ of 19. - Facit $1\frac{7}{12}$.

Note, In order to find the following Facits, the Fractions given must be reduced to their proper Quantities by Case 11, in Reduction, and then subtracted, as in Subtraction of whole Numbers.

9. From $\frac{1}{2}$ of a Pound take $\frac{3}{4}$ of a Shilling. Facit 9s. 3d.
10. From $\frac{1}{2}$ of a Shilling take $\frac{3}{4}$ of a Penny. Facit 5d. $\frac{1}{4}$.
11. From $\frac{3}{5}$ of an oz. take $\frac{1}{8}$ of a dwt. Facit 11 dwt. 3 gr.
12. From $\frac{1}{2}$ of an C.wt. take $\frac{7}{12}$ of a Pound. Facit 1 qr. 27 lb. 6 oz. 10 dr. $\frac{8}{12}$.
13. From $\frac{2}{3}$ of a League take $\frac{7}{10}$ of a Mile. Facit 1 mile, 2 fur. 16 poles.
14. From 1 Ell take $\frac{7}{10}$ of a qr. Facit 1 yd. 0 qr. 1 na. $\frac{2}{10}$.
15. From $\frac{3}{2}$ of a bbd. of Beer take 1 Gallon. Facit 12 gall. $\frac{1}{2}$.
16. From $\frac{1}{8}$ of a Chaldrone take $\frac{2}{3}$ of a Bushel. Facit 17 bush 1 peck $\frac{1}{3}$.
17. From 7 Weeks take 9 Days $\frac{7}{10}$. Facit 5 wks. 4 days, 7 hrs. 12 min.
18. From 4 days 7 hrs. $\frac{1}{2}$ take 1 day 9 hrs. $\frac{3}{10}$. Facit 2 days 22 hrs. $\frac{1}{3}$.

Of MULTIPLICATION of VULGAR FRACTIONS.

Q. How are Vulgar Fractions multiplied?

A. 1. Prepare the given Numbers (if need be) by the Rules of Reduction.

2. Multiply all the given Numerators for a new Numerator and all the Denominators for a new Denominator.

Note, When any Number, either whole or mixt, is multiplied by a Fraction; the Product is always less than the Multiplicand, in the same Proportion as the multiplying Fraction is less than 1 or an Unit.

E X A M P L E S.

E X A M P L E S.

1. Multiply $\frac{3}{7}$ by $\frac{3}{15}$. - - - - - Facit $\frac{9}{75}$.
2. Multiply $\frac{4}{8}$ by $\frac{2}{5}$. - - - - - Facit $\frac{8}{20}$.
3. Multiply $\frac{1}{3}$ of $\frac{4}{5}$ by $\frac{7}{10}$ of $\frac{11}{12}$. Facit $\frac{308}{1800}$.
4. Multiply $7\frac{1}{4}$ by $8\frac{1}{2}$. - - - - - Facit $61\frac{5}{8}$.
5. Multiply $4\frac{1}{2}$ by $\frac{1}{8}$. - - - - - Facit $\frac{9}{16}$.
6. Multiply $\frac{2}{3}$ by $13\frac{9}{10}$. - - - - - Facit $12\frac{13}{80}$.
7. Multiply $\frac{1}{2}$ of 7 by $\frac{3}{8}$. - - - - - Facit $1\frac{9}{16}$.
8. Multiply $\frac{2}{3}$ of 8 by $\frac{7}{8}$ of 5. - - - - - Facit 21.
9. Multiply $\frac{3}{5}$ by $\frac{4}{9}$ of 11. - - - - - Facit $2\frac{24}{45}$.
10. Multiply $\frac{4}{5}$ of 91 by $71\frac{1}{2}$. - - - - - Facit $5205\frac{2}{5}$.
11. Multiply $12\frac{3}{5}$ by $\frac{2}{5}$ of 7. - - - - - Facit $29\frac{12}{25}$.
12. Multiply $7\frac{1}{2}$ by $9\frac{1}{4}$. - - - - - Facit $69\frac{3}{8}$.

Of DIVISION of VULGAR FRACTIONS.

Q. How are Vulgar Fractions divided?

A. 1. Prepare the Numbers given (if need be) by the Rules of Reduction.

2. Multiply the Denominator of the Divisor into the Numerator of the Dividend, for a new Numerator; and the Numerator of the Divisor into the Denominator of the Dividend, for a new Denominator.

Note 1. When the Dividend is greater than the Divisor, the Quotient will be greater than the Dividend: But when the Dividend is less than the Divisor, then the Quotient will be less than the Dividend, and in the same Proportion as an Unit is greater or less than the dividing Fraction.

2. Multiplication and Division prove each other.

E X A M P L E S.

1. Divide $\frac{17}{25}$ by $\frac{3}{5}$. - - - - - Facit $1\frac{22}{63}$.
2. Divide $\frac{13}{19}$ by $\frac{7}{9}$. - - - - - Facit $\frac{117}{133}$.
3. Divide $\frac{14}{18}$ by $\frac{7}{10}$. - - - - - Facit $1\frac{14}{126}$.
4. Divide $1\frac{1}{2}$ by $4\frac{8}{15}$. - - - - - Facit $\frac{30}{95}$.
5. Divide $\frac{7}{8}$ by 4. - - - - - Facit $\frac{7}{32}$.
6. Divide 4 by $\frac{7}{8}$. - - - - - Facit $4\frac{4}{7}$.
7. Divide 99 by 108. - - - - - Facit $\frac{99}{108}$.
8. Divide $\frac{1}{2}$ of 19 by $\frac{2}{3}$ of $\frac{3}{4}$. - - - - - Facit $7\frac{18}{30}$.
9. Divide $\frac{1}{2}$ of $\frac{2}{3}$ by $\frac{2}{3}$ of $\frac{3}{4}$. - - - - - Facit $\frac{24}{36}$.
10. Divide $\frac{2}{3}$ of $\frac{3}{4}$ by $\frac{1}{2}$ of $\frac{2}{3}$. - - - - - Facit $1\frac{12}{24}$.
11. Divide $4\frac{5}{9}$ by $\frac{5}{9}$ of 4. - - - - - Facit $2\frac{1}{20}$.
12. Divide $\frac{5}{9}$ of 4 by $4\frac{5}{9}$. - - - - - Facit $\frac{20}{45}$.

Of the SINGLE RULE of THREE DIRECT
in VULGAR FRACTIONS.

Q. How is the Rule of Three in Fractions perform'd?

A. The Operations of the Rule of Three in Fractions, both Single and Double, Vulgar and Decimal, are exactly agreeable to the Principles laid down in the same Rules in whole Numbers.

Q. How are the following Examples proved?

A. By changing the Order of them.

E X A M P L E S.

1. If $\frac{11}{13}$ lb. of Sugar cost $\frac{7}{5}$ of a Shilling, what cost $\frac{32}{43}$ lb.?

Answ. $\frac{2912}{7095}$ s. = 4 d. 3 qrs. $\frac{4971}{7095}$.

2. If $\frac{2}{3}$ Ell cost $\frac{2}{3}$ £, what cost $\frac{12}{17}$ Ell? Answ. 15 s. 8 d. $\frac{36}{153}$.

3. If $\frac{4}{7}$ Ell cost $\frac{7}{3}$ £, what cost 1 Ell? Answ. 18 s. 10 d. $\frac{8}{52}$.

4. If 2 oz. of Silver cost 16 s. 5 d. what cost $\frac{3}{4}$ oz.? Answ. 6 s. 1 d. 3 qrs. $\frac{1}{2}$.

5. If 6 Yards $\frac{1}{2}$ cost 18 s. what cost 9 Yards $\frac{1}{4}$? Answ.

1 l. 5 s. 7 d. 1 qr. $\frac{28}{52}$.

6. If 1 Dollar be worth 56 d. $\frac{3}{5}$, what is 500 Dollars worth?

Answ. 117 l. 8 s. 4 d.

7. If 1 Ell cost 9 s. what cost 16 yds. $\frac{1}{4}$? Answ. 5 l. 17 s.

8. If 1 Pistole be 17 s. $\frac{1}{3}$, what is 100 Pistoles? Answ. 86 l.

9. If $\frac{5}{7}$ oz. cost $\frac{11}{12}$ l. what cost 1 oz.? Answ. 1 l. 5 s. 8 d.

10. If an Ingot of Siver weighs 16 oz. $\frac{41}{13}$, what is it worth at 5 s. 6 d. per oz? Answ. 4 l. 12 s. 0 d. 1 qr. $\frac{9}{15}$.

11. If $\frac{9}{10}$ C. cost 14 l. 4 s. what will 7 C. $\frac{1}{2}$ cost? Answ. 118 l. 6 s. 8 d.

12. If $\frac{2}{3}$ of an Ell cost $\frac{2}{3}$ of 19 s. what cost 7 Ells? Answ. 7 l. 7 s. 9 d. 1 qr. $\frac{3}{2}$.

13. If 8 lb. of Tobacco cost 4 s. 9 d. $\frac{3}{5}$, what cost 1 lb?

Answ. 7 d. $\frac{4}{5}$.

14. If 1 yd. of broad Cloth cost 15 s. $\frac{5}{8}$, what will 4 Pieces, each containing 27 yds. $\frac{3}{8}$ cost? Answ. 85 l. 10 s. 11 d. $\frac{1}{4}$.

15. A Mercer bought 3 Pieces $\frac{1}{2}$ of Silk, each containing 24 Yards $\frac{1}{3}$ at 6 s. 0 d. $\frac{1}{2}$ per Yard; I demand the Value of the 3 Pieces $\frac{1}{2}$, at that Rate? Answ. 25 l. 14 s. 6 d. 2 qrs. $\frac{4}{12}$.

16. If $\frac{1}{3}$ lb. leis by $\frac{1}{6}$ cost 13 d. $\frac{1}{3}$, what cost 14 lb. leis by $\frac{1}{5}$ of 2 lb.? Answ. 4 l. 9 s. 9 d. $\frac{3}{25}$.

17. A Merchant had 5 C. $\frac{8}{9}$ of Sugar, at 6 d. $\frac{3}{4}$ per lb. which he would barter for Tea at 8 s. $\frac{5}{8}$ per lb. I demand how much Tea must be given for the Sugar? Answ. 43 lb. $\frac{6}{414}$.

18. Bought 120 lb. of Tea, at 8 s. $\frac{5}{8}$ per lb. and sold it for 70 l. what was the Gain per Cent.? Answ. 35 l. 5 s. 3 d. 3 qrs. $\frac{25}{1633}$.

Of

*Of the SINGLE RULE of THREE INVERSE
in VULGAR FRACTIONS.*

1. If $3\frac{1}{4}$ Yards of Cloth that is $1\frac{1}{3}$ Yard wide, be sufficient to make a Cloke; how much must I have of that sort, which is $\frac{3}{4}$ Yard wide to make a Cloke of the same Bigness? *Answ.* $4\frac{7}{8}$ Yds.
2. If 16 Men finish a Piece of Work in $28\frac{1}{3}$ Days; how long will 12 Men require to do the same Work? *Answ.* $37\frac{2}{3}$ Days.
3. If $1\frac{1}{4}$ Yard in Breadth require $20\frac{1}{2}$ Yards long to make a Garment; what Length will $\frac{3}{4}$ Yard wide require to make the same? *Answ.* $136\frac{1}{2}$ Yards.
4. How many Pieces of Merchandise, at $20\frac{1}{2}$ per Piece, are to be given for $240\frac{1}{7}$ Pieces, at $125\frac{1}{2}$ per Piece? *Answ.* $104\frac{17}{22}\frac{84}{54}$ Pieces.
5. How many Yards of Canvas that is $1\frac{1}{4}$ Yard wide, will be sufficient to line 20 Yards of Say, that is $\frac{3}{4}$ Yard wide? *Answ.* 12 yds. of Canvas.

Of the DOUBLE RULE of THREE in VULGAR FRACTIONS.

1. If 9 Students spend $10\frac{1}{2}$. $\frac{7}{3}$ in 18 Days; how much will 20 Students spend in 30 Days? *Answ.* $41\frac{1}{2}$. $15\frac{1}{2}$. $11\frac{1}{2}$ +
2. Three Men having work'd $19\frac{1}{2}$ Days, received $8\frac{1}{2}$. $\frac{9}{10}$; how much must 20 Men have for $100\frac{1}{4}$ Days? *Answ.* $305\frac{1}{2}$. $0\frac{1}{2}$. $8\frac{1}{2}$ +
3. A Man and his Wife having laboured 1 Day, earned $4\frac{1}{2}$. $\frac{5}{8}$; I demand how much they must have for 10 Days $\frac{1}{2}$ when their two Sons help them? *Answ.* $4\frac{1}{2}$. $17\frac{1}{2}$. $1\frac{1}{2}$ $\frac{1}{2}$.
4. A Man with his Family, which in all were 5 Persons, did usually drink $7\frac{4}{5}$ Gallons of Beer in a Week; how much will be drank in 22 Weeks $\frac{1}{2}$, when 3 Persons more come into the Family? *Answ.* $40\frac{4}{33}$ gall.
5. Seven Men with their Wives, upon examining into their Expenses for 20 Weeks past, found that they had laid out $40\frac{1}{2}$. $\frac{4}{3}$; I demand in what time $20\frac{1}{2}$. $\frac{3}{7}$ may be spent by 46 Men in the like Proportion? *Answ.* $3\frac{1}{2}$ w. $1\frac{1}{2}$ d. $\frac{147\frac{84}{75}}{75\frac{84}{75}}$.
6. Three Sailors having been abroad $9\frac{1}{4}$ Months, received $40\frac{1}{2}$. $\frac{3}{5}$; I demand how much 100 Sailors must receive for 28 Months $\frac{3}{7}$ Service? *Answ.* $4118\frac{1}{2}$. $6\frac{1}{2}$. $0\frac{1}{2}$ +



THE

Schoolmasters Assistant.

PART III.

Of DECIMAL FRACTIONS.

Q.  *What do you understand by Decimals in general?*

A. Any Thing which is called *One*; as one *Foot*, one *Pound*, one *Shilling*, one *Year*, &c. is conceived in Imagination to be divided into *ten equal Parts*, and every one of those Parts into *ten other equal Parts*; and so on, by a *Decimal Division*, without end.

Q. *What is a Decimal Fraction?*

A. Any Number having a Point placed before it, thus *.641* is a *Decimal*.

Q. *How do you distinguish a whole Number from a Decimal Fraction?*

A. Any Number having a Point placed after it, thus *641.* is a *whole Number*.

Q. *What is a mixt Number?*

A. Any Quantity of Figures having a Point placed somewhere between them, thus *6.41*, is a *mixt Number*.

Note, The Decimal Point must never be omitted; because without it a Decimal cannot be distinguished from a whole or mixt Number.

Of NOTATION of DECIMALS.

Q. *How do Decimal Places increase?*

A. In the same manner as whole Numbers do; that is, by *Tens*: For every Place towards the left Hand is ten times greater than that which is next it towards the right Hand, as appears by the following *Table*.

Table;

T A B L E.

C. Thousands	X. Thousands	C. Thousands	Tens	Units	Tenth Parts	Hundredth Parts	Thousandth Parts	X. Thousandth Parts	C. Thousandth Parts
6	5	4	3	2	1.	2	3	4	5
									6

Q. May not Cyphers sometimes be annex'd to Decimals?

A. They may; but they alter not their Value: Thus .41 and .4100 are the same.

Q. May not Cyphers sometimes be prefix'd to Decimal Parts?

A. Yes; and then they decrease their Value, by removing them farther from the Point: Thus .0041 is less than .41

Of ADDITION and SUBTRACTION of DECIMALS.

Q. **H**OW are Decimals added or subtracted?

A. Place the Numbers according to their Value; and work as in *Addition* and *Subtraction* of whole Numbers.

Q. How are the Operations proved?

A. As in whole Numbers.

EXAMPLES in ADDITION.

Shillings.	Yds.	Galls.	£.
17.471	47.4	7004.16	71.001
1.191	19.71	712.712	120.07
1.8126	461.728	19.0174	31.121
3.6126	400.004	7.3126	13.4101
7.1281	7.1004	71.1851	76.04
18.8126	7.07	4.108	7.3

Miles.	lb.	Acres.	Ounces.
41.8102	86.18104	.61271	48.9108
140.037	3.14	.8712	1.8191
18.10	1.181	.012	3.1080
7.8141	7.7121	.87	.7012
16.4612	8.19817	.04	.0012
7.81	13.071	.4	.0018

EXAMPLES in SUBTRACTION.

Years.	Days.	Weeks.	Hours.
From 1081.761	712.10009	127.19	12.
Take 10.00012	7.121	121.	.12

Minutes.	Months.	Ells.	Tuns.
From 174.1	6100.	.172618	761.8109
Take 1.471	6.109	.0000148	18.9112

Of MULTIPLICATION of DECIMALS.

Q. HOW are Decimals multiplied?
A. As whole Numbers are.

Note 1. When Numbers are multiplied, make as many Decimal Places in the Product, as there are in the two Factors taken together.
2. If Decimal Places are wanting in the Product, supply them with Cyphers to the Decimal Point.
3. Observe the same Note here, which is given in Multiplication of Vulgar Fractions.

Q. How are the following Examples proved?
A. By inverting the Factors.

EXAMPLES.

E X A M P L E S.

1. Multiply .612 by 4.12	8. Multiply .00041 by .00017
2. Multiply 48. by .48	9. Multiply .0027 by 41.
3. Multiply 37.9 by 46.5	10. Multiply 410. by .0012
4. Multiply .121 by 17.2	11. Multiply .07 by .07
5. Multiply 1.81 by 71.	12. Multiply 1.007 by .41
6. Multiply 4.1 by 1.42	13. Multiply 4.001 by .004
7. Multiply .00071 by .121	14. Multiply .004 by .004

Of DIVISION of DECIMALS.

Q. **H**OW are Decimals divided?

A. As whole Numbers are.

Note 1. The Decimal Places of the Divisor and Quotient must always be equal to those in the Dividend.

2. If there be more Decimals in the Divisor than in the Dividend, annex as many Cyphers as you please to the Dividend, so as to be equal at least to the Divisor.

3. If Decimal Places are wanting in the Quotient, they must be supplied with Cyphers to the Decimal Point.

4. Observe the same Note here, which is given in Division of Vulgar Fractions.

Q. How are the following Examples to be proved?

A. By Multiplication.

E X A M P L E S.

1. Divide 19.4 by 37.5	7. Divide 9. by .7121
2. Divide 47121.1 by 47.	8. Divide 9. by .9
3. Divide 4.18 by .1812	9. Divide 14. by 47.31
4. Divide .76121 by 41.	10. Divide 1. by 863.
5. Divide .612812 by 7.21	11. Divide .012181 by .12
6. Divide .121819 by .721	12. Divide .0001212 by .018

Of REDUCTION of DECIMALS.

Q. **H**OW do you reduce a Vulgar Fraction to a Decimal?

A. Divide the upper Term by the lower.

Note, Both Terms are to be esteemed whole Numbers.

EXAMPLES.

E X A M P L E S.

1. Reduce $\frac{5}{26}$ to a Decimal. - - - *Facit* .1923076 +
2. Reduce $\frac{5}{28}$ to a Decimal. - - - *Facit* .1785714 +
3. Reduce $\frac{11}{14}$ of $\frac{10}{13}$ to a Decimal. *Facit* .6043956 +
4. Reduce 7 s. 6 d. to the Decimal of a Pound. *Facit* .375 l.
5. Reduce 10 s. 9 d. $\frac{1}{4}$ to the Decimal of a Pound. *Facit* .5385416 + l.
6. Reduce 24 Grains to the Decimal of a lb. Troy. *Facit* .0041666 + lb.
7. Reduce 14 Drams to the Decimal of a lb. Avoirdupois. *Facit* .0546875 lb.
8. Reduce 4 C. 2 qrs. to the Decimal of a Ton. *Facit* .225 Ton.
9. Reduce 14 C. to the Decimal of a Ton. *Facit* .7 Ton.
10. Reduce 174 Drams to the Decimal of an C. *Facit* .0060686 + C.
11. Reduce 4 Inches to the Decimal of a Yard. *Facit* .1111111 + Yard.
12. Reduce 76 Yards to the Decimal of a Mile. *Facit* .4318181 + Mile.
13. Reduce 1 Mile to the Decimal of a League. *Facit* .3333333 + League.
14. Reduce 3 qrs. 2 na; to the Decimal of a Yard. *Facit* .875 yd.
15. Reduce 4 Perches to the Decimal of an Acre. *Facit* .025 Acre.
16. Reduce 1 Pint to the Decimal of a Gallon. *Facit* .125 gall.
17. Reduce 1 Gallon of Wine to the Decimal of a bbd. *Facit* .015873 + bbd.
18. Reduce 7 Minutes to the Decimal of a Day. *Facit* .0048611 + Day.
19. Reduce 2 Days to the Decimal of a Week. *Facit* .2857142 + Week.
20. Reduce 72 Days to the Decimal of a Year. *Facit* .1972602 + Year.

C A S E 2.

Q. How do you find the proper Quantity of a Decimal Fraction in the known Parts of an Integer?

A. Multiply it by the common Parts of the Integer.

Q. How do you prove Questions in this Case?

A. By Case 1.

E X A M P L E S.

1. What is the proper Quantity of .76 of a Pound?
Ans. 15 s. 2 d. 1.6 qr.
2. What is the proper Quantity of .861 of a Cwt.?
Ans. 3 qrs. 12 lb. 6 oz. 14.592 dr.
3. What is the proper Quantity of .461 of a Shilling?
Ans. 5 d. 2.128 qrs.
4. What is the proper Quantity of .761 of a bbd. of Wine?
Ans. 47 gall. 3 qts. 1.544 pt.
5. What is the proper Quantity of .17 of a Tun of Wine?
Ans. 42 gall. 3.36 qts.
6. What is the proper Quantity of .761 of a Day?
Ans. 18 hrs. 15 min. 50.4 sec.
7. What is the proper Quantity of .7 of a lb. of Silver?
Ans. 8 oz. 8 dwts.
8. What is the proper Quantity of .71 of 4 oz. of Gold?
Ans. 2 oz. 16 dwts. 19.2 gr.
9. What is the proper Quantity of .67 of a League?
Ans. 2 miles, 0 fur. 3 poles, 1 yd. 0 feet, 3 in. 1.8 bc.
10. What is the proper Quantity of .712 of a Furlong?
Ans. 28 Poles, 2 yds. 1 foot, 11.04 in.
11. What is the proper Quantity of .07 of a Barrel of Ale?
Ans. 2 gall. 1.92 pt.
12. What is the proper Quantity of .4712 of an Ell English?
Ans. 2 qrs. 1.424 na.
13. What is the proper Quantity of .72 of a bbd. of Beer?
Ans. 38 gall. 3.52 qts.
14. What is the proper Quantity of .61 of a Tun of Wine?
Ans. 2 bbd. 27 gall. 2 qts. 1.76 pt.
15. What is the proper Quantity of .092 of 3 Acres, 2 Roods?
Ans. 1 Rood, 11.52 Poles.
16. What is the proper Quantity of .461 of a Chaldron of Coals?
Ans. 16 bush. 2.384 pecks.
17. What is the proper Quantity of .712 of 3 qrs. of Corn?
Ans. 17 bush. 2.816 qts.
18. What is the proper Quantity of .3 of a Year?
Ans. 109 Days 12 hrs.
19. What is the proper Quantity of .5 of an Hour?
Ans. 30 min.
20. A certain Tenant hired an House for 9 Years at 12.4 l. per Annum; how much was due at the End of the Term?
Ans. 111 l. 12 s.

Note, Addition and Subtraction of Decimals of different Denominations, may easily be perform'd, after the Decimals are reduced to their proper Quantities.

E X A M P L E S.

1. What is the Sum of .48*l.* and .16*s.* reduced to their proper Quantities? *Answe.* 9*s.* 9.12*d.*
2. What is the Sum of .17*lb.* Troy, and .84*oz.*? *Answe.* 2*oz.* 17*dwts.* 14.4*gr.*
3. What is the Sum of .17 Ton, .19*C.* .17*qr.* and .7*lb.*? *Answe.* 3*C.* 2*qrs.* 15.54*lb.*
4. What is the Difference between .17*l.* and .7*s.*? *Answe.* 2*s.* 8*d.* 1.6*qr.*
5. What is the Difference between .41 Day, and .16 Hour? *Answe.* 9*hrs.* 40*min.* 48*sec.*

Of the SINGLE RULE of THREE DIRECT
in DECIMALS.

Q. **H**OW do you prove the following Questions?

A. By changing their Order.

E X A M P L E S.

1. If 1.4*lb.* of Mace cost 14.5*s.* what cost 75.31*lb.*? *Answe.* 38*l.* 19*s.* 11*d.* 3.52*qrs.*
2. If 1.6*C.* of Sugar cost 3*l.* 12.76*s.* what cost 3*bbds.* each 11*C.* 3*qrs.* 10.12*lb.*? *Answe.* 80*l.* 15*s.* 3*d.* 3.36*qrs.*
3. If 1.5*oz.* of Silver be worth 7.8*s.* what is the Value of 9.7*lb.*? *Answe.* 30*l.* 5*s.* 3*d.* 1.44*qr.*
4. If 1.47*C.* of Sugar be worth 4.5*l.* what is 1.7*lb.* worth at that Rate? *Answe.* 11.1*d.*
5. If 1 Pint of Wine cost 1.2*s.* what cost 12.5*bbds.*? *Answe.* 378*l.*
6. If 8.4*lb.* of Tobacco cost 16*s.* 4.6*d.* what cost 3*bbds.* each 4*C.* 2*qrs.* 7.4*lb.*? *Answe.* 149*l.* 12*s.* 3*d.* 2*qrs.*
7. If 1 Yard of Cloth cost 12.3*s.* what cost 3 Pieces, each 21.5 Yards? *Answe.* 39*l.* 13*s.* 4.2*d.*
8. A Man bought a Piece of Cloth for 6*l.* 13.12*s.* I demand how many Yards there were in the same, when he gave after the Rate of 4*s.* 2.6*d.* per Yard? *Answe.* 31.569 Yards.
9. A Man bought 5.8 Tuns of Oil for 60.4*l.* but by Misfortune it chanced to leak out 50.9 Gallons; I demand how he must sell the rest per Gallon to be no loser? *Answe.* 10.27*d.* per Gallon.

10. Two Men bartered, *A* had 40.7 Yds. of Linen, for which *B* gave him 25.6 Ells of Holland, at 4.5 s. per Ell; I demand the Price of the Linen per Yard? *Answe.* 25. 9 d. 3.8 qrs.

11. A Grocer bought 7.6 C. of Sugar, at 40.1 s. per C. and sold the same out at 4.5 d. per lb. I demand whether he gained or lost, and how much? *Answe.* 14 s. 5 d. 1.12 qr. gain.

12. A Brewer made a Quantity of Beer which cost him 90.4 l. and afterwards sold it out at 26.7 s. per Barrel, by which he gain'd 10 l. I demand the Quantity that was brewed? *Answe.* 75 Bar. 7.4 + Gall.

13. A Grocer bought 3 C. 1.5 qr. of Cloves, at the Rate of 2.75 s. per lb. and sold them for 60 l. 11 s. 6 d. what did he gain or lose by the Bargain? *Answe.* he gain'd 8 l. 12 s.

14. A Merchant bought 436 Yards of Cloth for 8.5 s. per Yard, and sold it again for 10.75 s. per Yard; what did he gain by the Sale thereof? *Answe.* 49 l. 1 s. gain.

15. *A* owes *B* 296.85 l. but he compounds for 7.5 s. in the Pound; what must *B* receive for his Debt? *Answe.* 111 l. 6 s. 4 d. 2 qrs.

16. Bought 3 bbds. of Tobacco, each weighing 4 C. 1.9 qr. at 5.6 l. per C. which I sold out at 7 l. 16 s. per C. what did I gain by the Whole? *Answe.* 29 l. 10 s. 8 d. 1.6 qr.

17. A Jeweller bought a Diamond for 60 Guineas, which weighed 1.5 oz. and after it was neatly cut, he sold again for 3.25 s. per Grain; I demand how much he gain'd by the said Diamond; and also at what Rate per Cent. he made his Gain?

Answe. { Whole Gain - 54 l. 0 s. 0 d. 0 qr.
Gain per Cent. 85 14 3 1.7 +

Of CONVERGING SERIES;

• OR

Extracting the Roots of all POWERS.

A TABLE of POWERS.

Roots, or First Powers	1	2	3	4	5	6	7	8	9
Squares, or Second Powers	1	4	9	16	25	36	49	64	81
Cubes, or Third Powers	1	8	27	64	125	216	343	512	729
Biquadrats, or Fourth Powers	1	16	81	256	625	1296	2401	4096	6561
Sursolids, or Fifth Powers	1	31	243	1024	3125	7776	16807	32768	59049
Square-Cubes, or Sixth Powers	1	64	729	4096	15625	46656	117649	262144	531441
Second Sursolids, or Seventh Powers	1	128	2187	16384	78125	279936	823543	2097152	478296
Biquadrats squared, or Eighth Powers	1	256	6561	65536	390625	1679616	5764801	16777216	4304672
Cubes cubed, or Ninth Powers	1	512	19683	262144	1953125	10077696	40353607	134217728	38742048
Sursolids squared, or Tenth Powers	1	1024	59049	1048576	9765625	60466176	282475249	1073741824	348678441
Third Sursolids, or Eleventh Powers	1	2048	177147	4194304	48828125	362797056	1977326743	8589934592	313810592
Square-Cubes squared, or Twelfth Powers	1	4096	531441	16777216	244140625	2176782336	13841287201	68719476736	28242953441
Fourth Sursolids, or Thirteenth Powers	1	8192	1594323	67108864	1220703125	13060694016	96889010407	549755813888	2541865849
Second Sursolids squared, or Fourteenth Powers	1	16384	4782969	268435456	6103515625	78364164096	678223072849	4398046511104	228767924961
Sursolids cubed, or Fifteenth Powers	1	32768	14348907	1073741824	30517578125	470184984576	4747561509943	35184372088832	20589113209649

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Of the SQUARE-ROOT.

Q. **W**HAT is a Square?

A. Any Number multiplied by itself produces a *Square*.

Q. *What is the Extraction of the Square-Root?*

A. If a *Square* be given to find one Side, it is called the *Extraction of the Square-Root*.

Q. *How is the given Square to be prepared for Extraction?*

A. By pointing off at every two Figures, from the *Units Place*, both ways for a *Resolvend*.

Q. *What is a Surd?*

A. It is an imperfect *Square*, or such a Number, whose *Square-Root* can never be exactly found.

E X A M P L E S.

1. What is the Square of 17.1? - *Ans*w. 292.41

2. What is the Square of .09? - *Ans*w. .0081

3. What is the Square of .0094? *Ans*w. .00008836

4. What is the Square-Root of 4712.81261? - *Ans*w. 68.649+

5. What is the Square-Root of 9712.718051? - *Ans*w. 98.553+

6. What is the Square-Root of 3.1721812? - *Ans*w. 1.78106+

7. What is the Square-Root of 1.3976121? - *Ans*w. 1.1822+

8. What is the Square-Root of 761.801216? - *Ans*w. 27.6007+

9. What is the Square-Root of .0007612816? - *Ans*w. .02759+

10. What is the Square-Root of 4.000067121? - *Ans*w. 2.000016+

11. There is an Army consisting of a certain Number of Men, who are placed Rank and File, that is, in the Form of a *Square*, each Side having 472 Men; I demand how many Men the whole *Square* contains? *Ans*w. 222784 *Men*.

12. The Floor of a certain great Room is made exactly *Square*, each Side of which contains 75 Feet; I demand how many *Square Feet* are contained therein? *Ans*w. 5625 *Feet*.

13. Suppose 12544 Soldiers are to be put into Rank and File, in the Form of an equal *Square*; I demand how many Soldiers will be in the Front, and how many Deep? *Ans*w. 112.

14. A certain *Square Pavement* contains 197136 *Square Stones*, all of the same Size; I demand how many are contained in one of its Sides? *Ans*w. 444.

15. The

15. The Wall of a Town is 17 Feet high, which is surrounded by a Mote of 20 Feet in breadth; I demand the length of a Ladder which shall reach from the Outside of the Mote to the Top of the Wall? *Answ.* 26.2 + Feet.

Of the S Q U A R E - R O O T of a V U L G A R F R A C T I O N.

Q. How is the Square-Root of a Vulgar Fraction extracted?

A. 1. Reduce the Fraction to its lowest Term.
 2. Extract the Square-Root of the Numerator for a new Numerator, and the Square-Root of the Denominator for a new Denominator.
 3. If the Fraction be a Surd, reduce it to a Decimal, and then extract the Square-Root from it.
 4. The Decimal Fraction must consist of an even Number of Places; as two, four, &c.

E X A M P L E S.

1. What is the Square-Root of $\frac{3044}{6849}$? *Answ.* $\frac{2}{3}$.
 2. What is the Square-Root of $\frac{3455}{5400}$? *Answ.* $\frac{4}{5}$.
 3. What is the Square-Root of $\frac{7056}{9216}$? *Answ.* $\frac{7}{8}$.

S U R D S.

4. What is the Square-Root of $\frac{3168}{6192}$? *Answ.* .71528 +
 5. What is the Square-Root of $\frac{208}{272}$? *Answ.* .87447 +
 6. What is the Square-Root of $\frac{387}{735}$? *Answ.* .72414 +

Of the S Q U A R E - R O O T of a M I X T N U M B E R.

Q. How is the Square-Root of a mixt Number extracted?

A. 1. Reduce the fractional Part of the mixt Number to its lowest Term.
 2. Reduce the mixt Number to an improper Fraction.
 3. Extract the Roots of the Numerator and Denominator, for a new Numerator and Denominator.
 4. If the mixt Number given, be a Surd, reduce the fractional Part to a Decimal, and annex it to the whole Number, and extract the Square-Root from the Whole.

E X A M P L E S.

1. What is the Square-Root of $37\frac{36}{49}$? *Answ.* $6\frac{1}{7}$.
 2. What is the Square-Root of $17\frac{16}{25}$? *Answ.* $4\frac{1}{5}$.
 3. What is the Square-Root of $5\frac{288}{648}$? *Answ.* $2\frac{1}{3}$.

S U R D S.

4. What is the Square-Root of $76\frac{14}{25}$? *Answ.* 8.7649 +
 5. What is the Square-Root of $7\frac{9}{16}$? *Answ.* 2.7961 +

Of

Of the CUBE-ROOT.

Q. **W**HAT is a Cube?

A. Any Number multiplied by its *Square* produces a *Cube*.

Q. What is the Extraction of the Cube-Root?

A. If a *Cube* be given to find out a Number, which being multiplied into its *Square*, produceth the Number given; this is called the Extraction of the *Cube-Root*.

Q. How is the given Cube to be prepared for Extraction?

A. By pointing off at every three Figures, both ways, from the *Units Place*, for a *Resolvend*.

Q. What is a *Surd*?

A. An *imperfect Cube*, or such a Number, whose *Cube-Root* can never be exactly found.

Q. What is the Rule for extracting the Cube-Root of a Number?

A. This: The first Figure sought is the *Root* of the greatest *Cube* contained in the first Member, and it is called *a*; then $3aa + 3a$ is the *Divisor*, which finds a new Figure called *e*; then $3aae + 3ee + eee$ is the *Subtrahend* or Number to be subducted; which *Operation* is to be continued to every *Resolvend*.

Note, This Rule being somewhat dark, I shall, by way of Illustration, subjoin the Operation, at large, for extracting the Cube-Root of any Number.

What is the Cube-Root of 444194.947?

(1) Let the given Number be pointed as before directed; thus 444194.947

(2) The first Member, which contains the greatest Cube is 444; and the nearest Root, whose Cube is not greater than it, is 7, which set

thus 444194.947(7

(3) The Cube of 7 is 343, which set down and subtract, annexing the next three Figures or Member, viz. 194 for a *Resolvend*;

thus 444194.947(7

343
101194 Resolvend

(4) The Number 7, in the Root, is called a; then by the Rule, $3aa + 3a$ is the Divisor; thus,

$$\begin{array}{r}
 7 = a \\
 \underline{7 = a} \\
 49 = aa \\
 \underline{3} \\
 147 = 3aa \\
 \underline{21 = 3a} \\
 \text{Divisor } \underline{1491 = 3aa + 3a} \\
 \end{array}
 \quad
 \begin{array}{r}
 444194.947(7 \\
 \underline{343} \\
 101194 \text{ Resolvend}
 \end{array}$$

(5) The next Figure in the Root, viz. 6 (found by common Division) is called e; then by the Rule $3aae + 3eea + eee$, is the Subtrahend, or Number to be subduced; thus,

$$\begin{array}{r}
 147 = 3aa \\
 \underline{6 = e} \\
 882 = 3aae \\
 \underline{756 = 3eea} \\
 \underline{216 = eee} \\
 \text{Sub. } \underline{95976 = 3aae + 3eea + eee} \\
 \underline{756 = 3eea} \\
 \end{array}
 \quad
 \begin{array}{r}
 6 = e \quad \text{eee viz. } 6 = 216 \\
 \underline{6 = e} \\
 36 = ee \\
 \underline{3} \\
 108 = 3ee \\
 \underline{756 = 3eea} \\
 \end{array}
 \quad
 \begin{array}{r}
 444194.947(76. \\
 \underline{343} \\
 1491)101194 \text{ Resolvend} \\
 \underline{95976} \text{ Subtrahend} \\
 \underline{5218} \text{ 947 Resolvend}
 \end{array}$$

(6) When the next Member is brought down, viz. 947 as before, both Figures in the Root, viz. 76 must be called a; then to find a Divisor to this last Resolvend, say as before, $3aa + 3a$; thus,

$$\begin{array}{r}
 76 = a \quad 76 = a \\
 \underline{76 = a} \quad \underline{3} \\
 456 \quad 228 = 3a \quad 444194.947(76. \\
 \underline{532} \\
 5776 = aa \quad \underline{1491)101194} \text{ Resolvend} \\
 \underline{3} \\
 17328 = 3aa \quad \underline{95976} \text{ Subtrahend} \\
 \underline{228 = 3a} \\
 \text{Divisor } \underline{173508 = 3aa + 3a}
 \end{array}$$

(7) The next Figure in the Root, viz. 3, found as before, is also called e; then again 3aae + 3eea + eee is the other Subtrahend, or Number to be subducted; thus,

$$\begin{array}{rcl}
 17328 = 3aa & 3 = e & eee \text{ viz. } 3 = 27 \\
 \underline{3 = e} & \underline{3 = e} & \\
 51984 = 3aae & 9 = ee & \\
 2052 = 3eea & \underline{3} & \\
 27 = eee & 27 = 3ee & \\
 \hline
 \text{Sub. } 5218947 = 3aae + 3eea + eee & 76 = a & \\
 & \underline{162} & \\
 & \underline{189} & \\
 & 2052 = 3eea & \\
 444194.947 & (76.3 \text{ Answer}) & \\
 343 & & \\
 \hline
 1491)101194 \text{ Resolvend} & & \\
 95976 \text{ Subtrahend} & & \\
 173508)5218 \text{ 947 Resolvend} & & \\
 5218 \text{ 947 Subtrahend} & & \\
 \hline
 \end{array}$$

E X A M P L E S.

1. What is the Cube of 6.4? *Ans. 262.144*
2. What is the Cube of .13? *Ans. .002197*
3. What is the Cube of 41.1? *Ans. 69426.531*
4. What is the Cube of .09? *Ans. .000729*
5. What is the Cube of .007? *Ans. .000000343*
6. What is the Cube-Root of 7612.812161? *Ans. 19.67 +*
7. What is the Cube-Root of 7612181.7612? *Ans. 196.71 +*
8. What is the Cube-Root of 61218.00121? *Ans. 39.41 +*
9. What is the Cube-Root of 7121.1021698? *Ans. 19.238 +*
10. What is the Cube-Root of 12000.812161? *Ans. 22.89 +*
11. What is the Cube-Root of .121861281? *Ans. .495 +*
12. What is the Cube-Root of .0069761218? *Ans. .19107 +*
13. If a cubical Piece of Timber be 41 Inches long, 41 Inches broad, and 41 Inches deep; how many cubical Inches doth it contain? *Ans. 68921 Cubical Inches.*

14. Suppose a Cellar to be dug that shall be 12 Feet every way, in length, breadth, and depth; how many solid Feet of Earth must be taken out to compleat the same? *Answ.* 1728.

15. Suppose a Stone of a cubic Form to contain 474552 solid Inches; what is the superficial Content of one of its Sides? *Answ.* 6084 Inches.

Of the CUBE-ROOT of a VULGAR FRACTION.

Q. How do you extract the Cube-Root of a Vulgar Fraction?

- A.** 1. Reduce the Fraction to its lowest Term.
2. Extract the Cube-Roots of the Numerator and Denominator, for a new Numerator and Denominator.
3. If the Fraction be a Surd, reduce it to a Decimal, and then extract the Cube-Root from it.
4. The Decimal Fraction must consist of Ternaries of Places; as, three, six, nine, &c.

E X A M P L E S.

1. What is the Cube-Root of $\frac{352}{3168}$? *Answ.* $\frac{2}{3}$
2. What is the Cube-Root of $\frac{1944}{4608}$? *Answ.* $\frac{3}{4}$
3. What is the Cube-Root of $\frac{648}{3000}$? *Answ.* $\frac{3}{5}$

S U R D S.

4. What is the Cube-Root of $\frac{4}{9}$? *Answ.* .763 +
5. What is the Cube-Root of $\frac{6}{7}$? *Answ.* .949 +
6. What is the Cube-Root of $\frac{1}{3}$? *Answ.* .693 +

Of the CUBE-ROOT of a MIXT NUMBER.

Q. How do you extract the Cube-Root of a mixt Number?

- A.** 1. Reduce the Fractional Part to its lowest Term.
2. Reduce the mixt Number to an improper Fraction.
3. Extract the Cube-Roots of the Numerator and Denominator, for a new Numerator and Denominator.
4. If the mixt Number given be a Surd, reduce the fractional Part to a Decimal, and annex it to the whole Number, and extract the Cube-Root from the Whole.

E X A M P L E S.

1. What is the Cube-Root of $578\frac{19}{27}$? *Answ.* $8\frac{1}{3}$
2. What is the Cube-Root of $42\frac{21}{27}$? *Answ.* $3\frac{1}{2}$
3. What is the Cube-Root of $51\frac{94}{27}$? *Answ.* $1\frac{4}{3}$

S U R D S.

4. What is the Cube-Root of $8\frac{2}{27}$? *Answ.* 2.013 +
5. What is the Cube-Root of $7\frac{1}{3}$? *Answ.* 1.966 +

Of the BIQUADRATEROOT.

Q. **W**HAT is a Biquadrate Number?

A. Any Number involved four Times produces a Biquadrate.

Q. How is the Biquadrate Root extracted?

A. First extract the Square-Root of the given Resolvend; and then extract the Square-Root of that Square-Root, for the Biquadrate-Root required.

E X A M P L E S.

1. What is the Biquadrate of 48? Answ. 5308416.
2. What is the Biquadrate of 96? Answ. 84934656.
3. What is the Biquadrate-Root of 5308416? Answ. 48.
4. What is the Biquadrate-Root of 84934656? Answ. 96.
5. What is the Biquadrate-Root of 21743271936? - - - - - } Answ. 384.

Of the SURSOLID-ROOT.

Q. **W**HAT is a Sursolid?

A. Any Number involved five Times, produces a Sursolid.

Q. How is the Sursolid-Root, or the Root of any other bigger Power extracted?

A. By the following general Rules.

1. If any even Power be given, let the Square-Root of it be extracted, which reduces it to half of the given Power; then the Square-Root of that Power reduces it to half of the same Power; and so on till you come to a Square or a Cube.

For Example: Suppose a 24th Power be given; the Square-Root of that reduces it to a 12th Power; the Square-Root of the 12th Power reduces it to a 6th Power; and the Square-Root of the 6th Power to a Cube.

2. If any odd Power be given as the 17th, &c. observe

(1) From the Unity Place, both ways, point off at every such Number of Figures as is the Index of the Power for a Resolvend.

(2) Seek in the Table of Powers, for such a Power (being the same Power with the Index) as comes nearest the first Period, whether greater or less, calling its Root accordingly more than just, or less than just.

(3) Annex so many Cyphers to the Root, as there are Periods of whole Numbers remaining in the given Resolvend.

(4) Find the Difference between the given Resolvend, and the Power coming nearest the first Period.

(5) Whatever odd *Power* is given, the next lowest odd *Power* to that of the said *Root* must be found with its annexed *Cyphers*; i. e. if the 9th *Power* be given, find the 7th *Power* of the *Root* and *Cyphers*; if the 11th *Power* be given, find the 9th, &c.

(6) Multiply that next lowest odd *Power* by the *Index* of the given *Power*, and let that Product be a *Divisor* to the *Difference* between the given *Resolvend* and *Power* first found, which depresses it to a *Square*.

(7) Point this *Square* into *Periods* of two Figures each.

(8) Then make the first *Root* without its *Cyphers* a *Divisor*, and ask how oft it may be found in the first *Period* of the *Square*.

(9) If the *Divisor* be *less than just*, you must multiply the *Quotient-Figure* by half the *Index*, i. e. if the *Index* be 11, multiply the *Quotient-Figure* by 5; if the *Index* be 9, multiply it by 4, &c. and add it to the *Divisor*; but if it be *more than just*, you must subtract it from the *Divisor*, having a *Cypher* annexed, or supposed to be annexed to the *Divisor*; which *Sum* or *Difference* must be multiplied by the said *Quotient-Figure*, and so continued to every new Figure in the *Quotient*.

(10) If the first *Root* with its *Cyphers* be *more than just*, the *Quotient* must be subtracted from it; but if it be *less than just*, it must be added to it; and the *Sum* or *Difference* will be the *Root* required.

3. If an even *Power* be given, and the *Square-Root* of that *Power* being extracted, reduces it to an odd *Power*; you must then proceed with that odd *Power* as the foregoing *Rules* direct.

EXAMPLES.

1. What is the *Sursolid-Root* of 6436343?

6436343

32 the nearest *Sursolid*, whose *Root* and *Cypher* is 20

3236343

The Cube of 20 is = 8000

And 8000 \times 5 is = 40000

Then 40000)3236343(80

Lastly 20

Again 2)80(3

+ 3

+ 3 \times 2 = 6 78

—

1st. *Divisor* = 26 —

23 the *Sursolid-Root* required.

2 to be rejected.

Note, This is a very expeditious Way of extracting the Roots of high Powers, but it is not always exact, because (as Mr. Ward observes, for it was taken from him) there will be a Remainder, and sometimes an Excess or Defect in the last Figure of the Root, when the given Resolvend or Power hath a true Root; as appears by the fifth Example following, whose true Root should not be 384.3 as it there stands, but 384.

2. What is the Sursolid of 48? *Ans. 254803968.*
 3. What is the Sursolid-Root of 8153726976? *Ans. 96.*
 4. What is the Sursolid-Root of 254803968.? *Ans. 48.*
 5. What is the Sursolid-Root of 8349416423424.? *Ans. 384.3*

Of the SQUARE-CUBE-ROOT.

Q. **W**HAT is a Square-Cube?

A. Any Number involved *six Times*, produces a Square-Cube.

E X A M P L E S.

1. What is the Square-Cube of 48? *Ans. 12230590464.*
 2. What is the Square-Cube-Root of 782757789696.? *Ans. 96.*
 3. What is the Square-Cube-Root of 12230590464.? *Ans. 48.*
 4. What is the Square-Cube-Root of 3206175906594816.? *Ans. 384.*

Of the SECOND SURSOLID-ROOT.

Q. **W**HAT is a Second Sursolid?

A. Any Number involved *seven Times*, produces a second Sursolid.

E X A M P L E S.

1. What is the second Sursolid of 96.? *Ans. 75144747810816.*
 2. What is the second Sursolid-Root of 75144747810816.? *Ans. 96.*
 3. What is the second Sursolid-Root of 587068342272.? *Ans. 48.*
 4. What is the second Sursolid-Root of 1231171548132409344.? *Ans. 384.42*

Of the SQUARE-BIQUADRATEROOT.

Q. **W**HAT is a Square-Biquadrate?

A. Any Number involved *eight Times*, is a Biquadrate Squared.

E X A M P L E S.

1. What is the Squared Biquadrate of 48.? *Ans. 28179280429056.*

2. What is the Square Biquadrate-Root of 7213895789838336. ? - - - - - } Answ. 96.
 3. What is the Square-Biquadrate-Root of 28179280429056. ? - - - - - } Answ. 48.
 4. What is the Square-Biquadrate-Root of 472769874482845188096. ? - - - - - } Answ. 384.

Of the CUBED CUBE-ROOT.

Q. **W**HAT is a Cubed Cube?

A. Any Number involved nine Times, is a Cubed Cube.

E X A M P L E S.

1. What is the Cubed Cube-Root of 692533995824480256. ? - - - - - } Answ. 96.2
 2. What is the Cubed Cube-Root of 1352605460594688 ? - - - - - } Answ. 48.09
 3. What is the Cubed Cube-Root of 181543631801412552228864 ? - - - - - } Answ. 384.5.

Of the SQUARE-SURSOLID-ROOT.

Q. **W**HAT is a Squared Sursolid?

A. Any Number involved ten Times, produces a squared Sursolid.

E X A M P L E S.

1. What is the Squared Sursolid-Root of 64925062108545024. ? - - - - - } Answ. 48.
 2. What is the Squared Sursolid-Root of 66483263599150104576. ? - - - - - } Answ. 96.
 3. What is the Squared Sursolid-Root of 69712754611742420055883776. ? - - - - - } Answ. 384.3

Of the THIRD SURSOLID-ROOT.

Q. **W**HAT is a third Sursolid?

A. Any Number involved eleven Times, produces a third Sursolid.

E X A M P L E S.

1. What is the third Sursolid-Root of 952809757913927. ? - - - - - } Answ. 23.
 2. What is the third Sursolid-Root of 3116402981210161152. ? - - - - - } Answ. 48.
 3. What is the third Sursolid-Root of 6382393305518410039296. ? - - - - - } Answ. 96.

Of the SQUARED SQUARE-CUBE-ROOT.

Q. **W**HAT is a Squared Square-Cube?

A. Any Number involved twelve Times, produces a Squared Square-Cube.

E X A M P L E S.

1. What is the Root of this Squared Square-Cube 149587343098087735296. ?	} Answ. 48.
2. What is the Root of this Squared Square-Cube 612709757329767363772416. ?	} Answ. 96.
5. What is the Root of this Squared Square-Cube 10279563944029090291760398073856. ?	} Answ. 384.

A general Rule for extracting the ROOTS of all Powers.

1. PRepare the given Number for *Extraction*, by pointing off from the *Unity Place*, as the *Root* required directs.
2. Find the first Figure in the *Root* by your own Judgment, or by Inspection into the *Table of Powers*.
3. Subtract it from the *given Number*.
4. Augment the *Remainder* by the next Figure in the *given Number*, that is, by the first Figure in the next Point, and call this your *Dividend*.
5. Involve the *whole Root*, last found, into the next inferior *Power* to that which is given.
6. Multiply it by the *Index* of the *given Power*, and call this your *Divisor*.
7. Find a *Quotient Figure* by common *Division*, and annex it to the *Root*.
8. Involve all the *Root* thus found into the *given Power*.
9. Subtract this *Power* (always) from as many Points of the *given Power* as you have brought down, beginning at the lowest *Place*.
10. To the *Remainder* bring down the first Figure of the next Point for a new *Dividend*.
11. Find a new *Divisor* as before, and in like manner proceed till the Work is ended.

EXAM-

EXAMPLES.

1. What is the Cube-Root of 115501303.?

$$\begin{array}{r}
 115501303. (487 \\
 64 \\
 \hline
 48) 515 \text{ Dividend.}
 \end{array}$$

110592 Subtrahend.

6912)49093 Dividend.

115501303 Subtrahend.

$$\begin{array}{r}
 4 \times 4 \times 3 = 48 \text{ Divisor.} \\
 48 \times 48 \times 48 = 110592 \text{ Subtrahend.} \\
 48 \times 48 \times 3 = 6912 \text{ Divisor.} \\
 487 \times 487 \times 487 = 115501303 \text{ Subtrahend.}
 \end{array}$$

2. What is the Biquadrate-Root of 56249134561.?

$$\begin{array}{r}
 56249134561. (487 \\
 256 \\
 \hline
 256) 3064 \text{ Dividend.}
 \end{array}$$

5308416 Subtrahend.

442368)3164974 Dividend.

56249134561 Subtrahend.

$$\begin{array}{r}
 4 \times 4 \times 4 \times 4 = 256 \text{ Divisor.} \\
 48 \times 48 \times 48 \times 48 = 5308416 \text{ Subtrahend.} \\
 48 \times 48 \times 48 \times 4 = 442368 \text{ Divisor.} \\
 487 \times 487 \times 487 \times 487 = 56249134561 \text{ Subtrahend.}
 \end{array}$$

Note, This General Rule I received from my worthy Friend Mr. William Mountaine, Teacher of the Mathematics at Shad-Thames.

Of SIMPLE INTEREST.

Q. *W*hat particular Letters are used here?

A. These; P. any Principal.

T. the Time.

R. the Ratio of the Rate per Cent.

A. the Amount.

Q. *W*hat is the Ratio?

A. It signifies only the *Simple Interest* of 1*l.* for one Year, at any proposed Rate of Interest per Cent. and is thus found;

$$\begin{array}{cccc} l. & l. & l. \\ 100 : 6 & : & 1 : 0.06 \\ 100 : 5 & : & 1 : 0.05 \text{ &c.} \end{array}$$

A TABLE of RATIOS.

Rate per Ct.	Ratio.	Rate per Ct.	Ratio.
2	.02	6 $\frac{1}{2}$.065
3	.03	7	.07
3 $\frac{1}{2}$.035	7 $\frac{1}{2}$.075
4	.04	8	.08
4 $\frac{1}{2}$.045	8 $\frac{1}{2}$.085
5	.05	9	.09
5 $\frac{1}{2}$.055	9 $\frac{1}{2}$.095
6	.06	10	.1

C A S E I.

Q. *W*hen P, T, and R, are given to find A; how is it discovered?

A. Thus, $ptr + p = a$.

Note, Any Quantity of Letters put together like a Word, denote continual Multiplication.

E X A M P L E S.

1. What Sum will 567*l.* 10*s.* amount to in 9 Years, at 6 per Cent. per Ann.? *Answ.* 873*l.* 19*s.*

2. What will 508*l.* 14*s.* amount to in 1 Year, at 5 per Cent. per Ann.? *Answ.* 534*l.* 2*s.* 8*d.* 1*6qr.*

3. What will 600*l.* 14*s.* amount to in 10 Years, at 4 $\frac{1}{2}$ per Cent. per Ann.? *Answ.* 871*l.* 0*s.* 3*d.* 2*4qr.*

4. What will 4000*l.* amount to in 5 Years, at 3 $\frac{1}{2}$ per Cent. per Ann.? *Answ.* 4700*l.*

Note, When the Time given, does not consist of whole Years, then reduce the odd Time into Decimal Parts of a Year. And, unless such Parts of a Year chance to be just $\frac{1}{4}$, $\frac{1}{2}$ or $\frac{3}{4}$ of a Year, the best Way will be to reduce the odd Time into Days, and then work with the Decimal Parts of a Year, that are equivalent to those Days.

A TABLE

A TABLE for the ready finding the Decimal Parts of a Year, equal to any Number of Days, or Quarters of a Year.

Days.	Decimal Pts.	Days.	Decimal Pts.	Days.	Decimal Pts.
1	.00274	10	.027397	100	.273973
2	.005479	20	.054794	200	.547945
3	.008219	30	.082192	300	.821918
4	.010959	40	.109589	365	1.000000
5	.013699	50	.136986		
6	.016438	60	.164383		
7	.019178	70	.191781		$\frac{1}{4}$ of a Year .25
8	.021918	80	.219178		$\frac{1}{2}$ of a Year .5
9	.024657	90	.246575		$\frac{3}{4}$ of a Year .75

Note, When the true Number of Days cannot be found at one View in this Table, then both them and their Decimals must be taken out of the Table at twice or thrice, as their Number requires, and added together. So the Decimal Parts of a Year = 236 Days are thus found,

$$\begin{array}{r} 200 = .547945 \\ 30 = .082192 \\ 6 = .016438 \\ \hline 236 = .646575 \end{array}$$

E X A M P L E S.

5. What will 7200 l. amount to in $6\frac{1}{2}$ Years at 5 per Cent. per Ann.? Answ. 9540 l.

6. What will 1110 l. 18 s. amount to in $12\frac{3}{4}$ Years at 5 per Cent. per Ann.? Answ. 1819 l. 1 s. 11 d. 2.8 qrs.

7. What will 280 l. 10 s. amount to in 3 Years and 148 Days at 5 per Cent. per Ann.? Answ. 382 l. 5 s. 2 d. 3.38 + qrs.

8. What will 196 l. amount to in 189 Days at 4 per Cent. per Ann.? Answ. 200 l. 1 s. 2 d. 1 qr. 23 +

C A S E 2.

Q. When A, T, and R, are given to find P; how is it discovered?

A. Thus $\frac{a}{tr+1} = p$.

E X A M P L E S.

1. I demand what Principal will amount to 873 l. 19 s. in 9 Years at 6 per Cent. per Ann.? Answ. 567 l. 10 s.

2 I demand what Principal will amount to 534 l. 2 s. 8 d. 1.6 qr. in 1 Year at 5 per Cent. per Ann.? Answ. 508 l. 14 s.

3. I demand what Principal will amount to 9540 l. in $6\frac{1}{2}$ Years at 5 per Cent. per Ann.? Answ. 7200 l.

4. I demand what Principal will amount to 1819 l. 1 s. 11 d. 2.8 qrs. in $12\frac{3}{4}$ Years at 5 per Cent. per Ann.? Answ. 1110 l. 18 s.

5. I demand what Principal will amount to 871*l.* 0*s.* 3*d.*
2*4* *qrs.* in 10 Years at 4*1*/*2* per Cent. per Ann.? *Ans*w. 600*l.* 1*4s.*

6. I demand what Principal will amount to 4700*l.* in 5
Years at 3*1*/*2* per Cent. per Ann.? *Ans*w. 4000*l.*

7. I demand what Principal will amount to 328*l.* 5*s.* 2*d.*
3*38* *qrs.* in 3 Years and 148 Days at 5 per Cent.? *Ans*w.
280*l.* 10*s.*

8. What Principal being put to Interest for 189 Days at 4
per Cent. will amount to 200*l.* 1*s.* 2*d.* $\frac{1}{2}$? *Ans*w. 196*l.*

C A S E 3.

Q. When A, P, and T, are given to find R; how is it discovered?

A. Thus $\frac{a-p}{tp} = r.$

E X A M P L E S.

1. At what Rate per Cent. will 567*l.* 10*s.* amount to 873*l.*
19*s.* in 9 Years? *Ans*w. 6*l.* per Cent.

2. At what Rate per Cent. will 508*l.* 14*s.* amount to 534*l.*
2*s.* 8*d.* 1*6* *qr.* in 1 Year? *Ans*w. 5*l.* per Cent.,

3. At what Rate per Cent. will 7200*l.* amount to 9540*l.*
in 6*1*/*2* Years? *Ans*w. 5*l.* per Cent.

4. At what Rate per Cent. will 1110*l.* 18*s.* amount to
1819*l.* 1*s.* 1*d.* 2*8* *qrs.* in 12*3*/*4* Years? *Ans*w. 5*l.* per Cent.

5. At what Rate per Cent. will 600*l.* 14*s.* amount to 871*l.*
0*s.* 3*d.* 2*4* *qrs.* in 10 Years? *Ans*w. 4*1*/*2* per Cent.

6. At what Rate per Cent. will 4000*l.* amount to 4700*l.*
in 5 Years? *Ans*w. 3*1*/*2* per Cent.

7. At what Rate per Cent. will 280*l.* 10*s.* amount to 328*l.*
5*s.* 2*d.* 3*38* *qrs.* in 3 Years, and 148 Days? *Ans*w. 5*l.* per Cent.

8. At what Rate per Cent. will 196*l.* amount to 200*l.* 1*s.*
2*d.* $\frac{1}{2}$ in 189 Days? *Ans*w. 4*l.* per Cent.

C A S E 4.

Q. When A, P, and R, are given to find T; how is it discovered?

A. Thus $\frac{a-p}{rp} = t.$

E X A M P L E S.

1. In what Time will 567*l.* 10*s.* amount to 873*l.* 19*s.*
at 6 per Cent.? *Ans*w. 9 Years.

2. In what Time will 508*l.* 14*s.* amount to 534*l.* 2*s.*
8*d.* 1*6* *qr.* at 5 per Cent.? *Ans*w. 1 Year.

3. In what Time will 7200*l.* amount to 9540*l.* at 5 per
Cent.? *Ans*w. 6*1*/*2* Years.

4. In what Time will 1110*l.* 18*s.* amount to 1819*l.* 1*s.*
11*d.* 2.8*qrs.* at 5 per Cent. ? *Answ.* 12 $\frac{3}{4}$ Years.
5. In what Time will 600*l.* 14*s.* amount to 871*l.* 0*s.*
3*d.* 2.4*qrs.* at 4 $\frac{1}{2}$ per Cent. ? *Answ.* 10 Years.
6. In what Time will 4000*l.* amount to 4700*l.* at 3 $\frac{1}{2}$ per
Cent. ? *Answ.* 5 Years.
7. In what Time will 280*l.* 10*s.* amount to 328*l.* 5*s.* 2*d.*
3.38*qrs.* at 5 per Cent. ? *Answ.* 3 Years, and 148 Days.
8. In what Time will 196*l.* amount to 200*l.* 1*s.* 2*d.* $\frac{1}{2}$ at
4 per Cent. ? *Answ.* 189 Days.

Of ANNUITIES or PENSIONS in ARREARS.

Q. What is meant by Annuities or Pension in Arrears ?

A. Annuities or Pensions are said to be in Arrears, when they are payable, either Yearly, half Yearly, or Quarterly, and are unpaid for any Number of Payments.

Note, U, represents the Annuity, Pension, &c. R, T, and A, as before.

C A S E I.

Q. When U, R, and T, are given to find A; how is it discovered?

$$A. \text{ Thus } \frac{tu - tu}{2} \times r : + tu = a.$$

E X A M P L E S.

1. If an Annuity of 70*l.* be forborn 5 Years; what will it amount to in that Time at 5 per Cent. ? *Answ.* 385*l.*
2. If the Payment of a Pension be omitted for 7 Years; what will be the Amount in that Time at 6 per Cent. when the Pension is 56*l.* per Ann. ? *Answ.* 462*l.* 11*s.* 2*d.* 1.6*qr.*
3. An House is lett upon Lease for 7 Years at 50*l.* per Annun; I demand the Amount for that Time at 4*l.* per Cent. for the Forbearance of Payment ? *Answ.* 392*l.*
4. Suppose a Salary of 100*l.* per Ann. be forborn 7 Years; what is the Amount at 4 $\frac{1}{2}$ per Cent. ? *Answ.* 794*l.* 10*s.*

Note, When the Annuities or Rents are to be paid by half-yearly or quarterly Payments, as most generally they are, then,

For half-yearly Payments take (always) half of the Ratio, half of the yearly Rent, and twice the Number of Years; that is, reduce the Years into half Years, for R, U, and T; But,

For quarterly Payments, take a fourth Part of the Ratio, a fourth Part of the yearly Rent, and four Times the Number of Years; that is, reduce the Years into Quarters, and work as before.

E X A M P L E S.

5. If 70*l.* Annuity payable every half Year, were unpaid 5 Years; what will it amount to in that Time at 5 per Cent. ?
Answ. 389*l.* 7*s.* 6*d.*
6. If

6. If 70*l.* Annuity payable every Quarter, were unpaid 5 Years; what will it amount to in that Time at 5 per Cent.?

Answ. 391*l.* 11*s.* 3*d.*

Note, By comparing these two Examples with the first, it may be observed, that the Amount of half-yearly Payments, is more advantageous than yearly Payments; and quarterly, than half-yearly Payments.

C A S E 2.

Q. When A, R, and T, are given to find U; how is it discovered?

A. Thus $\frac{2a}{trt - tr + 2t} = u.$

E X A M P L E S.

1. If the Amount of an Annuity for 5 Years at 5 per Cent. be 385*l.* what is the Annuity? *Answ.* 70*l.*

2. If the Amount of a Pension be 462*l.* 11*s.* 2*d.* 1.6 qr. the Time be 7 Years, and the Rate per Cent. 6*l.* what is the Pension? *Answ.* 56*l.*

3. If an House be lett upon Lease for 7 Years, and the Amount for that Time be 392*l.* at 4 per Cent. what is the yearly Rent? *Answ.* 50*l.*

4. If a Salary amounts to 794*l.* 10*s.* in 7 Years at 4*1*/*2* per Cent. what is the Salary? *Answ.* 100*l.* per Ann.

Note, When the Payments are half-yearly, 4a must be divided; but when they are quarterly, then 8a must be divided as before.

E X A M P L E S.

5. If the Amount of an Annuity, payable half-yearly, for 5 Yrs. at 5 per Cent. be 389*l.* 7*s.* 6*d.* what is the Annuity? *Answ.* 70*l.*

6. If the Amount of an Annuity, payable quarterly, for 5 Yrs. at 5 per Cent. be 391*l.* 11*s.* 3*d.* what is the Annuity? *Answ.* 70*l.*

C A S E 3.

Q. When U, A, and T, are given to find R; how is it discovered?

A. Thus $\frac{2a - 2ut}{utt - ut} = r.$

E X A M P L E S.

1. If an Annuity of 70*l.* per Ann. amounts to 385*l.* in 5 Years; I demand the Rate per Cent.? *Answ.* 5*l.*

2. If a Pension of 56*l.* per Ann. amounts to 462*l.* 11*s.* 2*d.* 1.6 qr. in 7 Years; what is the Rate per Cent.? *Answ.* 6*l.*

3. If an House be lett upon Lease for 7 Years at 50*l.* per Ann. and the Amount for that Time be 392*l.* what is the Rate per Cent.? *Answ.* 4*l.* per Cent.

4. If a Salary of 100*l.* per Ann. being forbore 7 Years amounts to 794*l.* 10*s.* I demand the Rate per Cent.? *Answ.* 4*1*/*2*.

Note, When the Payments are half-yearly, then 4a — 4ut must be divided; but when they are quarterly, then 8a — 8ut must be divided, as before.

E X A M P L E S.

5. If an Annuity of 70*l.* per *Ann.* payable half-yearly, being forborn 5 Years, amounts to 389*l.* 7*s.* 6*d.* I demand the Rate per Cent.? *Answ.* 5*l.* per Cent.

6. If an Annuity of 70*l.* per *Ann.* payable quarterly, amounts to 391*l.* 11*s.* 3*d.* in 5 Years; I demand the Rate per Cent.? *Answ.* 5*l.* per Cent.

C A S E 4.

Q. When *U*, *A*, and *R*, are given to find *T*; how is it discovered?

A. Thus; First $\frac{2}{r} - 1 = x.$

Secondly $\sqrt{\frac{2A}{ru}} + \frac{xx}{4} - \frac{1}{2}x = t.$

E X A M P L E S.

1. In what Time will 70*l.* per *Ann.* amount to 385*l.* forborn at 5 per Cent.? *Answ.* 5 Years.

2. In what Time will a Pension of 56*l.* per *Ann.* amount to 462*l.* 11*s.* 2*d.* 1*6qr.* at 6 per Cent.? *Answ.* 7 Years.

3. If an House be lett upon Lease, for a certain Time, for 50*l.* per *Ann.* and the Amount be 392*l.* at 4 per Cent. I demand the Time that it was lett for? *Answ.* 7 Years.

4. If a Salary of 100*l.* per *Ann.* being forborn a certain Time, amount to 794*l.* 10*s.* at 4*1/2* per Cent. I demand the Time of Forbearance? *Answ.* 7 Years.

Note, If the Payments were half-yearly, then *T* will be equal to the Number of Half-Years, or Payments; but if they were to be made Quarterly, then *T* will be equal to the Number of Quarterly Payments.

E X A M P L E S.

5. If an Annuity of 70*l.* per *Ann.* payable half-yearly, being forborn, amount to 389*l.* 7*s.* 6*d.* at 5 per Cent. I demand the Time and Payments forborn? *Answ.* 10 Payments = 5 Years.

6. If an Annuity of 70*l.* per *Ann.* payable quarterly, being forborn, amount to 391*l.* 11*s.* 3*d.* at 5 per Cent. I demand the Time and Payments forborn? *Answ.* 20 Payments = 5 Years.

Of the PRESENT WORTH of ANNUITIES or PENSIONS, &c.

Note, *P*, represents the present Worth; *U*, *T*, and *R*, as in the last.

C A S E I.

Q. When *U*, *T*, and *R*, are given to find *P*; how is it discovered?

A. Thus $\frac{rtt - rt + 2t}{2rt + 2} : x u = p.$

E X A M -

E X A M P L E S.

1. What is the present Worth of 50*l.* per *Ann.* to continue 6 Years at 5 per Cent. ? *Answe.* 259*l.* 12*s.* 3*d.* 2*4* + *qrs.*
2. What is 80*l.* yearly Rent, to continue 5 Years, worth in ready Money at 6 per Cent. ? *Answe.* 344*l.* 12*s.* 3*d.* 2*5* + *qrs.*
3. What is a Salary of 40*l.* per *Ann.* to continue 7 Years, worth in ready Money at 4 per Cent. ? *Answe.* 245*l.*
4. What is a Pension of 30*l.* per *Ann.* for 5 Years, worth in ready Money at 4*1*/*2* per Cent. ? *Answe.* 133*l.* 9*s.* 4*d.* 2*6* + *qrs.*

Note, Observe the same Note here, which is given in Case 1. in *Annuities and Pensions in Arrears, concerning half-yearly and quarterly Payments.*

5. What is the present Worth of 50*l.* per *Ann.* payable half-yearly for 6 Years, at 5 per Cent. ? *Answe.* 262*l.* 10*s.*
6. What is the present Worth of 50*l.* per *Ann.* payable quarterly for 6 Years, at 5 per Cent. ? *Answe.* 263*l.* 18*s.* 9*d.* 3*6* *qrs.*

Note, By comparing these two Examples with the first, it may be observed, that the present Worth of half-yearly Payments, is more advantageous than yearly Payments, and the present Worth of quarterly than half-yearly Payments.

C A S E 2.

Q. When P, T, and R, are given to find U; how is it discovered?

A. Thus
$$\frac{rt + 1}{rt - rt + 2t} : X 2p = u.$$

E X A M P L E S.

1. There is a Lease of an House 6 Years to come; I demand the yearly Rent, when the present Worth at 5*l.* per Cent. is 259*l.* 12*s.* 3*d.* 2*qrs.* ? *Answe.* 50*l.* per *Ann.*
2. What yearly Rent is that, the present Worth of which for 5 Years is 344*l.* 12*s.* 3*d.* 2*qrs.* at 6 per Cent. ? *Answe.* 80*l.* per *Ann.*
3. What Salary is that which for 7 Years Continuance at 4 per Cent. produces 245*l.* for the present Worth ? *Answe.* 40*l.* per *Ann.*
4. If the present Worth of a Pension, to continue 5 Years at 4*1*/*2* per Cent. be 133*l.* 9*s.* 4*d.* 3*qrs.* I demand the Pension ? *Answe.* 30*l.*

Note, When the Payments to be made, are half-yearly, you must multiply by 4*p*; but when they are quarterly, then multiply by 8*p* to find *u*.

E X A M P L E S.

5. There is a Lease of an House, payable half-yearly, for 6 Years to come; I demand the yearly Rent, when the present Worth at 5 per Cent. is 262*l.* 10*s.* ? *Answe.* 50*l.*
6. There is a Lease of an House, payable quarterly, for 6 Years to come; I demand the yearly Rent, when the present Worth at 5 per Cent. is 263*l.* 18*s.* 9*d.* 3*6* *qrs.* ? *Answe.* 50*l.*

C A S E

C A S E 3.

Q. When U, P, and T, are given to find R, how is it discovered?

A. Thus;
$$\frac{2ut - 2p}{2pt - utt - ut} = r.$$

E X A M P L E S.

1. I demand at what Rate per Cent. will the yearly Rent of 50*l.* to continue 6 Years, produce the present Worth of 259*l.* 12*s.* 3*d.* 2*qrs.*? Answ. 5*l.* per Cent.

2. If the yearly Rent of 80*l.* per Ann. to continue 5 Years, bring 344*l.* 12*s.* 3*d.* 2*qrs.* present Worth; what is the Rate per Cent.? Answ. 6*l.* per Cent.

3. If a Salary of 40*l.* per Ann. to continue 7 Years, produce 245*l.* for the present Worth; what is the Rate per Cent.? Answ. 4*l.* per Cent.

4. If a Pension of 30*l.* per Ann. to continue 5 Years, produce 133*l.* 9*s.* 4*d.* 2*qrs.* for the present Worth, what is the Rate per Cent.? Answ. 4*l.* per Cent.

Note, When the Annuities or Rents, are to be paid half-yearly or quarterly, then

For half-yearly Payments, take half of the Annuity or yearly Rent, and twice the Number of Years; that is, reduce the Years into half Years, and then the Quotient of the upper Part divided by the lower, will be the Ratio, of half the Rate per Cent.

For quarterly Payments, take a fourth Part of the Annuity or yearly Rent, and four Times the Number of Years; that is, reduce the Years into Quarters; and then the Quotient of the upper Part divided by the lower, will be the Ratio of a fourth Part of the Rate per Cent.

E X A M P L E S.

5. A Lease of an House of 50*l.* per Ann. payable half-yearly, having 6 Years to come, is sold for 262*l.* 10*s.* I demand the Rate per Cent.? Answ. 5*l.* per Cent.

6. A Lease of an House of 50*l.* per Ann. payable quarterly, having 6 Years to come, is sold for 263*l.* 18*s.* 9*d.* 3*qrs.* I demand the Rate per Cent.? Answ. 5*l.* per Cent.

C A S E 4.

Q. When U, P, and R, are given to find T, how it is discovered?

A. Thus; First,
$$\frac{2}{r} - \frac{2p}{u} - 1 = x.$$

Secondly,
$$\sqrt{\frac{2p}{ru} + \frac{xx}{4}} : - \frac{x}{2} = t.$$

E X A M P L E

E X A M P L E S.

1. If 50*l.* yearly Rent, produce the present Worth of 259*l.* 12*s.* 3*d.* 2*qrs.* at 5 per Cent. what is the Time of its Continuance? *Answ.* 6 Years.

2. I demand how long 80*l.* per Ann. may be purchas'd for 344*l.* 12*s.* 3*d.* 2*qrs.* at 6 per Cent.? *Answ.* 5 Years.

3. How long must a Salary of 40*l.* per Ann. be enjoyed for 245*l.* at 4 per Cent.? *Answ.* 7 Years.

4. What Time may a Pension of 30*l.* per Ann. be bought for 133*l.* 9*s.* 4*d.* 2*qrs.* at 4*1*/*2* per Cent.? *Answ.* 5 Years.

Note 1, If the Payments are to be half-yearly, then *U* will be $\frac{1}{2}$ half of the given Lease, Pension, &c. and *R* will be $\frac{1}{2}$ half of the Ratio of the given Rate; and *T* which is required, will be $\frac{1}{2}$ the Number of Payments or half Years.

2. If the Payments are to be quarterly, then *U* will be $\frac{1}{4}$ a fourth Part of the given Lease, Pension, &c. and *R* will be $\frac{1}{4}$ a fourth Part of the Ratio of the given Rate; and *T* will be the Number of quarterly Payments.

E X A M P L E S.

5. A Lease of an House of 50*l.* per Ann. payable half-yearly, is sold for 262*l.* 10*s.* at 5 per Cent. I demand the Number of Payments, and the Time to come? *Answ.* 12 Payments = 6 Yrs.

6. A Lease of an House of 50*l.* per Ann. payable quarterly, is sold for 263*l.* 18*s.* 9*d.* 3*qrs.* at 5 per Cent. I demand the Number of Payments, and the Time to come? *Answ.* 24 Payments = 6 Years.

Of ANNUITIES, LEASES, &c. taken in REVERSION.

C A S E I.

Q. How do you find the present Worth of an Annuity, &c. in Reversion?

A. Thus; First, Find the present Worth of the yearly Sum at the given Rate, and for the Time of its Continuance; to do which, there are given *U*, *T*, and *R* to find *P*, which is thus discovered;

$$\frac{rtt - rt + 2t}{2rt + 2} : \times u = p.$$

Secondly, Find what Principal being put to Interest will amount to *P*, at the same Rate, and for the Time to come before the Annuity, &c. commences; and that will be the present Worth of the Annuity, &c. in Reversion: Therefore let *P* be changed into *A* = the Amount, and then there will be given *A*, *R*, and *T*, to find *P*, or the Principal, which is thus discovered;

$$\frac{a}{tr + 1} = p.$$

E X A M -

E X A M P L E S.

1. What is the present Worth of a Lease of 30*l.* per *Ann.* to continue 3 Years; but is not to commence till the end of 2 *Yrs.* allowing 4 per *Cent.* to the Purchaser? *Ans.* 77*l.* 7*s.* 7*d.*

2. I have the Promise of a Pension of 17*l.* per *Ann.* for 7 Years, but it does not commence till the end of 4 Years; and I am willing to dispose of the same for present Payment, at the Rate of 5 per *Cent.* I demand the present Worth? *Ans.* 84*l.* 9*s.* 6*d.*

3. There is a Legacy of 20*l.* per *Ann.* for 8 Years, left to a Person of 16 Years of Age; the Time of Payment is to commence at the Year of Perfection, *i.e.* at 21 Years; but he wanting a Sum of Money, is minded to sell the same at 4 per *Cent.* I demand the present Worth? *Ans.* 115*l.* 3*s.* 0*d.* 1.44*qr.*

4. A good-natured Gentleman, being minded to bestow a Favour upon an unthankful Wretch, settled upon him an Income of 35*l.* per *Ann.* for 12 Years, to commence 5 Years after such Settlement, but he wanting Money to follow his Extravagancies, sold it at the Rate of 10 per *Cent.* I demand how much he received for the present Worth? *Ans.* 197*l.* 5*s.* 5*d.* 1.792*qr.*

C A S E 2.

Q. How do you find the yearly Income of an Annuity, &c. in Reversion.

A. Thus; First, Find the Amount of the present Worth of the yearly Sum, at the given Rate, and for the Time before the Reversion, to do which, there are given *P*, *T*, and *R*, to find *A*, which is thus discovered;

$$ptr + p = a.$$

Secondly, Find what yearly Rent being sold, will produce *A*, for the present Worth *b*, at the same Rate, and for the Time of its Continuance; and that will be the yearly Sum required: Therefore change *A* into *P*, and then there will be given *P*, *R*, and *T*, to find *U*, or the yearly Sum, thus;

$$\frac{rt + 1}{rtt - rt + 2t} : \times 2p = u.$$

E X A M P L E S.

1. There is a Lease of an House taken for 3 Years, but commences not till the End of 2 Years; and the Lessee would sell the same for 77*l.* 7*s.* 7*d.* present Payment; I demand the yearly Rent? *Ans.* 30*l.* per *Ann.*

2. I have the Promise of a Pension for 7 Years, which will not commence till the End of 4 Years; and I have dispos'd of the same for the present Payment of 84*l.* 9*s.* 6*d.* allowing 5 per *Cent.* to the Purchaser; I demand the yearly Income? *Ans.* 17*l.*

3. There is a Legacy of a certain Rate *per Ann.* for 8 *Yrs.* left to a Person of 16 *Years* of Age; but the Time of Payment must not commence till the Age of Perfection; and the same Person wanting a Sum of Mony, sold it for 115*l.* 3*s.* 0*d.* 2*grs.* allowing 4 *per Cent.* to the Buyer; I demand the yearly Rate? *Answ.* 20*l.*

4. A good-natured Gentleman, being minded to bestow a Favour upon an unthankful Wretch, settled an Income upon him for 12 Years, at a certain Rate *per Ann.* to commence 5 Years after such Settlement; but he wanting Mony to follow his Extravagancies, sold it for 197*l.* 5*s.* 5*d.* 2*grs.* allowing 10 *per Cent.* to the Buyer for present Payment; I demand the yearly Value? *Answ.* 35*l.*

Of SIMPLE INTEREST for DAYS.

Q. How do you find the Simple Interest of any Sum of Mony, for any Number of Days?

A. Multiply the Interest of one Pound for one Day, at the given Rate, by the Principal, and by the Number of Days; the last Product is the Interest required.

Note, The Interest of one Pound for one Day at

per Cent.	1 <i>is</i>	= .00002739726
	2 <i>is</i>	= .00005479452
	3 <i>is</i>	= .00008219178
	4 <i>is</i>	= .00010958904
	5 <i>is</i>	= .0001369863
	6 <i>is</i>	= .00016438356
	7 <i>is</i>	= .00019178082
	8 <i>is</i>	= .00021917808
	9 <i>is</i>	= .00024657534
	10 <i>is</i>	= .0002739726

E X A M P L E S.

1. What is the Interest of 120*l.* for 126 Days, at 4 *per Cent.*? *Answ.* 1*l.* 13*s.* 1*d.* 2*grs.* +

2. What is the Interest of 126*l.* for 145 Days, at 6 *per Cent.*? *Answ.* 3*l.* 0*s.* 0*d.* 3*grs.* +

3. What is the Interest of 100*l.* from the 1st of June 1743, to the 9th of March following at 5 *per Cent.*? *Answ.* 3*l.* 16*s.* 1*d.* 3*grs.*

4. What is the Interest of 200*l.* from the 14th of August 1744, to the 19th of December following at 6 *per Cent.*? *Answ.* 4*l.* 4*s.* 1*d.* 3*grs.* +

5. What is the Interest of 10*l.* for 25 Days, at 5 *per Cent.*? *Answ.* 8*d.* +

6. What is the Interest of 40*l.* for 40 Days at 4 *per Cent.*? *Answ.* 3*s.* 6*d.* +

Note, There is another Way of answering Questions in Interest for Days, which is laid down in Case 1, in Simple Interest, Page 132; as appears by the eighth Question in that Case. The Reader may use which he likes best.

Of REBATE or DISCOUNT.

Q. What particular Letters are used in Rebate?

A. These :

S, the Sum to be discounted;

P, the present Worth of that Sum, due at any Time to come;

T, the Time before it becomes due;

R, the Ratio of the Rate per Cent.

C A S E 1.

Q. When *S*, *T*, and *R*, are given to find *P*; how is it discovered?

A. Thus; $\frac{s}{tr+1} = p$.

E X A M P L E S.

1. What is the present Worth of 795*l.* 11*s.* 2*d.* for 11 Months at 6 per Cent.? *Answ.* 754*l.* 1*s.* 8*d.* +

2. What is the present Worth of 161*l.* 10*s.* for 19 Months, at 5 per Cent.? *Answ.* 149*l.* 13*s.* 0*d.* 3*qrs.* +

3. If a Legacy of 1000*l.* is left me the 24th of July 1744, to be paid on the Christmas-day following; what must I receive when I allow 6 per Cent. for present Payment? *Answ.* 975*l.* 3*s.* 0*d.* 3*qrs.* +

C A S E 2.

Q. When *P*, *T*, and *R*, are given to find *S*; how is it discovered?

A. Thus; $ptr + p = s$.

E X A M P L E S.

1. Suppose I receive 754*l.* 1*s.* 8*d.* now, for a Sum of Money, due 11 Months hence, allowing 6 per Cent. for present Payment; I demand the Sum that was due at the first? *Answ.* 795*l.* 11*s.* 2*d.*

2. There is a certain Debt, payable 19 Months hence; but I agree with the Debtor to pay me down 149*l.* 13*s.* 0*d.* $\frac{3}{4}$ and allow him 5 per Cent. for present Payment; I demand how much the Debt is? *Answ.* 161*l.* 10*s.*

3. A Legacy was left me the 24th of July 1744, to be paid on the Christmas-day following, but I agree with the Executor, and allow him 6 per Cent. for the present Payment of 975*l.* 3*s.* 0*d.* 3*qrs.* I demand what the Legacy was? *Answ.* 1000*l.*

C A S E 3.

Q. When *S*, *P*, and *R*, are given to find *T*; how is it discovered?

A. Thus; $\frac{s-p}{rp} = t$.

EXAM.

EXAMPLES.

1. The present Worth of 795*l.* 11*s.* 2*d.* due for a certain Time to come, is 754*l.* 1*s.* 8*d.* at 6 per Cent. I demand in what Time the first Sum should have been paid, if no Rebate had been made? *Answ.* 11 Months.

2. There is 161*l.* 10*s.* due at a certain Time to come, but I allow 5 per Cent. to the Debtor, for the present Payment of 149*l.* 13*s.* 0*d.* 3*qrs.* I demand when the Sum should have been paid without any Rebate? *Answ.* 19 Months.

3. I have received 975*l.* 3*s.* 0*d.* 3*qrs.* for a Legacy of 1000*l.* allowing the Executor 6 per Cent. I demand when the Legacy was payable, without Rebate? *Answ.* 155 Days.

CASE 4.

Q. When S, P, and T, are given to find R; how is it discovered?

$$A. \text{ Thus; } \frac{s-p}{tp} = r.$$

EXAMPLES

1. At what Rate per Cent. will 795*l.* 11*s.* 2*d.* payable 11 Months hence, produce 754*l.* 1*s.* 8*d.* for present Payment? *Answ.* 6 per Cent.

2. At what Rate per Cent. will 161*l.* 10*s.* payable 19 Months hence, produce the present Payment of 149*l.* 13*s.* 0*d.* 3*qrs.*? *Answ.* 5 per Cent.

3. Suppose a Legacy of 1000*l.* is left me the 24th of July 1744, to be paid on the Christmas-day following; but I agree with the Executor for the present Payment of 975*l.* 3*s.* 0*d.* 3*qrs.* I demand the Rate per Cent. allow'd for his Money? *Answ.* 6 per Cent.

Of EQUATION of PAYMENTS; (the true Way.)

Q. How is the equated Time for the Payment of a Sum of Money, due at several Times found out?

A. Thus; 1. Find the present Worth of each Payment for its respective Time, as in Rebate; that is;

$$\frac{s}{tr+1} = p$$

2. Add all the present Worths together, and call that Sum also P; then is $s-p=d$ the Rebate.

3. $\frac{d}{pr} = e$ is the true equated Time.

EXAMPLES

EXAMPLES.

1. *A* owes *B* 200*l.* to be paid as follows, *viz.* 100*l.* at 2 Months; and 100*l.* at 4 Months; but they agree to have but one Payment of the Whole, Rebate being made at 6 per Cent. I demand the true equated Time? *Answ.* 3 Months.

2. A Merchant hath owing him 300*l.* to be paid as follows; 50*l.* at 2 Months, 100*l.* at 5 Months, and the rest at 8 Months, and it is agreed to have but one Payment of the Whole, Rebate being made at 5 per Cent. I demand the equated Time? *Answ.* 5.9796 Months.

3. Fowes to *H* 1000*l.* whereof 200*l.* is to be paid present; 400*l.* at 5 Months; and the rest at 10 Months; but they agree to have but one Payment of the Whole, at the Rate of 4 per Cent. Rebate; I demand the true equated Time? *Answ.* 181 Days.

4. A Man owes to a Merchant 1200*l.* to be paid as follows, 200*l.* down; 500*l.* at the End of 10 Months; and the rest at the End of 20 Months; and they agree to have but one Payment of the Whole, Rebate at 3 per Cent. I demand the true equated Time? *Answ.* 1 Year, 11 Days.

Of COMPOUND INTEREST.

Q. *W*THAT particular Letters are here used?

A. These;

P, the Principal;

T, the Time;

R, the Amount of 1*l.* for 1 Year, at any given Rate;

A, the Amount.

Q. How is the Amount of 1*l.* for 1 Year, at any propos'd Rate per Cent. found?

A. Thus;

$$\text{As } 100 : 106 :: 1 : 1.06$$

$$100 : 105 :: 1 : 1.05, \text{ &c.}$$

A TABLE of the AMOUNTS of 1*l.* for 1 Year.

Rates per Ct.	Amts. of 1 <i>l.</i>	Rates per Ct.	Amts. of 1 <i>l.</i>
2	1.02	6 $\frac{1}{2}$	1.065
3	1.03	7	1.07
3 $\frac{1}{2}$	1.035	7 $\frac{1}{2}$	1.075
4	1.04	8	1.08
4 $\frac{1}{2}$	1.045	8 $\frac{1}{2}$	1.085
5	1.05	9	1.09
5 $\frac{1}{2}$	1.055	9 $\frac{1}{2}$	1.095
6	1.06	10	1.1

CASE 1.

Q. When P, T, and R, are given to find A; how is it discovered?

A. Thus; $P \times r^t = A$.

EXAMPLES.

1. What Sum will 450*l.* amount to in three Years Time at 5 per Cent. per Ann.? Answ. 520*l.* 18*s.* 7*d.* 2*qrs.*
2. What will 400*l.* amount to in 4 Years at 6 per Cent. per Ann.? Answ. 504*l.* 19*s.* 9*d.* 3.15264*qrs.*
3. What will 480*l.* amount to in 6 Years at 5 per Cent. per Ann.? Answ. 643*l.* 4*s.* 11.0178*d.*
4. What is the Amount of 500*l.* at 4*1/4* per Cent. per Ann. for 4 Years? Answ. 590*l.* 11*s.* 5*d.* 2.95*+qrs.*

CASE 2.

Q. When A, R, and T, are given to find P; how is it discovered?

A. Thus; $\frac{A}{r^t} = P$.

EXAMPLES.

1. What Principal must be put to Interest, to amount to the Sum of 520*l.* 18*s.* 7*d.* 2*qrs.* in 3 Years at 5 per Cent. per Ann.? Answ. 450*l.*
2. What Principal will amount to 504*l.* 19*s.* 9*d.* 3.15264*qrs.* in 4 Years, at 6 per Cent. per Ann.? Answ. 400*l.*
3. What Principal will amount to 643*l.* 4*s.* 11.0178*d.* in 6 Years, at 5 per Cent. per Ann.? Answ. 480*l.*
4. What Principal will amount to 590*l.* 11*s.* 5*d.* 2.95*+qrs.* in 4 Years, at 4*1/4* per Cent. per Ann.? Answ. 500*l.*

CASE 3.

Q. When P, R, and A, are given to find T; how is it discovered?

A. Thus; $\frac{A}{P} = r^t$ which being continually divided by r ,
till nothing remain, the Number of
those Divisions will be $= t$.

EXAMPLES.

1. In what Time will 450*l.* amount to 520*l.* 18*s.* 7*d.* 2*qrs.* at 5 per Cent. per Ann.? Answ. 3 Years.
2. In what Time will 400*l.* amount to 504*l.* 19*s.* 9*d.* 3.15264*qrs.* at 6 per Cent. per Ann.? Answ. 4 Years.

3. In what Time will 480*l.* amount to 643*l.* 4*s.* 11*d.* at 5 per Cent. per Ann. ? Answ. 6 Years.

4. In what Time will 500*l.* amount to 590*l.* 11*s.* 5*d.* 3*qrs.* at 4*1*/*4* per Cent. per Ann. ? Answ. 4 Years.

CASE 4.

Q. When P, A, and T, are given to find R; how is it discovered?

A. Thus; $\frac{a}{p} = r^t$ { which must be extracted by the Rules of Extraction; the Time given in the Question = t shewing the Power.

EXAMPLES.

1. At what Rate per Cent. will 450*l.* amount to 520*l.* 18*s.* 7*d.* 2*qrs.* in 3 Years? Answ. 5 per Cent.

2. At what Rate per Cent. will 400*l.* amount to 504*l.* 19*s.* 9*d.* 3*2* *qrs.* in 4 Years? Answ. 6 per Cent.

3. At what Rate per Cent. will 480*l.* amount to 643*l.* 4*s.* 11*d.* in 6 Years? Answ. 5 per Cent.

4. At what Rate per Cent. will 500*l.* amount to 590*l.* 11*s.* 5*d.* 3*qrs.* in 4 Years? Answ. 4*1*/*4* per Cent.

Of ANNUITIES or PENSIONS in ARREARS.

CASE 1.

Note, U represents the Annuity, Pension, &c. T, R, and A, as before.

Q. When U, T, and R, are given to find A; how is it discovered?

A. Thus; $\frac{ur^t - u}{r - 1} = a.$

EXAMPLES.

1. What will an Annuity of 30*l.* per Ann. payable yearly, amount to in 4 Years at 5 per Cent. ? Answ. 129*l.* 6*s.* 0*d.* 3*6* *qrs.*

2. Suppose a Pension of 50*l.* per Ann. payable yearly, be granted to a superannuated Officer; what is the Amount for 5 Years Forbearance, at 4 per Cent. ? Answ. 270*l.* 16*s.* 3*d.* 3*4* *1*/*2* *qrs.*

3. If the yearly Rent of an House, which is 40*l.* be forborn 7 Years, at 6 per Cent. what is the Amount? Answ. 335*l.* 15*s.* 0*d.* 3*3* *1*/*2* *qrs.*

4. If a Salary of 35*l.* per Ann. to be paid yearly, be omitted for 6 Years at 5*1*/*2* per Cent. what is the Amount? Answ. 241*l.* 1*s.* 7*d.* 2*5* *1*/*2* *qrs.*

CASE 2.

Q. When R, T, and A, are given to find U; how is it discovered?

A. Thus; $\frac{ra - a}{r^t - 1} = u.$

EXAMPLES.

E X A M P L E S.

1. What Annuity, being forborn for 4 Years, will amount to 129 l. 6 s. 1 d. at 5 per Cent. ? *Answe.* 30 l. per Ann.
2. If a Pension, being forborn for 5 Years at 4 per Cent. per Ann. amount to 270 l. 16 s. 4 d. I demand how much it is per Ann. ? *Answe.* 50 l. per Ann.
3. If the yearly Rent of an House, being forborn for 7 Years at 6 per Cent. amount to 335 l. 15 s. 0 d. 3.4 qrs. I demand what the Rent is ? *Answe.* 40 l. per Annum.
4. If the Payment of a Salary be omitted 6 Years ; I demand how much the Salary is, when the Amount is 241 l. 1 s. 7 d. 2.6 qrs. at 5½ per Cent. ? *Answe.* 35 l. per Ann.

C A S E 3.

Q. When U, A, and R, are given to find T ; how is it discovered ?

A. Thus ;
$$\frac{ar + u - a}{u} = r^t$$
 } which being continually divided by r , till nothing remain, the Number of those Divisions will be $= t$.

E X A M P L E S.

1. In what Time will 30 l. per Ann. amount to 129 l. 6 s. 1 d. allowing 5 per Cent. for the Forbearance of Payment ? *Answe.* 4 Years.
2. In what Time will a Pension of 50 l. per Ann. amount to 270 l. 16 s. 4 d. at 4 per Cent. ? *Answe.* 5 Years.
3. In what Time will the yearly Rent of an House, being 40 l. per Ann. amount to 335 l. 15 s. 1 d. at 6 per Cent. for Non-payment ? *Answe.* 7 Years.
4. In what Time will a Salary of 35 l. per Ann. amount to 241 l. 1 s. 7 d. 2.6 qrs. at 5½ per Cent. for the Forbearance of Payment ? *Answe.* 6 Years.

Note, In this and the two next Sections might be placed Case 4 ; but because it requires an Algebraic Method of proceeding, in order to find R, I omit inserting it in its Place ; this being design'd to treat only of Numbers.

Of the PRESENT WORTH of ANNUITIES,
PENSIONS, &c.

Note, P, is the present Worth, U, R, and T, as in the last.

C A S E I.

Q. When U, T, and R, are given to find P ; how is it discovered ?

$$A. \text{ Thus ; } \frac{u}{r - 1} = p.$$

E X A M P L E S.

1. What is the yearly Rent of 20*l.* to continue 6 Years, worth in ready Money, at 5 per Cent. ? *Answe.* 101*l.* 10*s.* 3*d.* 3*qrs.*
2. What is the present Worth of a Pension of 30*l.* per *Ann.* for 5 Years, at 4 per Cent. ? *Answe.* 133*l.* 11*s.* 1*d.*
3. What must be the Discount of a Lease of 50*l.* per *Ann.* when present Payment is made for 4 Years at 3 per Cent. ? *Answe.* 14*l.* 2*s.* 10*d.* 2*qrs.*
4. An House is lett upon Lease for 4 Years at 70*l.* per *Ann.* and the Lessee is desired to make present Payment, provided the Lessor will allow him 5*3*/*4* per Cent. I demand how much must be paid down, and how much discounted ?

Answe. { 243*l.* 19*s.* 0*d.* 3*qrs.* to be paid down.
36*l.* 0*s.* 11*d.* 1*qr.* to be discounted.

C A S E 2.

Q. When P, T, and R, are given to find U ; how is it discovered ?

A. Thus ;
$$\frac{prt \times r - prt}{rt - 1} = u.$$

E X A M P L E S.

1. What Annuity or yearly Rent to continue 6 Years, may be purchased for 101*l.* 10*s.* 3*d.* 3*qrs.* at 5 per Cent. ? *Answe.* 20*l.*
2. Suppose the present Payment of 133*l.* 11*s.* 1*d.* were required for a Pension for 5 Years to come at 4 per Cent. what is that Pension ? *Answe.* 30*l.* per *Ann.*
3. If the present Payment of 185*l.* 17*s.* 1*d.* 2*qrs.* be made for the Lease of an House, 4 Years to come at 3 per Cent. what is the yearly Rent ? *Answe.* 50*l.* per *Ann.*
4. If an House is lett upon Lease for 4 Years, and the Lessee makes present Payment of 243*l.* 19*s.* 0*d.* 3*qrs.* for that Time at 5*3*/*4* per Cent. what is the yearly Rent of that House ? *Answe.* 70*l.* per *Ann.*

C A S E 3.

Q. When U, P, and R, are given to find T ; how is it discovered ?

A. Thus ;
$$\frac{u}{p + u - pr} = r^t$$
 } which being continually divided by *r*, till nothing remain, the Number of those Divisions will be $\equiv t.$

E X A M P L E S.

1. How long may a Lease of 20*l.* yearly Rent be had for 101*l.* 10*s.* 3*d.* 3*qrs.* allowing 5 per Cent. to the Purchaser ? *Answe.* 6 Years.
2. I

2. I demand what Time a Lease of 30*l.* per *Ann.* may be purchas'd for ; when present Payment of 133*l.* 11*s.* 1*d.* is made at 4 per Cent. ? *Answ.* 5 Years.

3. If 185*l.* 17*s.* 1*d.* 2*qrs.* be paid down for a Lease of 50*l.* per *Ann.* at 3 per Cent. how long is the Lease purchas'd for ? *Answ.* 4 Years.

4. An House is lett upon Lease for 70*l.* per *Ann.* and the Lessee makes present Payment of 243*l.* 19*s.* 0*d.* 3*qrs.* he being allow'd 5*1/4* per Cent. I demand how long the Lease is purchas'd for ? *Answ.* 4 Years.

Of ANNUITIES, LEASES, &c. taken in REVERSION.

CASE I.

Q. How many Operations are there in Case I ?

A. Two.

Q. What is the First ?

A. Find the present Worth of the yearly Sum at the given Rate, and for the given Time of its Continuance ; to do which, there are given *U*, *T*, and *R*, to find *P*.

Q. How is *P* discovered ?

$$A. \text{ Thus ; } \frac{u}{r - 1} = p.$$

Q. What is the Second ?

A. Find what Principal being put to Interest will amount to *P*, at the same Rate, and for the Time to come before the Annuity commences, and that will be the present Worth of the Annuity, &c. in Reversion ; therefore let *P* be changed into *A* = the Amount, and then there will be given *A*, *R*, and *T*, to find *P*, or the Principal.

Q. How is *P* discovered ?

$$A. \text{ Thus ; } \frac{a}{r^t} = p.$$

EXAMPLES.

1. What is the present Worth of the Reversion of a Lease of 20*l.* per *Ann.* to continue 4 Years, but not to commence till the End of two Years, allowing 5 per Cent. to the Purchaser ? *Answ.* 64*l.* 6*s.* 6*d.* 1*4* + *qr.*

2. There

2. There is a Lease of certain Lands worth 32l. per Ann. which is yet in being for 4 Years; and the Lessee is desirous to take a Lease in Reversion for 7 Years, to begin when the old Lease is expired: I demand the present Worth of the said Lease in Reversion, allowing 5 per Cent. to the Purchaser? *Ans*w. $152\text{l. 6s. 8d. 2 qrs. +}$

3. There is an House now building, which I have a mind to take a Lease of for 8 Years; but the House will not be finished within 2 Years; I demand how much I must pay down, when the yearly Rent is 100l. and the Landlord allows me 4 per Cent. on present Payment? *Ans*w. 622l. 9s. 7.2d.

C A S E 2.

Q. How many Operations are there in Case 2?

A. Two.

Q. What is the First?

A. Find the Amount of the present Worth of the yearly Sum at the given Rate, and for the Time before the Annuity commences, to do which, there are given P , R , and T , to find A .

Q. How is A discovered?

A. Thus; $pr^t = a$.

Q. What is the Second?

A. Find what yearly Rent being sold will produce A for the present Worth, at the same Rate, and for the Time of its Continuance; and that will be the yearly Sum required: Therefore let A be changed into P , and then there will be given P , R , and T , to find U , or the yearly Sum.

Q. How is U discovered?

A. Thus; $\frac{pr^t \times r - pr^t}{r^t - 1} = u$.

E X A M P L E S.

1. What Annuity or yearly Rent to be entered upon 2 Years hence, and then to continue 4 Years, may be purchased for $64\text{l. 6s. 6d. 2 qrs. ready Money at 5 per Cent.?$ *Ans*w. 20l.

2. There is a Lease of certain Lands in being for 4 Years, and the Lessee being minded to take a Lease in Reversion for 7 Years, to begin when the old Lease shall be expired, laid down $152\text{l. 6s. 8d. 2 qrs.}$ I demand the yearly Rent of the said Lands, when Allowance was made to the Lessee at 5 per Cent.? *Ans*w. 32l. per Ann.

3. The present Payment for the Lease of an House is 622*l.* 9*s.* 7*d.* Now I have taken a Lease in Reversion for 8 Years, which is to commence at the End of two Years; I demand how much the yearly Rent is, when for the said present Payment I was allowed 4 per Cent. ? *Answe.* 100*l.* per *Ann.*

C A S E 3.

Q. How many Operations are there in Case 3?

A. Two.

Q. What is the First?

A. Find the Amount of the present Worth of the yearly Sum at the given Rate, and for the Time before the Annuity, &c. commences; to do which, there are given *P*, *R*, and *T*, to find *A*, as in Case 2.

Q. How is *A* discovered?

A. Thus; $pr^t = a$.

Q. What is the second Operation?

A. Find what Time the yearly Rent given, being sold for, will produce *A* for the present Worth, at the same Rate, and that will be the Time required: Therefore change *A* into *P*, and then there will be given *U*, *P*, and *R*, to find *T*, as in Case 3, *Page 148.*

Q. How is *T* discovered?

A. Thus; $\frac{u}{p+u-pr} = r^t$ } which being continually divided by *r*, till nothing remains, the Number of those Divisions will be $= t$.

E X A M P L E S.

1. The present Worth of a certain Lease in Reversion, is 64*l.* 6*s.* 6*d.* 2*qrs.* the Lease is 20*l.* per *Ann.* and commences two Years hence, and the Allowance to the Purchaser is 5 per Cent. I demand the Time of its Continuance? *Answe.* 4 Years.

2. A certain Man took a Lease of some Lands for a Time, which by Agreement was not to commence till the Expiration of 4 Years; the yearly Rent was 32*l.* it was also agreed, that the Purchaser should lay down 152*l.* 6*s.* 8*d.* 2*qrs.* and be allow'd for his present Pay 5 per Cent. I demand the Time that the Lease was taken for? *Answe.* 7 Years.

3. The present Payment for the Lease of an House is 622*l.* 9*s.* 7*d.* and the yearly Rent is 100*l.* Now I have taken a Lease in Reversion, which is to commence at the End of 2 Years; I demand the Length of the Lease, when I was allow'd 4 per Cent. for my Money? *Answe.* 8 Years.

Of

Of purchasing FREEHOLD or REAL ESTATES.

Q. What do you understand by a Real or Freehold Estate?

A. Such as is bought to continue for ever.

Note, U, represents the yearly Rent ; R, the Amount of 1*l.* &c. and P the present Worth.

C A S E 1.

Q. When U, and R, are given to find P ; how is it discovered ?

A. Thus ; $\frac{u}{r-1} = p$.

E X A M P L E S.

1. Suppose a Freehold Estate of 40*l.* per Ann. is to be sold ; what is it worth, allowing the Buyer 5 per Cent. for his Money ?

Answ. 800*l.*

2. What is an Estate of 290*l.* per Ann. to continue for ever worth in present Money, allowing 4 per Cent. to the Buyer ?

Answ. 7250*l.*

C A S E 2.

Q. When P and R, are given to find U ; how is it discovered ?

A. Thus ; $p \times \sqrt{r-1} = u$.

E X A M P L E S.

1. If a Freehold Estate is bought for 800*l.* and the Allowance of 5 per Cent. is made to the Buyer ; I demand the yearly Rent ?

Answ. 40*l.* per Ann.

2. If an Estate be sold for 7250*l.* present Money, and 4 per Cent. is allowed to the Buyer for the same ; I demand the yearly Rent ?

Answ. 290*l.* per Ann.

C A S E 3.

Q. When P, and U, are given to find R ; how is it discovered ?

A. Thus ; $\frac{p+u}{p} = r$.

E X A M P L E S.

1. If a Real Estate of 40*l.* per Ann. be sold for 800*l.* I demand the Rate per Cent. ?

Answ. 5 per Cent.

2. If a Freehold Estate of 290*l.* per Ann. be bought for 7250*l.* I demand the Rate per Cent. allow'd ?

Answ. 4 per Cent.

Of purchasing FREEHOLD ESTATES in REVERSION.

C A S E I.

Q. How many Operations are there in Case 1?

A. Two.

Q. What is the First?

A. Find the *present Worth* of the yearly Sum at the given *Rate*; to do which, there are given *U*, and *R*, to find *P*.Q. How is *P* discovered?A. Thus; $\frac{u}{r - 1} = p$.

Q. What is the second Operation?

A. Find what *Principal* being put to *Interest* will amount to *P*, at the same *Rate*, and for the *Time* to come before the Estate commences, and that will be the *present Worth* of the Estate in *Reversion*: Therefore let *P* be changed into *A* = the *Amount*, and then there will be given *A*, *R*, and *T*, to find *P* = the *Principal*.Q. How is *P* discovered?A. Thus; $\frac{a}{r^t} = p$.

E X A M P L E S.

1. Suppose a Freehold Estate of 40*l. per Ann.* to commence 3 Years hence, is to be sold, what is it worth allowing the Purchaser 5*per Cent.* for his present Payment? *Answe.* 691*l. 1s. 4d. 3qrs. +*2. What is an Estate of 290*l. per Ann.* to continue for ever, but not to commence till the Expiration of 4 Years, worth in present Money, Allowance being made at 4*per Cent.*? *Answe.* 6197*l. 6s. 5d. 2qrs. +*

C A S E 2.

Q. How many Operations are there in Case 2?

A. Two.

Q. What is the First?

A. Find the *Amount* of the *present Worth* of the yearly Rent, at the given *Rate*, and for the *Time* before the Estate commences; to do which, there are given *P*, *T*, and *R*, to find *A*.

Q. How

Q. How is A discovered?

A. Thus ; $pr^t = a$

Q. What is the second Operation?

A. Find what yearly Rent being sold will produce A for the present Worth, at the same Rate, and that will be the yearly Sum required : Therefore let A be changed into P, and then there will be given P, and R, to find U, or the yearly Sum.

Q. How is U discovered?

A. Thus ; $\frac{pr \times r - pr}{r} = u$.

EXAMPLES

1. Suppose a Freehold Estate, to commence 3 Years hence, is sold for 691 l. 1 s. 5 d. allowing to the Purchaser 5 per Cent. I demand the yearly Income? Answ. 40 l. per Ann.

2. There is a certain Freehold Estate bought for 6197 l. 6 s. 5 d. 2 qrs. which does not commence till the Expiration of 4 Years ; the Buyer allowed 4 per Cent. for his Money ; I demand the yearly Income? Answ. 290 l. per Ann.

Of REBATE or DISCOUNT.

Q. What particular Letters are used here?

A. These;

S, the Sum to be discounted for;

P, the present Worth of that Sum, due at any Time to come;

T, the Time before it becomes due;

R, the Amount of 1 l. for 1 Year, at any Rate per Cent.

CASE I.

Q. When S, T, and R, are given to find P; how is it discovered?

A. Thus ; $\frac{s}{r^t} = p$.

EXAMPLES.

1. What is the present Worth of 520 l. 18 s. 7 d. 2 qrs. payable 3 Years hence at 5 per Cent.? Answ. 450 l.

2. There is a Debt of 504 l. 19 s. 9 d. 3 qrs. which is not due until 4 Years hence, but it is agreed to be paid in present Money; what Sum must the Creditor receive, allowing the Rebate of 6 per Cent. to the Debtor for his Money? Answ. 400 l.

3. If

3. If 643*l.* 4*s.* 11*d.* be payable in 6 Years Time; what is the present Worth, Rebate being made at 5 per Cent.? *Answ.* 480*l.*

C A S E 2.

Q. When P, T, and R, are given to find S; how is it discovered?

A. Thus; $p \times r^t = s$.

E X A M P L E S.

1. If 450*l.* be received for a Debt, payable 3 Years hence, and an Allowance of 5 per Cent. was made to the Debtor for his present Payment; I demand what the Debt was? *Answ.* 520*l.* 18*s.* 7*d.* 2*qrs.*

2. There is a Sum of Mony due at the Expiration of 4 Years, but the Creditor agrees to take 400*l.* down, allowing 6 per Cent. on present Payment; I demand what the Debt was? *Answ.* 504*l.* 19*s.* 9*d.* 3*qrs.*

3. If a Sum of Mony, due 6 Years hence, produces 480*l.* for present Payment, Rebate being made at 5 per Cent. I demand - how much the Debt was? *Answ.* 643*l.* 4*s.* 11*d.*

C A S E 3.

Q. When S, P, and R, are given to find T; how is it discovered?

A. Thus; $\frac{s}{p} = r^t$ { which being continually divided by r , till nothing remain, the Number of those Divisions will be $= t$.

E X A M P L E S.

1. A certain Man received 450*l.* down for a Debt of 520*l.* 18*s.* 7*d.* 2*qrs.* Rebate being made at 5 per Cent. I demand in what Time the Debt was payable? *Answ.* 3 Years.

2. There is a Debt of 504*l.* 19*s.* 9*d.* 3*qrs.* payable at a certain Time; but it is agreed to pay 400*l.* down at the Allowance of 6 per Cent. to the Debtor for his present Mony; I demand in what Time the Debt would become due, if no such Payment were to be made? *Answ.* 4 Years.

3. The present Payment of 480*l.* is made for a Debt of 643*l.* 4*s.* 11*d.* Rebate at 5 per Cent. I demand when the Debt was payable? *Answ.* 6 Years.

C A S E 4.

Q. When S, P, and T, are given to find R ; how is it discovered ?

A. Thus ; $\frac{s}{p} = r^t$ { which must be extracted by the Rules of Extraction ; the Time given in the Question = t , shewing the Power.

E X A M P L E S.

1. The present Worth of 520*l.* 18*s.* 7*d.* 2*qrs.* payable 3 Years hence is 450*l.* I demand at what Rate per Cent. Rebate was made ? *Ans*w. 5 per Cent.

2. A Debt of 504*l.* 19*s.* 9*d.* 3*qrs.* is due 4 Years hence ; but it is agreed to take 400*l.* down ; what was the Rate per Cent. that the Rebate was made at ? *Ans*w. 6 per Cent.

3. The Sum of 643*l.* 4*s.* 11*d.* is payable in 6 Years time ; and the present Worth of that Sum is 480*l.* I demand at what Rate per Cent. must Rebate be made, to produce the said present Worth ? *Ans*w. 5 per Cent.

Note 1. Equation of Payments at Compound Interest, should follow next ; but as that Rule is best done by the Logarithms, the kind Reader will, I hope, take this as a sufficient Reason for not placing it here.

2. The whole Business of Compound Interest, is better perform'd by the Logarithms, or by Tables calculated for that Purpose, than otherwise ; especially when the Time given is very long, as for 20, 30, or 40 Years, and when the Payments are to be made half-yearly or quarterly. What is here done serves only for whole Years, and shews what can be done by the Pen, where the Logarithms or Tables are wanting.

THE



THE Schoolmasters Assistant.

PART IV.

*A Collection of QUESTIONS to exercise
the foregoing RULES.*

1. RITE down nine Hundred Millions, seven Hundred sixty Thousand, and Twenty-one.



2. What must 20s. pay toward a Tax, when 326l. 6s. 8d. is assessed at 41l. 16s. 2d.? *Ans. 2s. 6d. 2 qrs. 77⁶⁰⁰₃₂₀.*

3. If the $\frac{1}{3}$ of 6 be 3; what shall the $\frac{1}{4}$ of 20 be? *Ans. 7 $\frac{1}{2}$.*

4. I demand the Sum of 1748 added to itself? *Ans. 3496.*

5. I demand the Product of 76 multiplied by itself? *Ans. 5776.*

6. I demand the Difference between 14676 and the Fourth of itself? *Ans. 11007.*

7. I demand the Quotient of the Square of 476 divided by the half of its Root? *Ans. 952.*

8. There is in 3 Bags the Sum of 1468l. *viz.* in the first Bag 461l. in the second 581l. I demand what is in the third Bag? *Ans. 426l.*

9. What Number is that which being multiplied by 13 the Product will be 221? *Ans. 17.*

10. Two Persons, *A* and *B*, owe several Debts; the lesser Debt, being that of *A*, is 2173l. the Difference is 371l. what is the Debt of *B*? *Ans. 2544l.*

11. A Captain and 160 Sailors took a Prize, worth 1360l. of which the Captain had $\frac{1}{3}$ for his Share, and the rest was equally divided among the Sailors; what was each Man's Part? *Ans. The Captain had 272l. and each Sailor had 6l. 16s.*

12. An ancient Lady being demanded how old she was; to avoid a direct Answer, said, I have 9 Children, and there are 3 Years between the Birth of each of them: The Eldest was born when I was 19 Years old, which is now exactly the Age of the Youngest; how old was the Lady? *Ans. 62 Years old.*

13. What Number is that from which if you take 341, the Remainder will be 726? *Ans. 1067.*

14. What Number is that which being added to 168, makes the Sum to be 706? *Ans. 538.*

15. What Number is that which being divided by 19, the Quotient will be 72? *Ans. 1368.*

16. A Broker bought for his Principal, in the Year 1720, 400*l.* Capital Stock in the *South-Sea*, at 650 *per Cent.* and sold it again when it was worth but 130 *per Cent.* how much was lost in the Whole? *Ans. 2080*l.**

17. The Sum of two Numbers is 4139, their Difference is 948; what is the lesser Number? *Ans. 3191.*

18. A Gentlemen went to Sea at 17 Years of Age; 8 Years after that, he had a Son born, who lived 46 Years, and died before his Father; after whom the Father lived twice 20 Years, and then died also; I demand the Age of the Father when he died? *Ans. 111 Years.*

19. Three Gardeners, *A*, *B*, and *C*, having bought a Piece of Ground, find the Profits of it amount to 120*l. per Annum*: Now the Sum of Money which they laid down was in such Proportion, that as often *A* paid 5*l.* *B* paid 7*l.* and as often as *B* 4*l.* *C* paid 6*l.* I demand how much each Man must have *per Annum* of the Gain?

	<i>l.</i>	<i>s.</i>	<i>d.</i>
<i>Ans.</i>	<i>A</i>	26	13 4
	<i>B</i>	37	6 8
	<i>C</i>	56	0 0
		120	0 0

20. *A*, *B*, and *C*, freight a Ship with Wine, *viz.* *A* lays out 1342*l.* *B* 1178*l.* *C* 630*l.* the whole 212 Tuns are sold at 32*l. per Tun*; what shall each Man receive?

	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>grs.</i>
<i>Ans.</i>	<i>A</i>	2890	3 11	3 ¹²³⁰ ₃₃₁₃₀
	<i>B</i>	2537 ² ₃₃₁₃₀		
	<i>C</i>	1356	16 0	

21. *A*, *B*, and *C*, made up a Stock of 1000*l.* whereof *A* put in 409*l.* *B* 198*l.* and they improved it to 1964*l.* I demand what was the Stock of *C*, and what was each Man's Share of the whole Gain?

	<i>l.</i>	<i>s.</i>	<i>d.</i>
<i>Ans.</i>	<i>C's Stock was</i>	393	0 0
	<i>A's Share was</i>	803	5 6 ²⁴⁰ ₁₀₀₀
	<i>B's - - - -</i>	388	17 5 ²⁸⁶ ₁₀₀₀
	<i>C's - - - -</i>	771	17 0 ⁴⁸⁰ ₁₀₀₀

22. *A*,

22. *A, B, and C, freight a Ship for the Canaries worth 3696*l.* whereof A put in 369*l.* B 897*l.* but by reason of a Storm, one third of the Goods was cast over-board ; I demand each Man's Share of the Loss.* Answ. A's Loss was 123*l.* B's 299*l.* and C's 810*l.*

23. *A and B, traded together and gained 100*l.* A put in 640*l.* B put in so much that he must receive 60*l.* of the Gain ; I demand how much B put in ?* Answ. 960*l.*

24. *What is the Value of 27 Dozen, 10 lb. of Candles at 5*d.* per lb. ?* Answ. 6*l.* 19*s.* 2*d.*

25. *Bought 28 qrs. 2 bush. of Wheat, at 4*s.* 6*d.* per Bushel, what is the Worth of it ?* Answ. 50*l.* 17*s.*

26. *If a Man earn 2*s.* 6*d.* 2*qrs.* per Day, how much is that for 19 Weeks, Sundays excepted ?* Answ. 14*l.* 9*s.* 9*d.*

27. *A, B, and C, traded together, the first laid in I know not how much ; B put in 20 Pieces of Cloth ; and C put in 500*l.* and they have gained 1000*l.* whereof A ought to have 350*l.* and B 400*l.* I demand C's Share, how much the first Man laid in, and what the 20 Pieces of Cloth were worth ?* Answ. C's Share was 250*l.* A laid in 700*l.* and B's Cloth was worth 800*l.*

28. *C hath Candles at 6*s.* per Dozen ready Money, but in Barter he will have 6*s.* 6*d.* per Dozen ; D hath Cotton at 9*d.* per lb. ready Money ; I demand what Price the Cotton must be at in Barter ; also how much Cotton must be barter'd for 100 Dozen of Candles ?* Answ. The Cotton must be at 9*d.* 3*qrs.* per lb. in Barter, and 7 C. 0*qr.* 16*lb.* of Cotton must be given for 100 Dozen of Candles.

29. *How many Ducats must I deliver at Venice, to receive at London 178*l.* 2*s.* the Exchange being at 4*s.* 4*d.* per Ducat ?* Answ. 822 Ducats.

30. *A Traveller would change 500 French Crowns at 4*s.* 6*d.* per Crown into Sterling Money, but he must pay a Half-penny per Crown for change ; how much must he receive ?* Answ. 111*l.* 9*s.* 2*d.*

31. *When a Factor taketh 1*l.* per Cent. for his Commission, what must he have for 743*l.* 17*s.* 3*d.* ?* Answ. 7*l.* 8*s.* 9*d.* 1*qr.* $\frac{192}{2400}$.

32. *Two Merchants in Company gain'd 100*l.* A laid in so much, that for his Share of the Gain he must have 60*l.* B laid in 720 Ducats at 6*s.* 8*d.* per Ducat ; I demand how much A laid in, and what the Ducats were worth ?* Answ. A laid in 360*l.* and the Ducats were worth 240*l.*

33. There were two Merchants who traded in Company : The first laid in the Sum of 640*l.* and took $\frac{5}{8}$ of the Gain ; I demand how much the second Merchant laid in ? *Answe.* 384*l.*

34. What Number is that which being multiplied by 15, the Product will be $\frac{3}{4}$? *Answe.* $\frac{1}{20}$.

35. I demand the $\frac{5}{8}$ of 20 Shillings ? *Answe.* 12*s.* 6*d.*

36. What Fraction is that to which if you add $\frac{2}{3}$ the Sum will be $\frac{5}{6}$? *Answe.* $\frac{1}{30}$.

37. What Number is that to which if you add $7\frac{2}{3}$ the Whole will be $12\frac{1}{4}$? *Answe.* $4\frac{7}{2}$.

38. What Number is that from which if you take $\frac{3}{5}$ the Remainder will be $\frac{1}{8}$? *Answe.* $\frac{29}{40}$.

39. What Number is that from which if you take $13\frac{1}{2}$ the Remainder will be $5\frac{5}{7}$? *Answe.* $19\frac{3}{4}$.

40. What Number is that, which being divided by $\frac{3}{4}$ the Quotient will be 21 ? *Answe.* $15\frac{3}{4}$.

41. What Number is that, which being multiplied by $\frac{2}{3}$ produceth $\frac{1}{4}$? *Answe.* $\frac{3}{8}$.

42. What Number is that, from which if you take $\frac{2}{3}$ of it-self, the Remainder will be 12 ? *Answe.* 20.

43. What Part of 25 is $\frac{5}{8}$ of an Unit ? *Answe.* $\frac{1}{40}$.

44. What Number is that, to which if you add its own $\frac{2}{3}$ the Whole shall be 20 ? *Answe.* 12.

45. What Number is that, which maketh 9 to be the $\frac{2}{3}$ of it ? *Answe.* $13\frac{1}{2}$.

46. If a Cannon may be discharged at twice with 6*lb.* of Powder ; how many Times will 7*C.* 3*qrs.* 17*lb.* discharge the same Piece ? *Answe.* 295 Times.

47. If $\frac{3}{8}$ of a Ship be worth 3740*l.* what is the whole Worth ? *Answe.* 9973*l.* 6*s.* 8*d.*

48. A young Man received 210*l.* which was $\frac{2}{3}$ of his elder Brother's Portion ; now three times the elder Brother's Portion was half of the Father's Estate ; I demand how much the Estate was ? *Answe.* 1890*l.*

49. A Factor bought a certain Quantity of broad Cloth, and Drugget, which together cost himt 81*l.* The Quantity of broad Cloth that he bought was 50 Yards, at 18*s.* per Yard, and for every five Yards of broad Cloth, he had nine Yards of Drugget ; I demand how many Yards of Drugget he had, and how much the Drugget cost him per Yard ? *Answe.* 90 Yards of Drugget, at 8*s.* per Yd.

50. A certain Usurer lent out 90*l.* for 12 Months, and received Principal and Interest 95*l.* 8*s.* I demand at what Rate per Cent. he received Interest? *Answe.* 6*l.* per Cent.

51. Two Men depart both from one Place, the one goes North, and the other South, the one goes 7 Miles a Day, and the other 11 Miles a Day; how far are they distant the 12th Day after their Departure? *Answe.* 216 Miles.

52. A Merchant bought 8 Tuns of Wine, which having received Damage, he selleth for 400*l.* and 12*l.* per Cent. Loss; I demand how much it cost him per Tun, and how he sold it per Gallon, to lose after the said Rate?

Answe. { Cost -- 56*l.* 0*s.* 0*d.* per Tun.

Answe. { Sold at 0*l.* 3*s.* 11*d.* 2*qrs.* $\frac{960}{2016}$ per Gallon.

53. Two Men depart both from one Place, and both go the same Road; the one travels 12 Miles every Day, the other 17 Miles every Day; how far are they distant the tenth Day after their Departure? *Answe.* 50*l.* Miles.

54. If a Gentleman hath an Estate of 1000*l.* per Ann. how much may he spend one Day with another, to lay up threescore Guineas at the Year's End? *Answe.* 2*l.* 11*s.* 4*d.* $\frac{40}{365}$.

55. If 76*lb.* of Cinnamon cost 40*l.* 10*s.* 8*d.* and 1 C.wt. of Nutmegs 59*l.* 14*s.* 8*d.* I demand the Price of 3*oz.* one with another? *Answe.* 2*s.*

56. A Grocer deliver'd 17*C.* 3*qrs.* 10*lb.* of Tobacco in the Roll to be cut and dried, and when it came home, it held out 16*C.* 0*qr.* 14*lb.* I demand how much was lost in every *lb.* and also supposing it cost in the Roll 8*d.* $\frac{6}{7}$ per *lb.* and the cutting 1*d.* $\frac{5}{8}$ per *lb.* I demand what it now stands him in?

Answe. { Lost per *lb.* 1*oz.* 8*dr.* $\frac{1200}{1998}$.

Answe. { It stands him in 87*l.* 5*s.* 3*d.* 1*qr.* $\frac{16}{36}$.

57. If Tallow be sold for 4*d.* per *lb.* what is the Value of 3 Tubs, each 3*C.* 1*qr.* 10*lb.* Gross, Tare per Tub 25*lb*? *Answe.* 17*l.* 9*s.*

58. Shipt from Spain 10 Tuns of Wine, at 10*l.* Sterling per *Hbd.* paid Custom at the Port of London, 1*s.* per Gallon: The Charges for Lighterage, Cartage, and Porterage, amounted to 5*l.* afterwards by the Misfortune of a Pipe staving, containing 126 Gallons, I lost 59 Gallons; the next Day 28 Gallons more run out, and the Remainder of the Pipe not being Saleable, I threw it away: The Market-Price not running high, I sold the rest for 17*l.* per *Hbd.* I demand how much I gain'd or lost by the Sale of the said Wine? *Answe.* Gain'd 115*l.*

59. A Ship's Company took a Prize of 300*l.* which is to be divided among them, according to their Pay, and the Time they have been on board; the Officers and Midshipmen 5 Months, and the Sailors 3 Months. The Officers, one with another, had 40*s.* per Month: The Midshipmen 30*s.* per Month, and the Sailors 22*s.* There were 6 Officers, 12 Midshipmen, and 84 Sailors; what must each Party have of the Prize, and what each single Person?

	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>grs.</i>		<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>gr.</i>
<i>Answ.</i>	<i>The Officers</i>	144	4	7	$1\frac{2}{3}\frac{4}{5}$	24	0	9	0
	<i>Midshipmen</i>	108	3	5	$2\frac{6}{7}\frac{4}{5}$	9	0	3	1
	<i>Sailors</i>	- -	47	11	$11\frac{1}{2}\frac{8}{5}$	0	11	3	3

60. If 1000*lb.* of Beef, serve 240 Men 8 Days, how many *lb.* will serve 460 Men 10 Weeks? *Answ.* 16770*lb.* 13*oz.* $\frac{640}{1920}$.

61. What is the Amount of 1000*l.* for five Years and a Half, at $4\frac{3}{4}$ per Cent. simple Interest? *Answ.* 1261*l.* 5*s.*

62. Sold Goods, amounting to the Value of 700*l.* for two $\frac{1}{2}$ Months; what is the present Worth, at 5 per Cent. simple Interest? *Answ.* 682*l.* 19*s.* 5*d.* 2*grs.*

63. A Merchant bought 400 Cloths, at 12*l.* per Cloth, which he shipped for Spain, to have Returns from thence, the one half in Wine, at 30*l.* per Tun, and the other half in Rice, at 28*s.* per C.wt. I demand how much of each must be return'd for the Cloths? *Answ.* 80 Tuns of Wine; and 3714*C.* 1*gr.* 4*lb.* of Rice.

64. A Tobacconist having several sorts of Tobacco, viz. of 12*d.* per *lb.* of 16*d.* per *lb.* of 18*d.* per *lb.* and of 2*s.* per *lb.* and he is desirous to make a Mixture of an *C.wt.* worth 20*d.* per *lb.* I demand how much of each sort must be taken?

	<i>lb.</i>	<i>oz.</i>	<i>d. per lb.</i>
<i>Answ.</i>	17	$3\frac{1}{2}\frac{8}{5}$	at 12
	17	$3\frac{1}{2}\frac{8}{5}$	at 16
	17	$3\frac{1}{2}\frac{8}{5}$	at 18
	60	$4\frac{2}{3}\frac{4}{5}$	at 24

65. A Brewer mixed 17 Gallons of Ale, at 8*d.* per Gallon with 19 Gallons at 10*d.* per Gallon, and with 40 Gallons, at 6*d.* per Gallon; I demand what one Gallon of this Mixture is worth; and also the Worth of the whole Quantity?

Answ. { 0*l.* 0*s.* 7*d.* 1*qr.* $\frac{60}{75}$ per Gallon.
{ 2*l.* 7*s.* 2*d.* the Price of the whole Mixture.

66. There are two Numbers, the one 48, the other twice as much; I demand the Difference between their Sum and Difference? *Answ.* 96.

67. There are two Numbers, the one 63, the other half as much ; I demand the Product of their Squares, and the Difference of their Product and Sum ?

Ans. $\left\{ \begin{array}{l} \text{Product of the Squares } 3938240.25 \\ \text{Difference } \dots \dots \dots 1890. \end{array} \right.$

68. There are two Numbers, the one 25, the other the Square of 25 ; I demand the Square-Root of the Sum of their Squares ? *Ans. 625.4998+*

69. There are two Numbers, whose Product is 1058, and Multiplicand 46 ; I demand the Multiplier ; the Sum of the Factors ; and the Difference between the Sum of the Cubes of the Factors, and the Square of the Product ?

Ans. $\left\{ \begin{array}{l} \text{Multiplier } \dots \dots \dots 23. \\ \text{Sum of the Factors } 69. \\ \text{Difference } 1009861. \end{array} \right.$

70. There are two Numbers, whose Dividend is 1216, and the Quotient 76 ; I demand the Divisor ; the Difference between the Cube of the Quotient, and the Sum of the Squares of the Divisor and Dividend ; and the Cube-Root of the Sum of the Cubes of the Divisor, Dividend, and Quotient ?

Ans. $\left\{ \begin{array}{l} \text{Divisor } \dots \dots \dots 16. \\ \text{Difference } 1039936. \\ \text{Cube-Root } \dots \dots \dots 1216. \end{array} \right.$

71. Two Men set out at the same time from the same Place, but go contrary Ways ; and they travel each of them 34 Miles a Day ; I demand the Time in which they will have travelled 2000 Miles ? *Ans. 29 days, 9 hrs. 52 min. $\frac{6}{7}$ sec.*

72. Six Rogues, *viz.* A, B, C, D, E, and F, having entered into a Confederacy, do agree to divide whatever Sums of Money they shall at any Time take upon the Highways, according to their Valour, that is, in proportion to the Number of Scars they should then have on their Faces : Now the first two, *viz.* A, and B, being very bold and daring Fellows, had received A 20, and B 19 Scars : The next two, *viz.* C, and D, having a less Share of Courage, and not caring to stand all Brunts, had each of them but 9 Scars ; but the other two, *viz.* E, and F, being mere Cowards, always turn'd their Backs at the least Opposition, and so by chance they had one a-piece ; and they having, at several Times, stolen the Sum of 700*l.* 13*s.* do desire to know how they must divide it ?

Ans.

	<i>l.</i>	<i>s.</i>	<i>d.</i>	<i>grs.</i>
A must have	237	10	2	0 ⁸ ₃₉
B	225	12	7	3 ⁴⁷ ₃₉
C	106	17	6	3 ³⁹ ₃₉
D	106	17	6	3 ³⁹ ₃₉
E	11	17	6	0 ²⁴ ₃₉
F	11	17	6	0 ²⁴ ₃₉

Answ.

73. There are three Numbers, 17, 19, and 48; I demand the Difference between the Sum of the Squares of the first and last, and the Cube of the Middlemost? *Answ.* 4266.

74. In 7 Cheeses, each weighing 1 C. 2 grs. 5 lb. how many Allowances for Sea Men may be cut, each weighing 5 oz. 7 drams? *Answ.* 3563¹⁵₈₇ Allowances.

75. In 81034 Rundlets of Brandy, each 18 Gallons, how many Gross of Bottles each $\frac{3}{2}$ of a Quart? *Answ.* 45581 gross, 7 doz. 6 Bottles.

76. In 731 doz. Bottles of Wine, each $1\frac{5}{7}$ Pint, how many Hhds? *Answ.* 29 bbd. 52 gal. 5 pints $\frac{5}{7}$.

77. Sold 8 C. $\frac{1}{2}$ of Steel at 12 d. per lb. how much Flemish Mony at 33 s. 8 d. per Pound Sterling, am I to receive for the same? *Answ.* 80 l. 2 s. 6 d. $\frac{96}{240}$. Flemish.

78. If 48 taken from 120 leave 72, and 72 taken from 91 leave 19, and 7 taken from thence leave 12; what Number is that, out of which, when you have taken 48, 72, 19, and 7, leaves 12? *Answ.* 158.

79. A hath $\frac{1}{2}$ of a Ship, B $\frac{1}{4}$, C $\frac{1}{16}$, D $\frac{3}{16}$; the Master clears 120 l. how much must each Owner have?

	<i>l.</i>	<i>s.</i>	<i>d.</i>
A must have	60	0	0
B	30	0	0
C	7	10	0
D	22	10	0

Answ.

80. A Gentleman having 50 s. to pay among his Labourers for a Day's Work, would give to every Boy 6 d. to every Woman 8 d. and to every Man 16 d. the Number of Boys, Women, and Men, was the same? I demand the Number of each? *Answ.* 20 of each sort.

81. A Gentleman had 7 l. 17 s. 6 d. to pay among his Labourers; to every Boy he gave 6 d. to every Woman 8 d. and to every Man 16 d. and there were for every Boy three Women, and for every Woman two Men; I demand the Number of each? *Answ.* 15 Boys, 45 Women, and 90 Men.

82. Admit

82. Admit a Tax of 39*l.* is laid on a Town for the building of a Bridge, and the Value of the Town-Rent is 900*l. per Ann.* what shall a Man pay towards it, whose Income is worth 100*l. per Ann.*? *Ans*w. 4*l. 6 s. 8 d.*

83. Suppose *A* hath an Estate of 53*l. per Ann.* and pays 5*s. 10 d.* to a Subsidy; what shall *B* pay, whose Estate is worth 100*l. per Ann.*? *Ans*w. 11*s. 0 d. $\frac{4}{3} s.$*

84. If 136*l.* are to be divided between two Men, so as the lesser Share may have such Proportion to the greater, as 2 to 5, what must each Man have?

l. s. d. qrs.
*Ans*w. { One must have 38 17 1 2 $\frac{6}{7}$
{ The other - - 97 2 10 1 $\frac{1}{7}$

85. There are 1000*l.* to be divided among 3 Men, in such Manner, that if *A* have 3*l.* *B* shall have 5*l.* and *C* 8*l.* how much must each Man have?

l. s.
*Ans*w. { A must have 187 10
{ B - - - - 312 10
{ C - - - - 500 0

86. Shipt for *Jamaica* 550 Pair of Stockings, at 11*s. 6 d.* per Pair, and 460 Yards of Stuff, at 14*d. per Yard*; in return for which, I had 46 C. 3 qrs. of Sugar, at 24*s. 6 d. per C.* and 1570*lb.* of Indigo, at 2*s. 4 d. per lb.* what remains due to me of my Adventure? *Ans*w. 102*l. 12 s. 11 d. 2 qrs.*

87. If one Pound ten, and forty Groats

Will buy a Load of Hay;

How many Pounds with nineteen Crowns

For twenty Loads will pay? *Ans*w. 38*l. 11 s. 8 d.*

88. A Man driving his Geese to the Market, was met by another, who said, Good-morrow Master with your Hundred Geese. Says he, I have not an Hundred; but if I had half as many as I now have, and the Square of two more, beside the Number I have already, I should have an Hundred: How many had he? *Ans*w. 64.

89. If a Tower be 384 Feet high from the Foundation, and a sixth Part be under the Earth, and an eighth Part under the Water; how much in heighth is visible? *Ans*w. 272 Feet.

90. A Merchant would lay out in Spices 560*l.* at the following Prices, *viz.* Cloves at 4*s. per lb.* Mace at 7*s.* Cinnamon at 3*s.* Nutmegs at 12*s.* and Pepper at 2*s. per lb.* and he would have an equal Quantity of each Sort; I demand that Quantity? *Ans*w. 400*lb.* of each Sort.

91. The computed Distance between *London* and *York* is 150 Miles; now if a Man set out from *London*, and walk every Day toward *York* 20 Miles, and back again toward *London* 15 Miles; how long will it be before he gets to his Journey's End? *Answe.* 30 Days.

92. Bought 127 Pieces of Cloth for which I delivered 3589 Ells of *Holland* at 7s. 11d. per Ell *English*; what cost a Piece of that Cloth? *Answe.* 11L 3s. 8d. 2qrs. $\frac{9}{127}$.

93. The Account of a certain School is as followeth; *viz.* $\frac{1}{16}$ of the Boys learn Geometry, $\frac{3}{8}$ learn Grammar, $\frac{3}{10}$ learn Arithmetic, $\frac{3}{20}$ learn to write, and 9 learn to read; I demand the Number of each? *Answe.* 5 *Geometers*, 30 *Grammarians*, 24 *Aritbmeticians*, 12 *Writers*, and 9 *Readers*.

94. I have laid out for a Merchant 638L 17s. 3d. he allows me $2\frac{3}{4}$ per Cent. before that, I owed him 184L 17s. 9d. how much is he indebted to me? *Answe.* 471L 10s. 10d. 1qr.

95. Bought a Tun of Wine for 78L 17s. at what Price must I sell it per Quart to gain 5L 10s. by the Whole, when there were 22 Gallons leaked out? *Answe.* 22d. +

96. If out of 10s. per Week I lay up 4d. 2qrs. per Day, Sundays excepted; and have saved 9L 2s. 3d. how long was I in laying it up; and how much have I spent in that Time?

Answe. { 567 Days in laying up.
{ 31L 7s. 9d. spent.

97. If I buy 1000 Ells *Flemish* of Linen for 90L what may I sell it per Ell in *London* to gain 10L by the Whole? *Answe.* 3s. 4d. per Ell.

98. Bought threescore Pieces of *Holland* for three times as many Pounds, and sold them again for four times as much; but if they had cost me as much as I sold them for, what should I have sold them for, to gain after the same Rate? *Answe.* 320L

99. There are three Quantities of Silver, each of the same Weight, but different in Value; the Weight of each Quantity is 10oz. the Value of the first Sort is 4s. per oz. of the second 4s. 6d. per oz. and of the third 5s. per oz. I demand the Worth of an Oz. when they are all melted down together? *Answe.* 4s. 6d. per oz.

100. I have received Advice from my Factor, that he has disbursed upon my Account, the Sum of 4000 Guilders, 15 Stivers; I demand what Sum I must answer for that in *English* Money, Exchange at Par; and also what his Commission comes to at 2 per Cent.?

Answe. { 400L 1s. 6d. *Sterling*.
{ 8L 0s. 0d. 1qr. *Commission*.

101. A Merchant bought a Parcel of Jewels for 220*l.* and sold them again for 440*l.* payable at the End of 6 Months; I demand what the Gain was worth in ready Money, Rebate being made at 6 per Cent.? *Answe.* 213*l.* 11*s.* 10*d.* +

102. A Factor bought 4 Chests of Sugar, the Mark and Weight as follows;

C. qrs. lb.

A	-	-	10	3	14
B	-	-	12	1	17
C	-	-	13	1	19
D	-	-	14	2	10

now supposing the Tare or Weight of every Chest, when it is empty, to be 3*lb.* I demand the Neat Weight of the said Sugar; also I demand the Prime Cost of the same, supposing it came to 18*s.* per C. including the Charges of Lighterage, Porterage, Warehouse-Room, Custom, &c. also I demand the whole Gain, and the Gain per Cent. supposing the Chests A and B were sold afterwards at 28*s.* per C. and the other two Chests, viz. C and D at 4*d.* per *lb.*

		I.	s.	d.
<i>Answe.</i>	Prime Cost	-	-	42 4 $\frac{1}{2}$
	Whole Gain	-	-	34 16 $\frac{1}{2}$
	Gain per Cent.	-	-	82 8 $\frac{3}{4}$

103. A poor Woman carrying some Eggs to Market, met with a rude Fellow, who broke them all; but presently after, considering what he had done, went back and told the Woman he was willing to make Satisfaction, provided she could tell how many there were; she answered, she could not tell, but the best Account that she could give, was, that when she told them in by two at a time, there was one left, when by three, there was one left, and when by four, there was one left; but when she told them in by five, there was none left; I demand how many Eggs the Woman had? *Answe.* 25.

104. A Gentleman a Chaise did buy,

An Horse and Harness too;

They cost the Sum of threescore Pounds,

Upon my Word 'tis true.

The Harness came to half of th' Horse;

The Horse twice of the Chaise;

And if you find the Price of them,

Take them and go your Ways.

<i>Answe.</i>	Cbaise	-	-	-	15
	Horse	-	-	-	30
	Harness	-	-	-	15

A short Collection of pleasant and diverting QUESTIONS

1. A General having a Castle, situate on a Square, and garrison'd by 48 Soldiers, so order'd them, as that any two Corners and the Side between them, should consist of 18 Men ; but he thinking there were not Men enow, hired 8 more, but still kept the same Number of 18 Men as before : Afterwards 16 Men were paid off, he not having Occasion for them ; but yet he kept up his Number of 18 Men ; I demand how he must place the said Men, to make 18 every Way, when he had 48, 56, and 40 Soldiers ?
2. Suppose the nine Digits to be placed in a quadrangular Form ; I demand in what Order they must stand, that any three Figures in a right Line may make just 15 ?
3. Let 12 be set down in four Figures, and let each Figure be the same.
4. A Country Man having a Fox, a Goose, and a Peck of Corn, in his Journey came to a River, where it so happened that he could carry but one over at a Time. Now, as no two were to be left together that might destroy each other : So he was at his Wits-end how to dispose of them : For says he, Tho' the Corn can't eat the Goose, nor the Goose eat the Fox, yet the Fox can eat the Goose, and the Goose eat the Corn. The Question is how he must carry them over ?
5. Three jealous Husbands with their Wives, being ready to pass by Night over a River, do find at the River-side a Boat which can carry but two Persons at once, and for want of a Waterman, they are necessitated to row themselves over the River at several Times : The Question is, how these 6 Persons shall pass by 2 and 2, so that none of the three Wives may be found in the Company of 1 or 2 Men unless her Husband be present ? *Wingate.*
6. Two merry Companions are to have equal Shares of 8 Gallons of Wine, which are in a Vessel containing exactly 8 Gallons : Now to divide it equally between them, they have only two other empty Vessels, of which 1 contains 5 Gallons, and the other 3 ; the Question is, how they shall divide the said Wine between them by the help of these 3 Vessels, so that they may have 4 Gallons a-piece ? *Wingate.*

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F I N I S.



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